



In cooperation with the
Lower Colorado River Authority

Peak-Flow Frequency for Tributaries of the Colorado River Downstream of Austin, Texas

Water-Resources Investigations Report 98–4015

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By William H. Asquith

U.S. GEOLOGICAL SURVEY

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**Austin, Texas
1998**

U.S. DEPARTMENT OF THE INTERIOR

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Peak-Flow Frequency for Tributaries of the Colorado River Downstream of Austin, Texas

By William H. Asquith

Abstract

A procedure to estimate the peak discharge associated with large floods is needed for tributaries of the Colorado River downstream of Austin, Texas, so that appropriate peak discharges can be used to estimate floodplain boundaries and used for the design of bridges and other structures. The U.S. Geological Survey, in cooperation with the Lower Colorado River Authority, studied flood peaks for streams in all or parts of 22 counties in that part of the Colorado River Basin extending downstream of Town Lake in Austin to the Gulf of Mexico. The study area was selected because the streams in this area either are tributaries to the Colorado River or have flood characteristics similar to those tributaries.

Peak-flow frequency for 38 stations with at least 8 years of data in natural (unregulated and nonurbanized) basins was estimated on the basis of annual peak-streamflow data through water year 1995. Peak-flow frequency represents the peak discharges for recurrence intervals of 2, 5, 10, 25, 50, 100, 250, and 500 years. The peak-flow frequency and drainage basin characteristics for the stations were used to develop two sets of regression equations to estimate peak-flow frequency for tributaries of the Colorado River in the study area. One set of equations was developed for contributing drainage areas less than 32 square miles, and another set was developed for contributing drainage areas greater than 32 square miles. A procedure is presented to estimate the peak discharge at sites where both sets of equations are considered applicable. Additionally, procedures are presented to compute the 50-, 67-, and 90-percent prediction interval for any estimation from the equations.

INTRODUCTION

The tributaries of the Colorado River downstream of Austin, Texas, are in an area subject to continentally generated storms and hurricanes. These storms occasionally produce local or widespread flooding, sometimes with little warning. Many storms exceeding 10 inches (in.) of precipitation have been documented in the area, including some exceeding 36 in. (Ellsworth, 1923). These storms typically produce large peak discharges that can threaten lives and property. A procedure to estimate the peak discharge associated with large floods is needed for tributaries in this area so that appropriate peak discharges can be used to estimate floodplain boundaries and used for the design of bridges and other structures.

In 1997, the U.S. Geological Survey (USGS), in cooperation with the Lower Colorado River Authority, studied flood peaks for streams in all or parts of 22 counties in the Colorado River Basin (watershed) extending downstream of Town Lake in Austin to the Gulf of Mexico. The study area (fig. 1) was selected because the streams either are tributaries to the Colorado River or have flood characteristics similar to those tributaries. Another study, conducted simultaneously with this one, documents peak-flow frequency along the main stem of the Colorado River downstream of Austin (Asquith, 1997).

The mean annual precipitation in the study area for 1951–80 ranges from about 32 in. in the Austin area to about 44 in. near the mouth of the Colorado River in the Gulf of Mexico (Riggio and others, 1987, p. 23). Recently, storms producing severe flooding have occurred in or near the study area (Liscum and East, 1994; National Oceanic and Atmospheric Administration, 1995; Hejl and others, 1996).

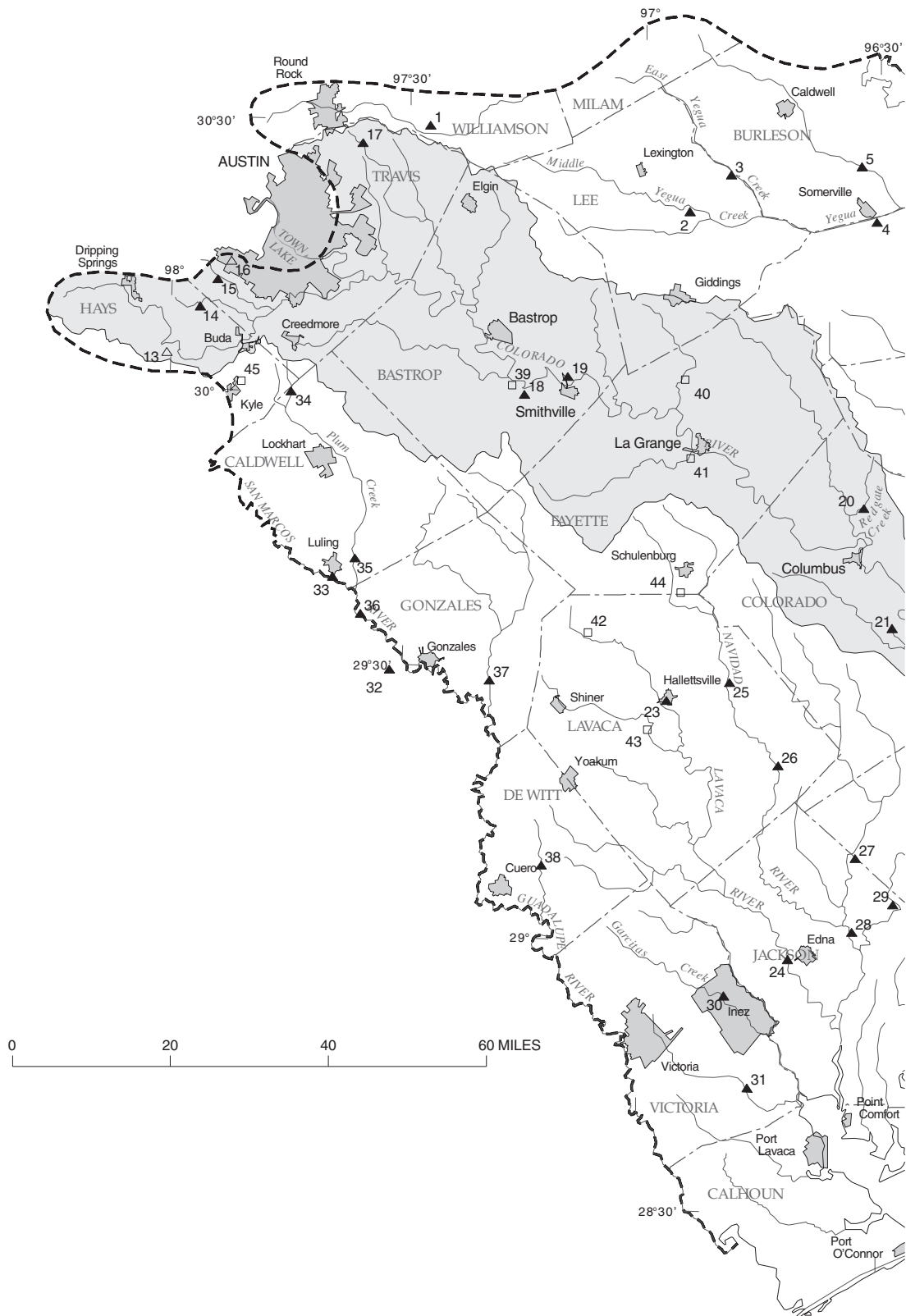
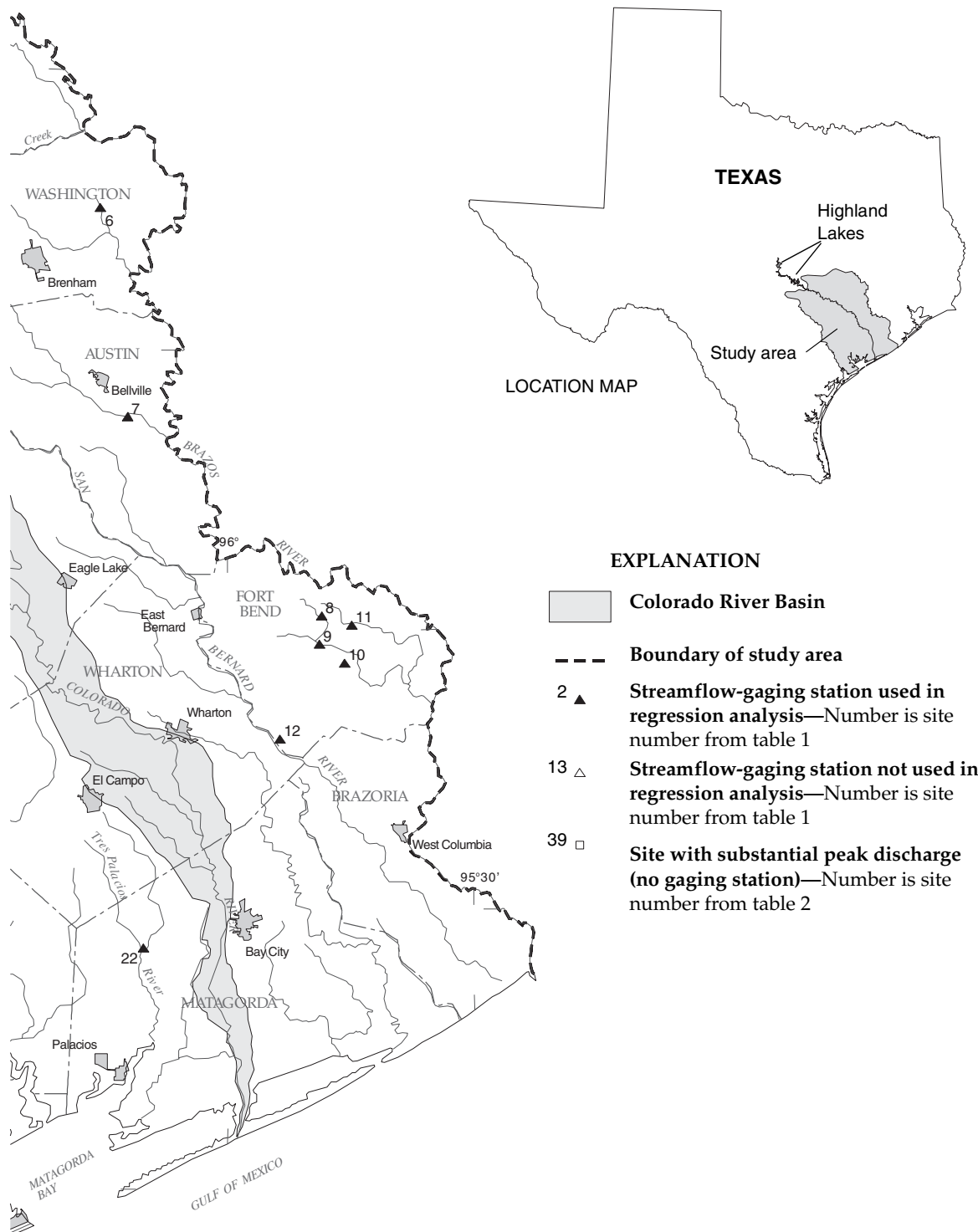


Figure 1. Location of streamflow-gaging stations and sites with substantial peak discharges in the vicinity of the



Colorado River Basin downstream of Austin, Texas.

Purpose and Scope

The purpose of this report is to present equations to estimate peak-flow frequency for tributaries of the Colorado River in the study area. These tributaries have natural drainage basins; a natural drainage basin is defined as having less than 10-percent impervious cover and less than 10 percent of its drainage area controlled by reservoirs. Peak-flow frequency in this report refers to the peak discharges for recurrence intervals of 2, 5, 10, 25, 50, 100, 250, and 500 years.

Peak-flow frequency for 38 streamflow-gaging stations (stations) with at least 8 years of data in natural (unregulated and nonurbanized) basins in the study area (fig. 1, table 1 at end of report) was estimated on the basis of annual peak-streamflow data through water year 1995. The peak-flow frequency was estimated following guidelines established by the Interagency Advisory Committee on Water Data (IACWD, 1982). One station, East Pecan Branch near Gonzales (site 32), lies just outside the study area, but was included in the data base. This station represents a small basin (defined in the "Peak-Flow Frequency Estimation" section), and its addition to the data base was considered necessary to increase data availability.

Equations to estimate peak-flow frequency were developed for streams with natural drainage basins in the study area. These equations were developed from selected stations based on the relation between peak-flow frequency and basin characteristics for each station. The entire period of systematic record (through 1995) was used in the frequency analysis for each qualified station except for stations with regulated streamflow during part of the record. These stations are Yegua Creek near Somerville (site 4) and Plum Creek near Luling (site 35). One or more reservoirs were constructed in the basins upstream of each of these stations during the period of systematic record, resulting in regulated annual peak discharges. The regulated data were excluded from the analysis.

Peak-Flow Frequency for Streamflow-Gaging Stations

Peak discharges are or have been monitored at each of the stations in the study area. These stations have various periods of systematic record (table 1). The peak discharges used in this study include the largest

peak discharge for each year of systematic record (annual peak discharge) and all known historical peak discharges through 1995. A historical peak discharge—documented by newspaper articles, personal recollections, or other historical sources—represents the largest peak discharge since a known date preceding the beginning of the systematic record. Historical peak discharges can occur before or within the systematic record. The historical record is the number of years represented by the historical peaks. For example, 33 years of systematic record (1963–95) exist for the station Davidson Creek near Lyons (site 5). However, the October 1994 peak discharge is the highest since at least 1902; thus, the 1994 peak is the largest in at least 94 years (1902–95).

The annual and historical peak discharges for each station were used, together with the USGS computer program PEAKFQ (Slade and Asquith, 1996), to estimate peak discharges for the 2-, 5-, 10-, 25-, 50-, 100-, 250-, and 500-year recurrence intervals (table 1). The computer program for peak-flow frequency analysis follows the guidelines established by the Interagency Advisory Committee on Water Data (1982) and uses the log-Pearson Type III (LPIII) frequency distribution.

The skew in the distribution of annual peaks is characterized by a skew coefficient. A reliable skew coefficient is difficult to estimate for stations having short records. Therefore, the IACWD recommends using a weighted skew coefficient with the LPIII distribution. This weighted skew coefficient is computed by weighting the skew coefficient calculated for a station (station skew coefficient) with a generalized skew coefficient representative of the surrounding area. The weighted skew coefficient is based on the inverse of the respective mean square errors for the station and on generalized skew coefficients. Generalized skew coefficients were determined in a previous study for stations in the study area (Judd and others, 1996). A weighted skew coefficient then was used in the calculation of the peak-flow frequency for each station except Dry Creek near Rosenberg (site 11). For this station, only the station skew coefficient was used because, compared to the weighted skew coefficient, it produces a better fit of the LPIII frequency curve to the data.

Additionally, the IACWD provides a procedure for estimating low-outlier thresholds; annual peak

discharges less than this threshold are excluded from the fitting of the LPIII frequency curve. The estimation of low-outlier thresholds is critical in the calculation of peak-flow frequencies. The IACWD procedure for estimating low-outlier thresholds is not always suitable for all stations in Texas because of the large variability and skewness of annual peaks at a single station. An equation to estimate low-outlier thresholds for Texas stations with natural basins was developed by Asquith and others (1995) and was used to estimate most low-outlier thresholds for the present investigation. The equation estimates low-outlier thresholds by using the mean, standard deviation, and skew of the logarithms for the systematic annual peak discharges. At one station—Mill Creek near Bellville (site 7)—the low-outlier threshold differed from the threshold from the equation. This alternative low-outlier threshold was identified by visually fitting the LPIII frequency curve to the peak-flow data.

Basin Characteristics for Streamflow-Gaging Stations

Selected basin characteristics were aggregated for each station (table 1). The characteristics selected for estimation of peak-flow frequency are from previous investigations of peak-flow frequency in Texas (Schroeder and Massey, 1977; Slade and others, 1995; Asquith and others, 1996). The 2-year 24-hour precipitation comes from Hershfield (1962). The mean annual precipitation comes from U.S. Geological Survey (1986, p. 432) and is for the period 1951–80. The contributing drainage area (CDA) represents the areal extent of the drainage basin. The stream length represents the length, in miles, of the longest mapped channel from the station to the drainage divide at the headwaters, based on USGS quadrangle maps (scale, 1:100,000). The basin shape factor is the ratio of the square of the stream length to the CDA; the shape factor represents the ratio of the longest stream length to the mean width of the basin. The stream slope is the ratio of the change in elevation of the longest mapped channel (from the station upstream to the drainage divide at the headwaters) to the stream length in feet per mile.

Large Recorded Floods

The USGS routinely has documented substantial peak discharges at stream sites without stations. Such sites in the Colorado River Basin downstream of Austin (from Asquith and Slade, 1995) are identified in figure 1 (sites 39–45), and ancillary information is listed in table 2 (at end of report). The relation to CDA of maximum peak discharge for the stations and substantial peak discharge at stream sites without stations is shown in figure 2. The relation provides an informative description of large recorded floods in the study area.

PEAK-FLOW FREQUENCY ESTIMATION

Development of equations for estimation of peak-flow frequency is a multistep process requiring investigation of the relation between peak discharge and selected basin characteristics. The following sections discuss multiple regression, the relation between the 100-year peak discharge and selected basin characteristics, prediction interval calculation, and application of the equations. A detailed example of peak-discharge estimation is available in the appendix.

Multiple-Regression Equations to Estimate Peak-Flow Frequency

Multiple-regression analysis was used to establish statistical relations between one dependent and one or more independent variables. The 2-, 5-, 10-, 25-, 50-, 100-, 250-, and 500-year peak discharges were used as dependent variables, and the selected basin characteristics were used as independent variables. Logarithmic transformations of the dependent and independent variables were used to increase linearity between variables. Logarithmic transformations traditionally have been used for hydrologic regression. In this report, logarithmic transformations are base 10 and are represented as “log.”

A forward-stepwise weighted least-squares (WLS) regression procedure was used for the development of the equations to estimate peak-flow frequency. In WLS regression, each data point can be assigned a weighting factor. The weights generally are representative of the relative accuracy of each value for the dependent variable; greater weights are assigned to values having greater accuracy.

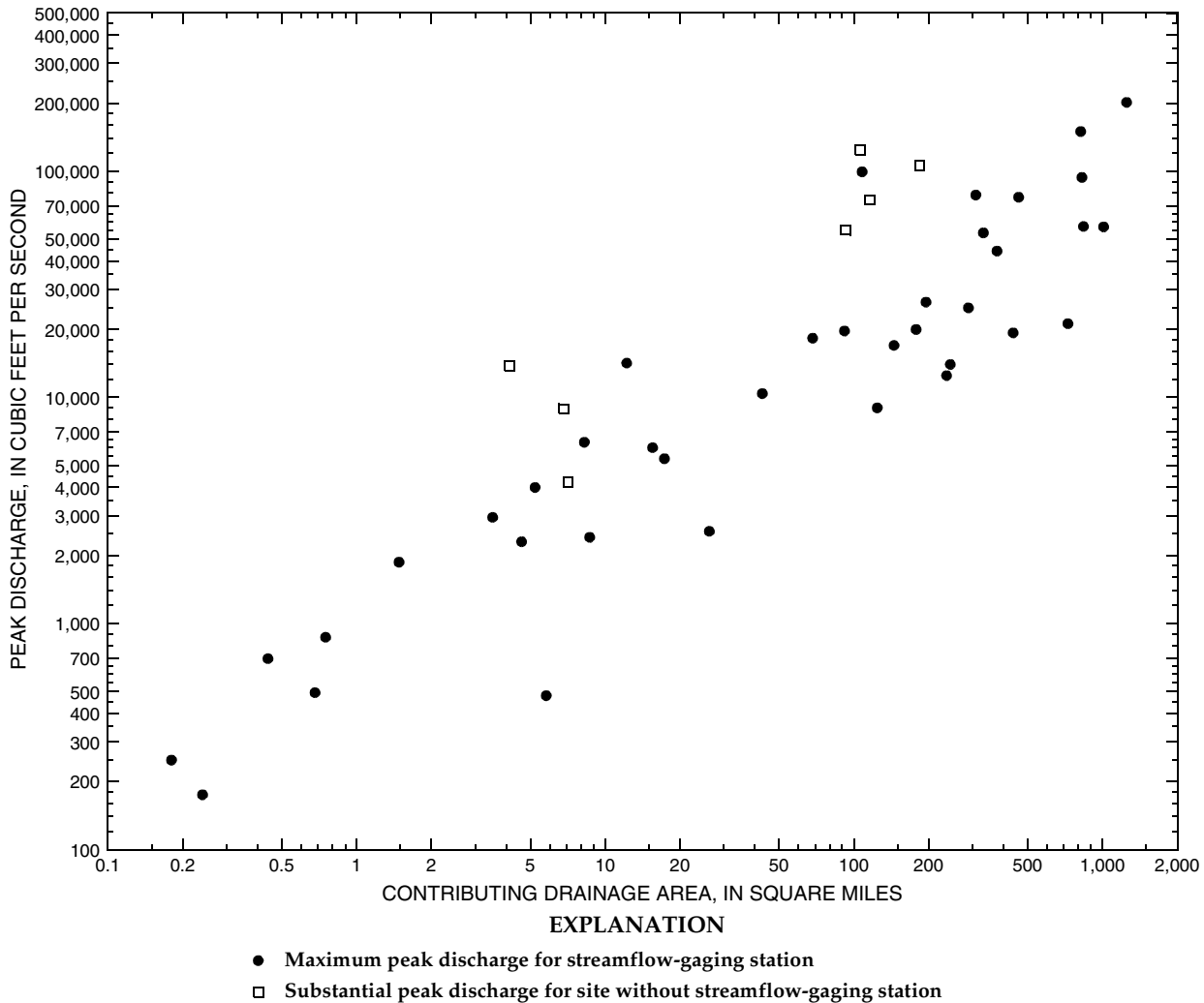


Figure 2. Large floods recorded in the Colorado River Basin downstream of Austin, Texas.

Empirical equations (G.D. Tasker, U.S. Geological Survey, written commun., 1994) based on Monte Carlo simulations (Tasker and Thomas, 1978; Stedinger and Cohn, 1986) were used to calculate a regression weight factor. The regression weight factor represents an equivalent “years of record” for each station with historical information. This factor is based on the length of systematic record, length of historical record, and number of high outliers; the regression weight factor for each station is listed in table 1. These factors were used as the weights for the WLS regression procedure in this report.

In forward-stepwise regression, the independent variable (basin characteristic) having the highest math-

ematical correlation to the dependent variable (peak-flow frequency) is entered into the equation, and successively, the remaining independent variables are tested for their statistical significance to the dependent variable. Each independent variable testing statistically significant (F ratio > 1.5) is entered into the equation. Thus, each independent variable in the final equation is considered statistically significant, and a basin characteristic’s inclusion into the equation contributes to the explanation of the variance in the dependent variable.

Before the final equations were developed, an investigation of the relation between the 100-year peak discharge (Q_{100}) and the principal physical basin

characteristics (CDA, stream slope, and basin shape factor) was conducted. The 100-year peak discharge was selected because this discharge information most often is needed by water managers and planners. Similar results, as described below, were recorded for the other recurrence intervals. The relation between Q_{100} and CDA, stream slope, and basin shape factor is presented in figure 3. Additionally, 16 stations (including Fox Branch near Oak Hill, site 16) with a CDA less than 32 square miles (mi^2), and 22 stations (including Onion Creek near Driftwood, site 13) with a CDA greater than 32 mi^2 are shown in figure 3. Hereafter, in this report, stations with a CDA less than 32 mi^2 are referred to as “small basin” stations, and stations with a CDA greater than 32 mi^2 are referred to as “large basin” stations. A study of peak-flow frequency conducted by Asquith and Slade (1997) indicates that a change in flood characteristics for many parts of the State occurs at CDA of about 32 mi^2 or 1.5 $\log\text{-mi}^2$.

The relation between Q_{100} and the basin characteristics indicates that a slight curvilinear relation exists between Q_{100} and CDA. By developing separate regression equations for the small and large basin stations, improved estimates of Q_{100} are calculated because of increased linearity (Asquith and Slade, 1997). Also, classifying the stations as “small” and “large” produces a change in the slope of the relation between Q_{100} and CDA. The slope (fig. 3b) is better correlated to Q_{100} for the large basins than for the small basins. The apparent change in the relation of stream slope between the large and small basins indicates that separate regression equations would improve Q_{100} estimation.

Also in figure 3b the relation between stream slope and Q_{100} is proportional for each CDA class (small and large basin stations)—larger slopes are associated with larger values of Q_{100} . However, if all the stations are considered together, then the apparent relation between Q_{100} and stream slope becomes inversely proportional—larger slopes are associated with smaller values of Q_{100} . Asquith and Slade (1997) found slope to be proportional to Q_{100} . It is thought that steep slopes produce more rapid runoff and therefore larger peak discharges. Thus, the classification of stations as small and large produces a stream slope and Q_{100} relation with some conceptualized physical basis.

Two stations were excluded from the regression analysis; Onion Creek near Driftwood (site 13) and one

of its tributaries, Fox Branch near Oak Hill (site 16). The watershed for each of these stations (fig. 1) lies entirely within the Texas Hill Country where topography and soil characteristics are significantly different than for the remaining stations in the study area. Both Onion Creek near Driftwood and Fox Branch near Oak Hill have stream slopes that are substantially different in comparison to other stations in their respective CDA classes (fig. 3b). Excluding these two stations reduces the number of stations available for the regression analysis to 15 small basin stations and 21 large basin stations.

Two sets of equations were developed using the 15 small basin and 21 large basin stations to estimate 2-, 5-, 10-, 25-, 50-, 100-, 250-, and 500-year peak discharges (table 3 at end of report). Of the six independent variables considered, stream length was excluded from the regression analysis because it correlates highly with the CDA. Many equations were developed for each recurrence interval using various combinations of the five remaining independent variables (2-year 24-hour precipitation, mean annual precipitation, CDA, basin shape factor, and stream slope) in the forward-stepwise regression procedure. CDA and stream slope consistently were the most significant independent variables. Additional basin characteristics were significant for some recurrence intervals but were not retained in the final equations. Testing of equations showed that if the independent variables were not consistent among the equations, some combinations of variable values can produce inconsistent peak discharges between recurrence intervals. For example, an inconsistent peak discharge would occur if the peak discharge for a given recurrence interval is less than the peak discharge for a smaller recurrence interval. Thus, only CDA and stream slope appear in the equations listed in table 3.

Discussion of Regression Equations

CDA proved to be the most significant variable in all the regression equations (table 3); whereas, stream slope proved to be the second most significant variable. Also, the exponents on CDA and stream slope are positive, which indicates that peak discharge is directly proportional to each of these characteristics. Additionally, the exponents on CDA and stream slope increase with increasing recurrence interval, a characteristic

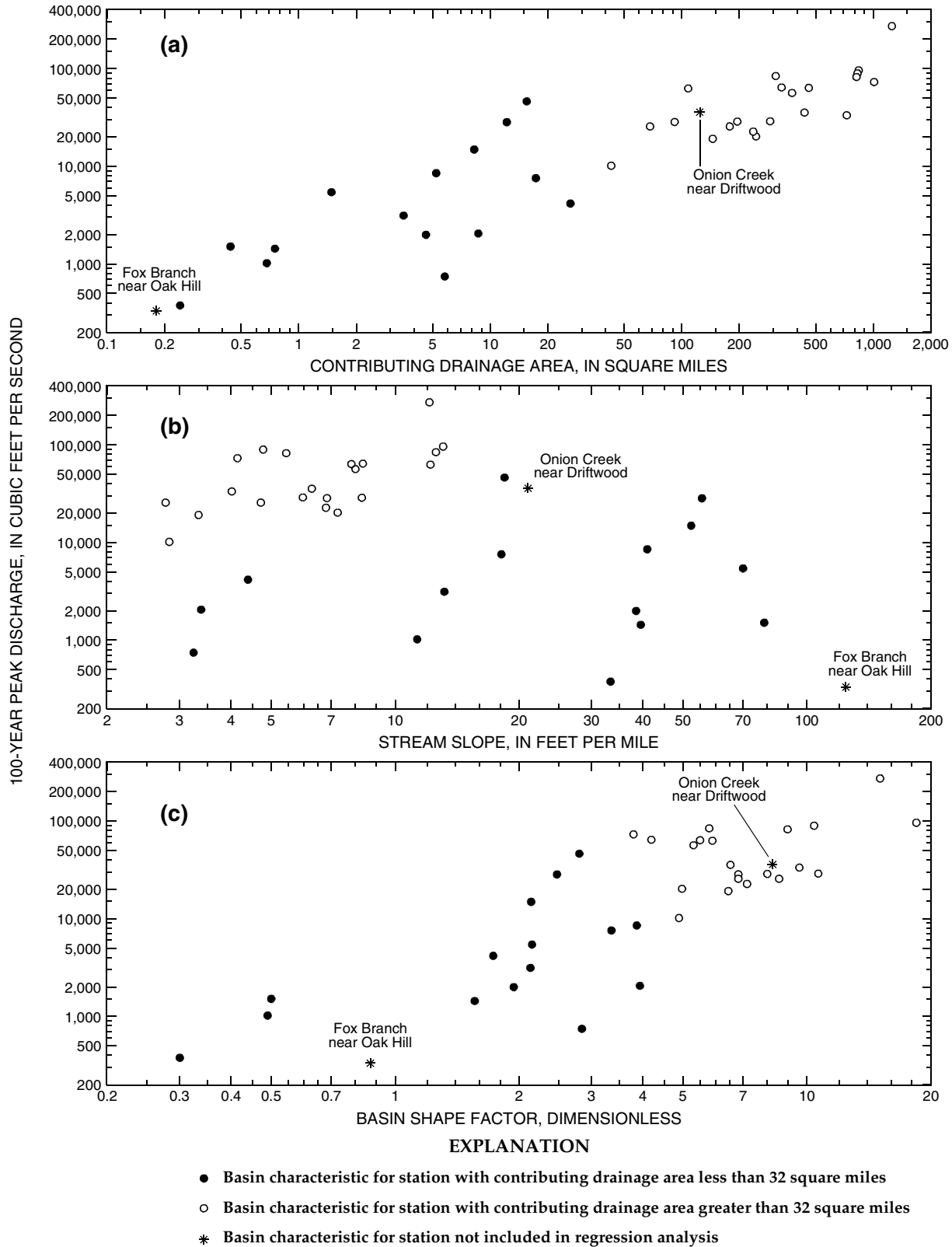


Figure 3. Relation between 100-year peak discharge and (a) contributing drainage area, (b) stream slope, and (c) basin shape factor for streamflow-gaging stations in the vicinity of the Colorado River Basin downstream of Austin, Texas.

frequently seen in peak-flow frequency equations (Schroeder and Massey, 1977; Slade and others, 1995; Asquith and others, 1996; and Asquith and Slade, 1997). The regression constants for each of the two sets of equations are similar as recurrence interval increases, which indicates that CDA and stream slope produce increasing peak discharge for increasing recurrence interval. The exponent on stream slope for each 2-year equation is considerably smaller than the analogous value for larger recurrence intervals (table 3). The influence of slope—as represented by large exponents—increases with increasing recurrence interval.

The (weighted) standard errors of estimate (standard deviation of residuals) for small basins generally are greater than the standard errors of estimate for large basins. The greater error is attributed to availability of short record (less than 20 years) for 13 of 15 small basin stations. Consequently, the peak-flow frequency for the short record stations shows greater variability. The mean record length for the small basin stations is about 14 years, whereas the mean record length for the large basin stations is about 33 years. Thus, the peak-flow frequency for the small basin stations has more potential error.

Finally, the standard error of estimate dramatically increases as the recurrence interval increases for the small basin stations (table 3), whereas the standard error remains relatively constant for the large basin stations. The increasing standard errors with recurrence interval for the small basins are also partially attributed to the short record availability, which results in increased extrapolation errors of the LPIII distribution for the larger recurrence intervals.

Prediction Intervals

The regression equations of table 3 list individual estimates of peak discharge, and the adjusted R-squared and (weighted) standard errors of estimate provide overall measures of equation accuracy. However, frequently the accuracy (error) of individual estimates from the equation is desired. As estimates are made for basin characteristics (independent variables) further “away” from the basin characteristics of the stations on which the regression is based, the accuracy of the estimate decreases. The means for evaluating the accuracy of any estimate from the equations is the cal-

culuation of the prediction intervals (Helsel and Hirsch, 1992, p. 241–242, 300).

The prediction interval of any discharge estimate for a site from the regression equations in table 3 is computed from the relation (Helsel and Hirsch, 1992, p. 300, sec. 11.4.4):

$$\begin{aligned} \log Q_T - t_{(\alpha/2, n-p)} \sqrt{s^2(1+h_o)} &\leq \log Q_T \\ &\leq \log Q_T + t_{(\alpha/2, n-p)} \sqrt{s^2(1+h_o)}, \end{aligned} \quad (1)$$

where

$\log Q_T$ = the logarithm of T-year recurrence interval peak discharge for a site from a regression equation, in log-cubic feet per second,

$t_{(\alpha/2, n-p)}$ = the critical value of t-distribution for a $100 \cdot (1-\alpha)$ -percent confidence interval,

n = the number of stations in a regression equation,

p = the number of independent variables (basin characteristics) plus one (for regression constant),

s^2 = the square of standard error of estimate, and

h_o = the leverage of the site.

The leverage of a site is an expression of the distance of the site’s basin characteristics from the center of the multidimensional space defined by the independent variables in the regression. The prediction interval is related directly to the square root of the magnitude of the leverage. The leverage of a site is computed by the following equation (Helsel and Hirsch, 1992, p. 300):

$$h_o = \mathbf{x}_o \{ \mathbf{X}^T \mathbf{W}^{-1} \mathbf{X} \}^{-1} \mathbf{x}_o^T, \quad (2)$$

where

\mathbf{x}_o = a row vector of the log basin characteristics for the site,

$\{ \mathbf{X}^T \mathbf{W}^{-1} \mathbf{X} \}^{-1}$ = the covariance matrix of the regression equation, and

\mathbf{x}_o^T = a column vector of the log basin characteristics of the site.

The covariance matrices for the regression equations are listed in table 4 (at end of report); the covariance matrices are in log-space. Critical values for the t-distribution for selected prediction intervals pertinent to the regression equations are also listed in table 4. Application of the above equations for prediction interval calculation is presented later.

Application of Regression Equations

The equations are designed to be used only for sites on the Colorado River tributaries in the study area. The equations are less applicable as the distance from the center of the study area increases. However, quantification of the diminishing applicability with increasing distance from the center of the study area is difficult. Also, the applicability of the equations for sites outside the study area is questionable.

In order to provide a smooth transition in determining peak discharge between small and large basins (separated at a CDA of 32 mi²), a weighted peak-discharge estimate is used for sites within a CDA interval of 10 to 100 mi² (Asquith and Slade, 1997, p. 12). The logarithmically-weighted peak discharge (eq. 3) is based on estimates from both the equation for CDA less than 32 mi² and the equation for CDA greater than 32 mi².

$$Q_{TW} = (2 - \log A)Q_{T1} + (\log A - 1)Q_{T2} , \quad (3)$$

where

Q_{TW} = the weighted peak discharge associated with the T-year recurrence interval, in cubic feet per second,

Q_{T1} = the peak discharge associated with the equation for sites with CDAs less than 32 mi², in cubic feet per second,

Q_{T2} = the peak discharge associated with the equation for sites with CDAs greater than 32 mi², in cubic feet per second, and

A = the CDA of the site, in square miles.

Since a weighted peak discharge is used for sites within the CDA range of 10 to 100 mi², a weighted prediction interval is needed as well. The prediction interval (see "Prediction Intervals" section) of a weighted peak discharge for a site within the 10- to 100-mi² CDA range is estimated by the following equations, which are constructed similar to equation 3:

$$Q_{TW-UP} = (2 - \log A)Q_{T1-UP} + (\log A - 1)Q_{T2-UP}, \text{ and} \quad (4)$$

$$Q_{TW-LOW} = (2 - \log A)Q_{T1-LOW} + (\log A - 1)Q_{T2-LOW} , \quad (5)$$

where

Q_{TW-UP} = the upper prediction interval of the Q_{TW} (eq. 3), in cubic feet per second,

Q_{T1-UP} = the upper prediction interval of the Q_{T1} (eq. 3), in cubic feet per second,

Q_{T2-UP} = the upper prediction interval of the Q_{T2} (eq. 3), in cubic feet per second,

Q_{TW-LOW} = the lower prediction interval of the Q_{TW} (eq. 3), in cubic feet per second,

Q_{T1-LOW} = the lower prediction interval of the Q_{T1} (eq. 3), in cubic feet per second, and

Q_{T2-LOW} = the lower prediction interval of the Q_{T2} (eq. 3), in cubic feet per second.

For sites at or near the stations included in the regression analyses, the peak discharge for such sites can be calculated from the regression equations (Q_T^r). However, the regression equations might provide estimates that conflict with those from the LPIII frequency analysis of the station data (Q_T^f). Thus, a weighted discharge (Q_T^w) calculated from Q_T^r and Q_T^f can be used. The weighted discharge is calculated from equation 6 in which the relative weights assigned to Q_T^r and Q_T^f are inversely related for the error variances (squared standard errors of estimate in log units) for the values of Q_T^r and Q_T^f .

$$Q_T^w = \frac{Q_T^r(SE_T^f)^2 + Q_T^f(SE_T^r)^2}{(SE_T^f)^2 + (SE_T^r)^2} , \quad (6)$$

where:

Q_T^w = the weighted peak-discharge estimate for recurrence interval T , in cubic feet per second,

Q_T^r = the peak-discharge estimate from regression, in cubic feet per second,

Q_T^f = the peak-discharge estimate from the LPIII frequency analysis, in cubic feet per second,

SE_T^f = the square standard error of the LPIII distribution, in log-cubic feet per second, and

SE_T^r = the square standard error from the regression, in log-cubic feet per second.

The standard error from the regression (SE_T^f) in the above equation is estimated from one-half the difference of the logarithmic 67-percent prediction interval,

$$\frac{1}{2}[\log(Q_T^r - Q_{T-HIGH}^{67 \text{ percent}}) - \log(Q_T^r - Q_{T-LOW}^{67 \text{ percent}})].$$

The standard error from the LPIII distribution is estimated as one-half the difference of the logarithmic 67-percent confidence limits, which can be determined from program PEAKFQ (confidence limits set at 83.5 percent¹ documented by Slade and Asquith (1996)).

Equation 6 provides a simple and convenient means of combining Q^r and Q^f ; however, the development of an always appropriate weighting procedure is difficult. The difficulties include: (1) the consideration of the number of years of record available at a station; peak discharges calculated from the regression equations are preferred in cases of very short record (about 15 years or less); (2) the consideration of the fit of the LPIII distribution to the station data; and (3) the knowledge that the presence of low and high outliers in the data can greatly affect the resulting LPIII distribution. Another difficulty in developing an always appropriate weighting procedure is how to quantify what is meant by “near” a station. The Q_T^f , derived from annual peak data, is increasingly less applicable for sites increasingly farther away (upstream or downstream) from the station.

A final consideration when using a specific equation for a specific site concerns the range in basin characteristics for which the equations are applicable. If a regression equation is used to estimate peak discharge for a site having a combination of basin characteristics substantially different from the stations on which the equation is based, erroneous estimates could result. Two techniques are available for evaluation of equation applicability. Each of these techniques involves analysis of the differences between the basin characteristics of the site and the basin characteristics involved in the regression. The first technique is to graphically compare the basin characteristics of the site with the characteris-

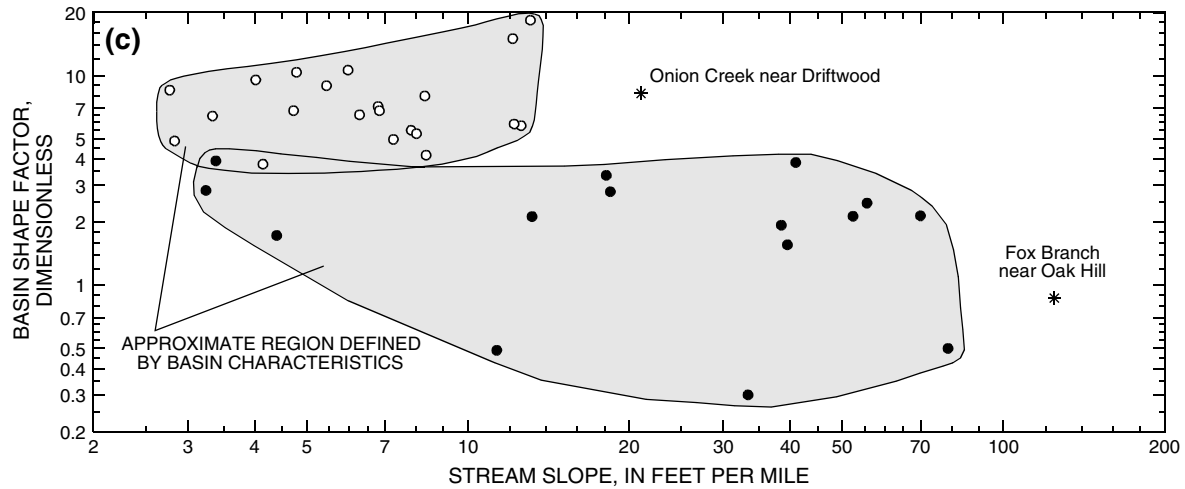
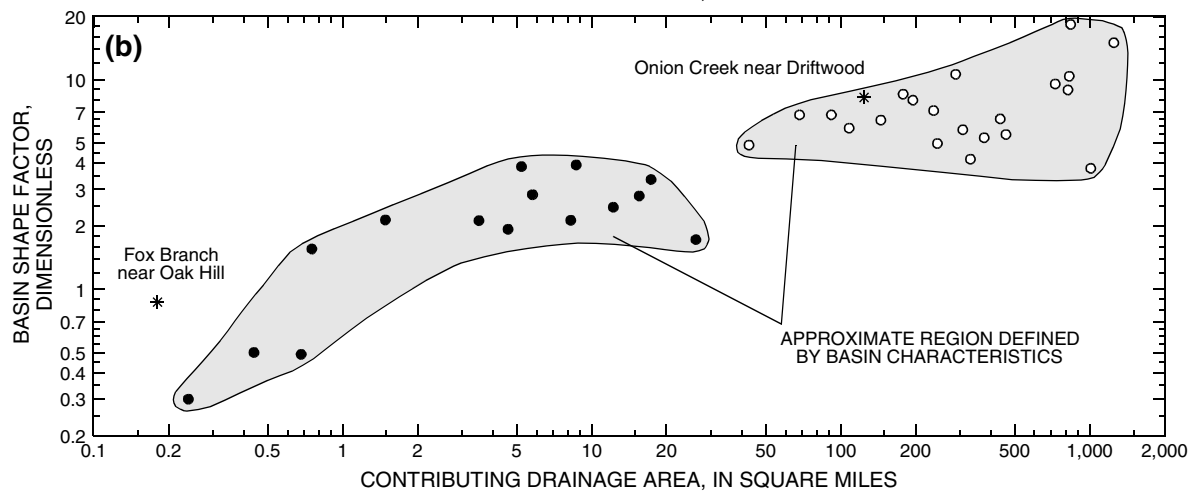
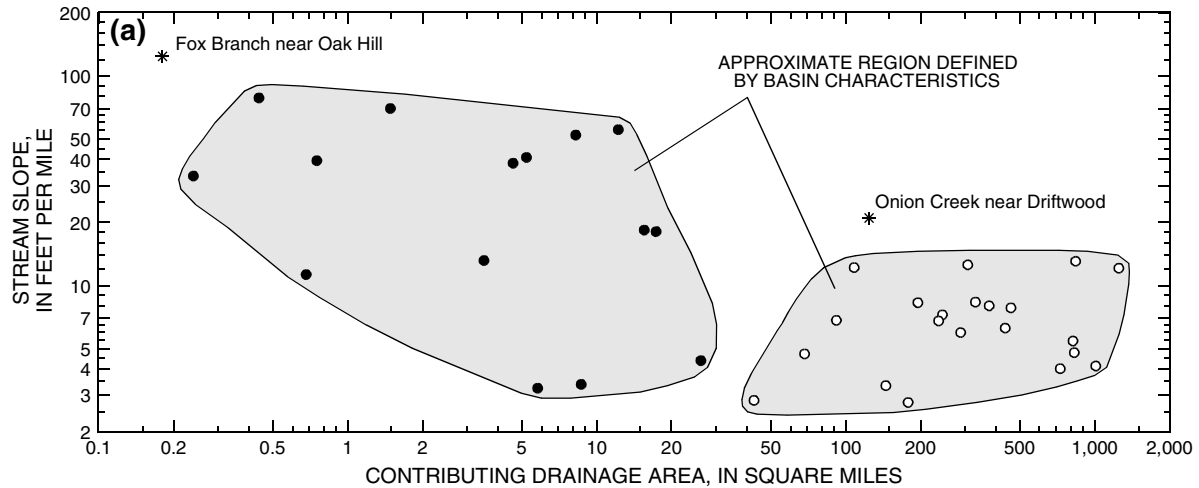
tics involved in the regression. The second technique is to compare the leverage of the site with the maximum or mean leverage of the stations in the regression.

The graphical technique for evaluating the applicability of an equation is done by using the relation among the basin characteristics involved in the regression equations; the internal relation among the basin characteristics (CDA, stream slope, and basin shape factor) is shown in figure 4. If the basin characteristics for a site plot near or outside the approximate region defined by the basin characteristics (indicated by the shaded area), the resulting peak discharge could be erroneous. Consequently, the equations become less applicable when the site basin characteristics plot farther away from the shaded areas. Although, basin shape factor does not appear in the equations, the shape factor is intrinsically involved because it was considered in the regression analysis. For example, if stations with substantially different shape factors were available in the study area, then shape factor could have proven statistically significant. Therefore, the applicability of the equations is reduced for sites having basin shape factors substantially different from those in the data base.

The second technique for evaluation of equation applicability uses the leverage statistic, h_o (eq. 2). Because leverage is a measure of the distance from the center of the multidimensional space defined by the basin characteristics involved in the regression analysis, the error of a peak-discharge estimate is directly proportional to the square root of leverage (eq. 1)—high leverage sites have large prediction intervals. The applicability of the equations diminishes as the site leverage increases. One guide in considering applicability of the equation is whether the site leverage is less than the maximum leverage of the regression. The maximum leverage for the small basin equations is 0.54, whereas the maximum leverage for the large basin equations is 0.38. Another guide in considering the equation applicability is whether the site leverage is less than 2 to 3 times the mean leverage. The mean leverage for the small basin equations is 0.24, whereas the mean leverage for the large basin equations is 0.14. More thorough discussion pertinent to interpretation of the leverage statistic is available in Helsel and Hirsch (1992, p. 300–305).

The most reliable peak-discharge estimates from the equations are for sites that plot within the shaded areas of figure 4 and have sufficiently small leverage

¹Program PEAKFQ uses a different definition of confidence limits than used in the current report. The 67-percent confidence limits of this report are the $\{100 - (100 - 67)/2\} = 83.5$ -percent confidence limits in PEAKFQ.



EXPLANATION

- Basin characteristic for station with contributing drainage area less than 32 square miles
- Basin characteristic for station with contributing drainage area greater than 32 square miles
- * Basin characteristic for station not included in regression analysis

Figure 4. Relation between (a) stream slope and contributing drainage area, (b) basin shape factor and contributing drainage area, and (c) basin shape factor and stream slope for streamflow-gaging stations in the vicinity of the Colorado River Basin downstream of Austin, Texas.

statistics. The reliability of peak-discharge estimates is questionable for sites that plot near or outside the shaded areas in figure 4 or for sites that have large leverage. However, it is difficult to determine for which sites the equations become unapplicable.

SUMMARY

Equations estimating peak-flow frequency are described for tributaries of the Colorado River in a study area encompassing all or parts of 22 counties downstream of Austin, Texas, to the Gulf of Mexico. The study area was selected because streams in the area are either tributaries to the Colorado River or have characteristics similar to the tributaries.

The peak-flow frequency was estimated for 38 qualified streamflow-gaging stations (stations) in the study area. Peak-flow frequency refers to the peak discharges for recurrence intervals of 2, 5, 10, 25, 100, 250, and 500 years. Qualified stations have at least 8 years of peak-flow data collected from natural basins. A natural drainage basin has less than 10-percent impervious cover and less than 10 percent of its drainage area controlled by reservoirs. The entire period of systematic record (through water year 1995) was used in the frequency analysis for each station, except at stations where streamflow was regulated during part of the record. Regulated data was excluded from the analyses.

Data from 36 of 38 stations were used to develop regressions equations to estimate peak-flow frequency. Multiple-regression analysis was performed using weighted least squares. Two sets of regression equations for peak-flow frequency were developed on the basis of the relation between peak-flow frequency and the basin characteristics of the stations. One set of equations was developed for contributing drainage area (CDA) less than 32 mi², and another set was developed for CDA greater than 32 mi². Procedures to compute the 50-, 67-, and 90-percent confidence limits for any estimation derived from the equations are presented. Additionally, a procedure is presented for determining a weighted discharge for sites where both sets of equations are applicable.

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Table 1. Selected basin characteristics and peak-flow frequency for streamflow-gaging stations in the vicinity of the Colorado River Basin downstream of Austin, Texas

[in., inches; FM, Farm Road; mi², square miles; mi, miles; ft/mi, feet per mile; yr, years; ft³/s, cubic feet per second; Q₅₀₀, 500-year peak discharge; Q₁₀₀, 100-year peak discharge]

Site no. (fig. 1)	Station no.	Station name	Latitude	Longitude	Available period of systematic record ¹	2-year 24-hour precipitation (in.)	Mean annual precipitation 1951–80 (in.)
1	08105900	Avery Branch near Taylor	30°29'11"	97°27'27"	1967–74	4.19	33.0
2	08109700	Middle Yegua Creek near Dime Box	30°20'21"	96°54'16"	1963–95	4.32	35.0
3	08109800	East Yegua Creek near Dime Box	30°24'26"	96°49'02"	1963–95	4.35	36.0
4	08110000	Yegua Creek near Somerville	30°19'18"	96°30'26"	1925–66 ²	4.39	36.0
5	08110100	Davidson Creek near Lyons	30°25'10"	96°32'24"	1963–95	4.42	36.0
6	08111100	Winkleman Creek near Brenham	30°15'19"	96°15'44"	1966–74	4.62	39.0
7	08111700	Mill Creek near Bellville	29°52'51"	96°12'18"	1964–93	4.60	40.0
8	08114900	Seabourne Creek near Rosenberg	29°31'27"	95°48'28"	1967–74	4.90	43.0
9	08115000	Big Creek near Needville	29°28'35"	95°48'45"	1947–95	4.88	43.0
10	08115500	Fairchild Creek near Needville	29°26'45"	95°45'41"	1945–54	4.92	43.0
11	08116400	Dry Creek near Rosenberg	29°30'42"	95°44'48"	1959–79	4.93	43.0
12	08117500	San Bernard River near Boling	29°18'48"	95°53'37"	1955–95	4.75	42.0
13	08158700	Onion Creek near Driftwood ³	30°04'59"	98°00'29"	1980–95	4.01	32.5
14	08158810	Bear Creek below FM 1826 near Driftwood	30°09'19"	97°56'23"	1979–95	4.06	33.0
15	08158840	Slaughter Creek at FM 1826 near Austin	30°12'32"	97°54'11"	1978–95	4.07	32.5
16	08158900	Fox Branch near Oak Hill ³	30°14'01"	97°52'29"	1966–74	4.08	32.0
17	08159150	Wilbarger Creek near Pflugerville	30°27'16"	97°36'02"	1964–80	4.15	32.0
18	08159450	Reeds Creek near Bastrop	30°00'26"	97°15'03"	1965–74	4.32	36.0
19	08160000	Dry Creek at Buescher Lake near Smithville	30°02'32"	97°09'34"	1940–66	4.35	36.5
20	08160800	Redgate Creek near Columbus	29°47'56"	96°31'55"	1962–95	4.60	40.5
21	08161580	Dry Branch tributary near Altair	29°34'39"	96°28'16"	1967–74	4.65	41.0
22	08162600	Tres Palacios River near Midfield	28°55'40"	96°10'15"	1971–95	4.79	42.0
23	08163500	Lavaca River at Hallettsville	29°26'35"	96°56'39"	1940–95	4.43	38.0
24	08164000	Lavaca River near Edna	28°57'35"	96°41'10"	1939–95	4.47	37.5
25	08164300	Navidad River near Hallettsville	29°28'00"	96°48'45"	1962–95	4.47	38.5
26	08164350	Navidad River near Speaks	29°19'18"	96°42'32"	1982–89	4.48	39.0
27	08164450	Sandy Creek near Louise	29°09'34"	96°32'47"	1980–95	4.60	41.0
28	08164500	Navidad River near Ganado	29°01'32"	96°33'08"	1939–80	4.57	40.0
29	08164503	West Mustang Creek near Ganado	29°04'17"	96°28'01"	1980–95	4.70	41.0
30	08164600	Garcitas Creek near Inez	28°53'28"	96°49'08"	1971–95	4.51	37.0
31	08164800	Placedo Creek near Placedo	28°43'30"	96°46'07"	1971–95	4.53	38.0
32	08169850	East Pecan Branch near Gonzales	29°29'58"	97°31'36"	1966–74	4.28	34.5
33	08172000	San Marcos River at Luling	29°39'54"	97°38'59"	1940–95	4.03	33.0
34	08172100	West Elm Creek near Niederwald	29°59'04"	97°44'39"	1966–74	4.16	34.0
35	08173000	Plum Creek near Luling	29°41'58"	97°36'12"	1930–63 ⁴	4.19	35.0
36	08173500	San Marcos River at Ottine	29°35'36"	97°35'22"	1916–43	4.10	33.5
37	08174600	Peach Creek below Dilworth	29°28'26"	97°18'59"	1960–79	4.32	36.5
38	08176200	Irish Creek near Cuero	29°08'02"	97°12'10"	1967–74	4.41	35.0

¹ Stations with available record ending 1995 were active as of 1996.

² Somerville Lake completed in 1967. Only peak discharges for 1925–66 used in analysis.

³ Station not used in regression analysis.

⁴ Many small reservoirs completed in 1964. Only peak discharges for 1930–63 used in analysis.

Table continued on next two pages.

Table 1. Selected basin characteristics and peak-flow frequency for streamflow-gaging stations in the vicinity of the Colorado

Site no. (fig. 1)	Contributing drainage area (mi ²)	Stream length (mi)	Basin shape factor (dimensionless)	Stream slope (ft/mi)	Available unregulated systematic record (yr)	No. of historical peaks	Historical record (yr)	Equivalent years of record (regression weight factor)
1 (Avery Branch-Taylor)	3.52	2.74	2.13	13.17	8	0	0	8
2 (Middle Yegua Creek-Dime Box)	236	41.08	7.15	6.79	33	1	83	51
3 (East Yegua Creek-Dime Box)	244	34.84	4.97	7.25	33	0	0	33
4 (Yegua Creek-Somerville)	1,009	61.83	3.79	4.14	42	0	0	42
5 (Davidson Creek-Lyons)	195	39.52	8.01	8.30	33	2	94	56
6 (Winkleman Creek-Brenham)	.75	1.08	1.56	39.49	9	0	0	9
7 (Mill Creek-Bellville)	376	44.62	5.30	8.01	30	0	0	30
8 (Seabourne Creek-Rosenberg)	5.78	4.06	2.84	3.24	8	0	0	8
9 (Big Creek-Needville)	42.8	14.47	4.89	2.83	48	0	0	48
10 (Fairchild Creek-Needville)	26.2	6.73	1.73	4.39	8	0	0	8
11 (Dry Creek-Rosenberg)	8.65	5.83	3.93	3.38	21	1	48	31
12 (San Bernard River-Boling)	727	83.45	9.58	4.01	41	0	0	41
13 (Onion Creek-Driftwood)	124	31.99	8.25	21.02	16	0	0	16
14 (Bear Creek-Driftwood)	12.2	5.49	2.47	55.55	17	1	81	40
15 (Slaughter Creek-Austin)	8.24	4.20	2.14	52.32	18	0	0	18
16 (Fox Branch-Oak Hill)	.18	.40	.87	124.32	9	0	0	9
17 (Wilbarger Creek-Pflugerville)	4.61	2.99	1.94	38.44	17	1	87	42
18 (Reeds Creek-Bastrop)	5.22	4.49	3.86	40.91	10	0	0	10
19 (Dry Creek-Smithville)	1.48	1.78	2.15	69.96	26	1	32	28
20 (Redgate Creek-Columbus)	17.3	7.61	3.35	18.11	34	0	0	34
21 (Dry Branch tributary-Altair)	.68	.58	.49	11.31	8	0	0	8
22 (Tres Palacios River-Midfield)	145	30.55	6.44	3.33	25	0	0	25
23 (Lavaca River-Hallettsville)	108	25.23	5.89	12.18	56	2	156	92
24 (Lavaca River-Edna)	817	85.59	8.97	5.44	57	3	116	80
25 (Navidad River-Hallettsville)	332	37.31	4.19	8.35	34	0	0	34
26 (Navidad River-Speaks)	437	53.39	6.52	6.27	8	0	0	8
27 (Sandy Creek-Louise)	289	55.48	10.65	5.97	16	0	0	16
28 (Navidad River-Ganado)	826	92.67	10.40	4.78	42	2	105	66
29 (West Mustang Creek-Ganado)	178	39.05	8.56	2.77	16	0	0	16
30 (Garcitas Creek-Inez)	91.7	24.98	6.81	6.83	25	2	93	51
31 (Placedo Creek-Placedo)	68.3	21.57	6.81	4.72	25	1	29	27
32 (East Pecan Branch-Gonzales)	.24	.27	.30	33.33	9	0	0	9
33 (San Marcos River-Luling)	838	124.26	18.43	13.07	56	0	0	56
34 (West Elm Creek-Niederwald)	.44	.47	.50	78.72	9	0	0	9
35 (Plum Creek-Luling)	309	42.30	5.79	12.56	34	1	96	56
36 (San Marcos River-Ottine)	1,249	137.12	15.05	12.11	28	0	0	28
37 (Peach Creek-Dilworth)	460	50.28	5.50	7.83	20	1	40	28
38 (Irish Creek-Cuero)	15.5	6.59	2.80	18.43	8	0	0	8

Continued from previous page.

River Basin downstream of Austin, Texas—Continued

Date of maximum peak discharge of record	Maximum peak discharge of record (ft ³ /s)	Peak discharge for indicated recurrence interval obtained from log-Pearson Type III frequency curve (ft ³ /s)								$\frac{Q_{500}}{Q_{100}}$
		2 yr	5 yr	10 yr	25 yr	50 yr	100 yr	250 yr	500 yr	
05/01/1972	2,950	691	1,188	1,580	2,147	2,619	3,135	3,697	4,519	1.44
12/22/1991	12,500	1,490	4,650	7,860	13,060	17,640	22,270	28,220	36,080	1.62
05/24/1975	14,000	2,150	5,290	8,129	12,480	16,200	20,280	24,690	31,020	1.53
07/01/1940	56,800	6,790	16,960	26,680	42,460	56,760	73,200	91,890	120,200	1.64
10/17/1994	26,400	3,660	8,160	12,100	18,070	23,180	28,810	34,960	43,890	1.52
03/24/1973	870	302	555	748	1,010	1,220	1,440	1,660	1,970	1.37
06/13/1973	44,400	13,630	22,840	29,890	39,800	47,870	56,510	65,760	79,010	1.40
06/13/1973	480	269	395	479	586	667	747	827	935	1.25
06/26/1960	10,400	2,520	4,200	5,470	7,240	8,660	10,170	11,770	14,050	1.38
05/18/1953	2,560	997	1,680	2,210	2,940	3,530	4,160	4,840	5,800	1.39
10/31/1959	2,410	689	995	1,220	1,530	1,790	2,060	2,350	2,760	1.34
06/28/1960	21,200	7,080	12,350	16,550	22,660	27,780	33,400	39,550	48,570	1.45
06/06/1985	8,990	2,680	7,380	12,120	20,080	27,440	36,030	45,890	60,980	1.69
1939	14,200	793	3,100	6,120	12,370	19,240	28,380	40,250	60,930	2.15
12/20/1991	6,330	718	2,240	3,990	7,280	10,650	14,920	20,230	29,120	1.95
09/04/1967	249	49	99	142	208	267	332	407	518	1.56
1921	2,300	596	980	1,240	1,550	1,780	2,000	2,210	2,480	1.24
05/16/1965	4,000	230	840	1,660	3,450	5,550	8,520	12,640	20,410	2.40
06/30/1940	1,870	226	756	1,390	2,590	3,840	5,440	7,440	10,790	1.90
05/22/1979	5,360	1,790	3,120	4,110	5,460	6,510	7,590	8,710	10,250	1.35
06/13/1973	495	133	283	417	626	811	1,020	1,260	1,620	1.59
10/17/1983	17,000	5,130	8,250	10,590	13,820	16,420	19,180	22,110	26,280	1.37
08/31/1981	99,500	7,720	16,210	24,070	36,880	48,740	62,750	79,220	105,300	1.68
10/19/1994	150,000	11,590	22,910	33,120	49,520	64,540	82,190	102,800	135,400	1.65
09/13/1974	53,500	9,710	19,800	28,370	41,240	52,250	64,420	77,800	97,460	1.51
05/14/1982	19,300	6,480	12,110	16,730	23,540	29,290	35,620	42,560	52,740	1.48
10/19/1994	24,900	5,050	9,410	13,090	18,670	23,530	29,010	35,170	44,480	1.53
1936	94,000	13,620	25,760	36,660	54,240	70,450	89,650	112,300	148,500	1.66
10/19/1994	20,000	3,850	7,540	10,790	15,870	20,410	25,650	31,650	40,920	1.60
06/12/1981	19,700	4,550	8,860	12,540	18,140	23,020	28,510	34,670	43,930	1.54
10/31/1981	18,300	5,930	10,300	13,610	18,170	21,810	25,630	29,650	35,270	1.38
09/13/1974	175	81	141	188	257	314	377	445	545	1.45
09/12/1952	57,000	10,250	23,090	35,250	55,330	74,000	96,100	122,000	163,000	1.70
05/15/1970	700	185	402	599	910	1,190	1,510	1,880	2,440	1.62
07/01/1936	78,500	6,330	15,590	25,370	43,160	61,240	84,260	113,300	162,900	1.93
05/29/1929	202,000	14,800	39,880	68,870	126,100	188,600	273,200	386,000	592,300	2.17
04/20/1977	76,800	7,420	16,040	24,060	37,170	49,280	63,570	80,300	106,700	1.68
05/10/1972	6,000	1,550	5,380	10,250	20,260	31,380	46,410	66,280	101,900	2.20

Table 2. Substantial peak discharges for sites without streamflow-gaging stations in the vicinity of the Colorado River Basin downstream of Austin, Texas

[mi², square miles; ft³/s, cubic feet per second]

Site no. (fig. 1)	Stream site name and approximate location	Latitude	Longitude	Contributing drainage area (mi ²)	Date of substantial peak discharge	Substantial peak discharge (ft ³ /s)
39	Little Piney Creek near Bastrop	30°01'00"	97°16'38"	7.08	05/12/1969	4,220
40	Rabbs Creek near Warda	30°01'50"	96°54'40"	92.8	06/30/1940	55,000
41	Buckners Creek near La Grange	29°53'07"	96°53'55"	184	06/30/1940	106,000
42	Youngs Branch near Moulton	29°33'50"	97°06'40"	6.8	06/30/1940	8,900
43	Rocky Creek near Hallettsville	29°23'10"	96°59'00"	116	06/30/1940	74,700
44	West Navidad River near Schulenburg	29°38'20"	96°55'00"	106	06/30/1940	124,000
45	Bunton Branch near Kyle	30°01'00"	97°51'00"	4.12	06/30/1936	13,800

Table 3. Weighted least-squares regression equations for estimation of peak-flow frequency for the Colorado River Basin downstream of Austin, Texas

[mi², square miles; yr, year; CDA, contributing drainage area in square miles; SL, stream slope in feet per mile—ratio of change in elevation of (1) the length of the longest mapped channel to (2) the distance from the longest mapped channel of the site (or station) to the headwaters; SH, basin shape factor—ratio of length of longest mapped channel (stream length) squared to contributing drainage area (dimensionless)]

Recurrence interval	Weighted least-squares regression equation for corresponding recurrence interval ¹ (cubic feet per second)	Range of indicated independent variables (units as noted)	Adjusted R-squared ²	Weighted standard error of estimate (percent)	Weighted standard error of estimate (log ₁₀ units)	No. of stations in equation
Sites³ with contributing drainage area less than 32 mi² (small basin stations)						
2 yr	$Q_2 = 176.4 \text{ CDA}^{0.611} \text{ SL}^{0.0460}$	CDA: 0.24 to 26.2 square miles	0.79	38	0.16	15
5 yr	$Q_5 = 139.3 \text{ CDA}^{0.701} \text{ SL}^{0.326}$.87	31	.13	Do.
10 yr	$Q_{10} = 126.8 \text{ CDA}^{0.744} \text{ SL}^{0.460}$	SL: 3.24 to 78.72 feet per mile	.85	38	.16	Do.
25 yr	$Q_{25} = 117.5 \text{ CDA}^{0.788} \text{ SL}^{0.594}$.79	51	.21	Do.
50 yr	$Q_{50} = 113.3 \text{ CDA}^{0.814} \text{ SL}^{0.676}$.75	63	.25	Do.
100 yr	$Q_{100} = 110.6 \text{ CDA}^{0.836} \text{ SL}^{0.746}$	SH: 0.30 to 3.93 dimensionless	.71	75	.29	Do.
250 yr	$Q_{250} = 108.9 \text{ CDA}^{0.856} \text{ SL}^{0.807}$.67	88	.33	Do.
500 yr	$Q_{500} = 107.9 \text{ CDA}^{0.879} \text{ SL}^{0.878}$.63	103	.37	Do.

Footnotes at end of table.

Table 3. Weighted least-squares regression equations for estimation of peak-flow frequency for the Colorado River Basin downstream of Austin, Texas—Continued

Recurrence interval	Weighted least-squares regression equation for corresponding recurrence interval ¹ (cubic feet per second)	Range of indicated independent variables (units as noted)	Adjusted R-squared ²	Weighted standard error of estimate (percent)	Weighted standard error of estimate (log ₁₀ units)	No. of stations in equation
Sites³ with contributing drainage area greater than 32 mi² (large basin stations)						
2 yr	$Q_2 = 460.6 \text{ CDA}^{0.379} \text{ SL}^{0.239}$	CDA: 42.8 to 1,249 square miles	0.32	57	0.23	21
5 yr	$Q_5 = 571.8 \text{ CDA}^{0.414} \text{ SL}^{0.407}$.54	43	.18	Do.
10 yr	$Q_{10} = 617.3 \text{ CDA}^{0.437} \text{ SL}^{0.499}$.63	38	.16	Do.
25 yr	$Q_{25} = 650.4 \text{ CDA}^{0.466} \text{ SL}^{0.598}$	SL: 2.77 to 13.07 feet per mile	.69	38	.16	Do.
50 yr	$Q_{50} = 662.6 \text{ CDA}^{0.486} \text{ SL}^{0.664}$.71	38	.16	Do.
100 yr	$Q_{100} = 667.0 \text{ CDA}^{0.506} \text{ SL}^{0.725}$.72	41	.17	Do.
250 yr	$Q_{250} = 665.4 \text{ CDA}^{0.525} \text{ SL}^{0.781}$	SH: 3.79 to 18.43 dimensionless	.73	41	.17	Do.
500 yr	$Q_{500} = 656.6 \text{ CDA}^{0.549} \text{ SL}^{0.849}$.72	43	.18	Do.

¹ Order of independent variables (basin characteristics) in each equation from left to right indicates the relative statistical significance of each independent variable to the dependent variable (peak-flow frequency).

² Presented so that equations based on different numbers of stations can be compared.

³ For stream sites with CDA within the range 10 to 100 mi², use equation 3 to calculate weighted discharge and equations 4 and 5 to calculate weighted prediction interval.

Table 4. Covariance matrices and critical values of the t-distribution for regression equations

[These matrices can be used to compute the prediction interval for any estimation from the regression equations (table 3). Qualifications as to which equations a matrix applies to are shown in this table. CDA, contributing drainage area; mi², square miles]

Matrix $\{X^T W^{-1} X\}^{-1}$							
	Sites with CDA less than 32 mi²			Sites with CDA greater than 32 mi²			
	Area	Slope	Constant	Area	Slope	Constant	
Area	0.28411	0.10328	-0.34482	Area	0.27877	-0.052138	-0.64721
Slope	.10328	.37361	-.59347	Slope	-.052138	1.1778	-.85108
Constant	-.34482	-.59347	1.1372	Constant	-.64721	-.85108	2.3593
Critical values of the t-distribution for selected confidence limits (two-tailed)							
	Sites with CDA less than 32 mi² Degrees of freedom = 12			Sites with CDA greater than 32 mi² Degrees of freedom = 18			
50 percent ($\alpha = 0.25$)	0.69548			0.68836			
67 percent ($\alpha = 0.165$)	1.0153			1.0012			
90 percent ($\alpha = 0.05$)	1.7823			1.7340			

Appendix— Example of Calculations

The following example illustrates the calculation of peak-flow frequency and prediction intervals for a site. The example involves the estimation of the 100-year peak discharge for a 50-mi² site with a stream slope of 10.5 feet per mile (ft/mi) and a basin shape factor of 5.0; additionally, the 67-percent prediction interval is desired. Because the CDA for the site is within the interval 10 to 100 mi², estimates are made from equations with CDA both less than and greater than 32 mi².

The estimate from the equation for CDA < 32 mi² (small basin estimate) is:

$$Q_{100<32} = 110.6 (50)^{0.836} (10.5)^{0.746} = 16,800 \text{ cubic feet per second (ft}^3/\text{s)}.$$

The estimate from the equation for CDA > 32 mi² (large basin estimate) is:

$$Q_{100>32} = 667 (50)^{0.506} (10.5)^{0.725} = 26,600 \text{ ft}^3/\text{s}.$$

Because the CDA of the site lies within the 10- to 100-mi² interval, the weighted estimate is:

$$Q_{100W} = [2 - \log(50)] (16,800) + [\log_{10}(50) - 1] (26,600) = 0.30 (16,800) + 0.70 (26,600)$$

$$Q_{100W} = 23,700 \text{ ft}^3/\text{s}.$$

A check on the applicability of the equations indicates that this site's basin characteristics plot in or near the shaded regions in figure 4. Notice that the site CDA and stream slope plot closer to the shaded region of the large CDA basins than to the shaded region of the small CDA basins; therefore, the large basin estimate has the larger weight factor (0.070) in the weighting equation than the small basin estimate (0.30). Thus, the large basin estimate is considered slightly more applicable than the small basin estimate.

The calculation of the 67-percent prediction interval for the large basin equation begins with calculation of the leverage, h_o , using the covariance matrix for sites with a CDA greater than 32 mi² from table 4. The \mathbf{x}_o vector for this site is $[\log(50) \log(10.5) 1]$ or $[1.6990 \ 1.0212 \ 1]$. The large basin leverage is:

$$h_o = [1.6990 \ 1.0212 \ 1] \begin{bmatrix} 0.27877 & -0.052138 & -0.64721 \\ -0.052138 & 1.1778 & -0.85108 \\ -0.64721 & -0.85108 & 2.3593 \end{bmatrix} \begin{bmatrix} 1.6990 \\ 1.0212 \\ 1 \end{bmatrix} = 0.27388 .$$

Now, using equation 1 with s^2 equal to $(0.17)^2$ or 0.0289 from table 3 and a critical value for the t-distribution of 1.0012 from table 4, the prediction interval is calculated from equation 1:

$$\log Q_{100>32-UP} = \log (26,600) + 1.0012 [0.0289 (1 + 0.27388)]^{0.5} = 4.6170 \text{ log-ft}^3/\text{s}$$

$$Q_{100>32-UP} = 41,400 \text{ ft}^3/\text{s}.$$

$$\log Q_{100>32-LOW} = \log (26,600) - 1.0012 [0.0289 (1 + 0.27388)]^{0.5} = 4.2328 \text{ log-ft}^3/\text{s}$$

$$Q_{100>32-LOW} = 17,100 \text{ ft}^3/\text{s}.$$

There is a 67-percent chance that this prediction interval contains the true 100-year peak discharge for this site and equation, and the true discharge falls within the interval 17,100 to 41,400 ft³/s. However, because this site lies within the CDA range of 10 to 100 mi², and two separate equations are considered applicable; the weighted prediction intervals are needed (eqs. 4 and 5). The 67-percent prediction interval for the 100-year peak discharge for a site with less than 32 mi² are (eq. 1):

$$\log Q_{100<32-UP} = \log (16,800) + 1.0153 [0.0841 (1 + 0.32152)]^{0.5} = 4.5638 \text{ log-ft}^3/\text{s}$$

$$Q_{100<32-UP} = 36,600 \text{ ft}^3/\text{s}.$$

$$\log Q_{100<32-LOW} = \log (16,800) - 1.0153 [0.0841 (1 + 0.32152)]^{0.5} = 3.8868 \text{ log-ft}^3/\text{s}$$

$$Q_{100<32-LOW} = 7,710 \text{ ft}^3/\text{s}.$$

The weighted prediction interval is calculated using the weighting equations 4 and 5:

$$Q_{100W-UP} = [2 - \log (50)] (36,600) + [\log (50) - 1] (41,400) = 0.30 (36,600) + 0.70 (41,400)$$

$$Q_{100W-UP} = 39,960 \text{ ft}^3/\text{s}.$$

$$Q_{100W-LOW} = [2 - \log (50)] (7,710) + [\log (50) - 1] (17,100) = 0.30 (7,710) + 0.70 (17,100)$$

$$Q_{100W-LOW} = 14,300 \text{ ft}^3/\text{s}.$$

The prediction interval constructed for a prediction from any one regression equation can be statistically interpreted. However, the weighted prediction interval is only estimated, and therefore strict statistical interpretation of it requires relaxation.

A check on the leverage statistics on the large basin equation indicates that the site leverage (0.27) is less than the maximum leverage (0.38) and less than 2 to 3 times the mean leverage (0.28 to 0.42). A check on the leverage statistics on the small basin equation indicates that the site leverage (0.32) is less than the maximum leverage (0.54) and less than 2 to 3 times the mean leverage (0.48 to 0.72). The two site leverages (0.27 and 0.32) cannot be compared to each other to determine which equation is the most applicable for a site. Both sets of equations are considered applicable because both site leverages are sufficiently less than the maximum leverage and less than 2 to 3 times the mean leverage of their respective equations.