

SPARROW Surface Water Quality  
Workshop  
October 29-31, 2002  
Reston, Virginia

Section 7. SPARROW Model Applications

# Section 7. SPARROW Model Applications

## Topics for Consideration

- Prediction statistics
- Management applications
- Uncertainty analysis
- Web access to SPARROW applications

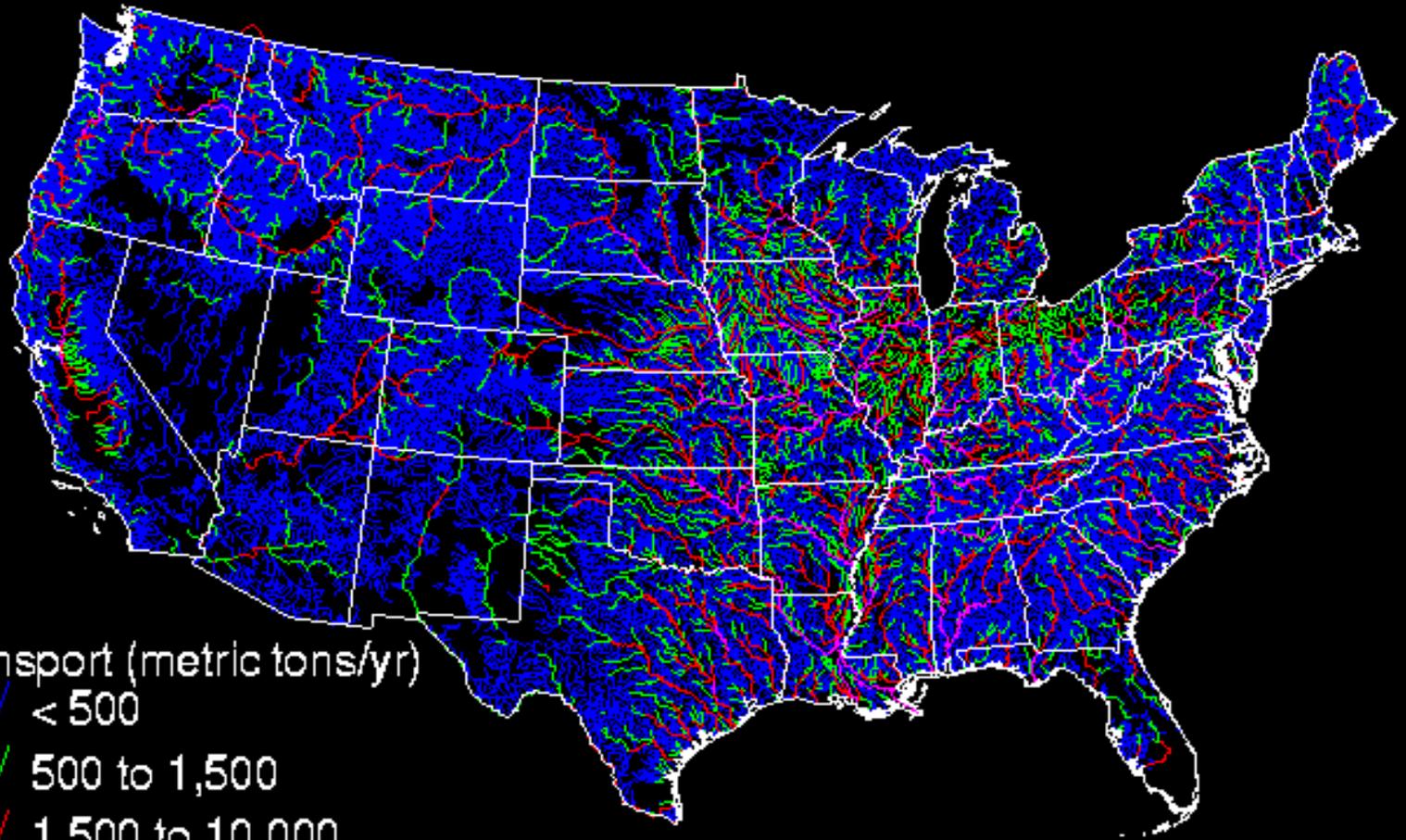
# SPARROW Prediction Statistics

## (Mean & Percentiles)

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- Loads/yields exported from watersheds
- Contaminant losses in streams and reservoirs
- Loads/yields delivered to downstream sites (e.g., estuaries, reservoirs)
- Contaminant sources and budgets
- Concentration
- Probability of exceeding environmentally relevant load/concentration thresholds

# SPARROW Predictions of Total Nitrogen Transport in Rivers of the Conterminous United States



Transport (metric tons/yr)

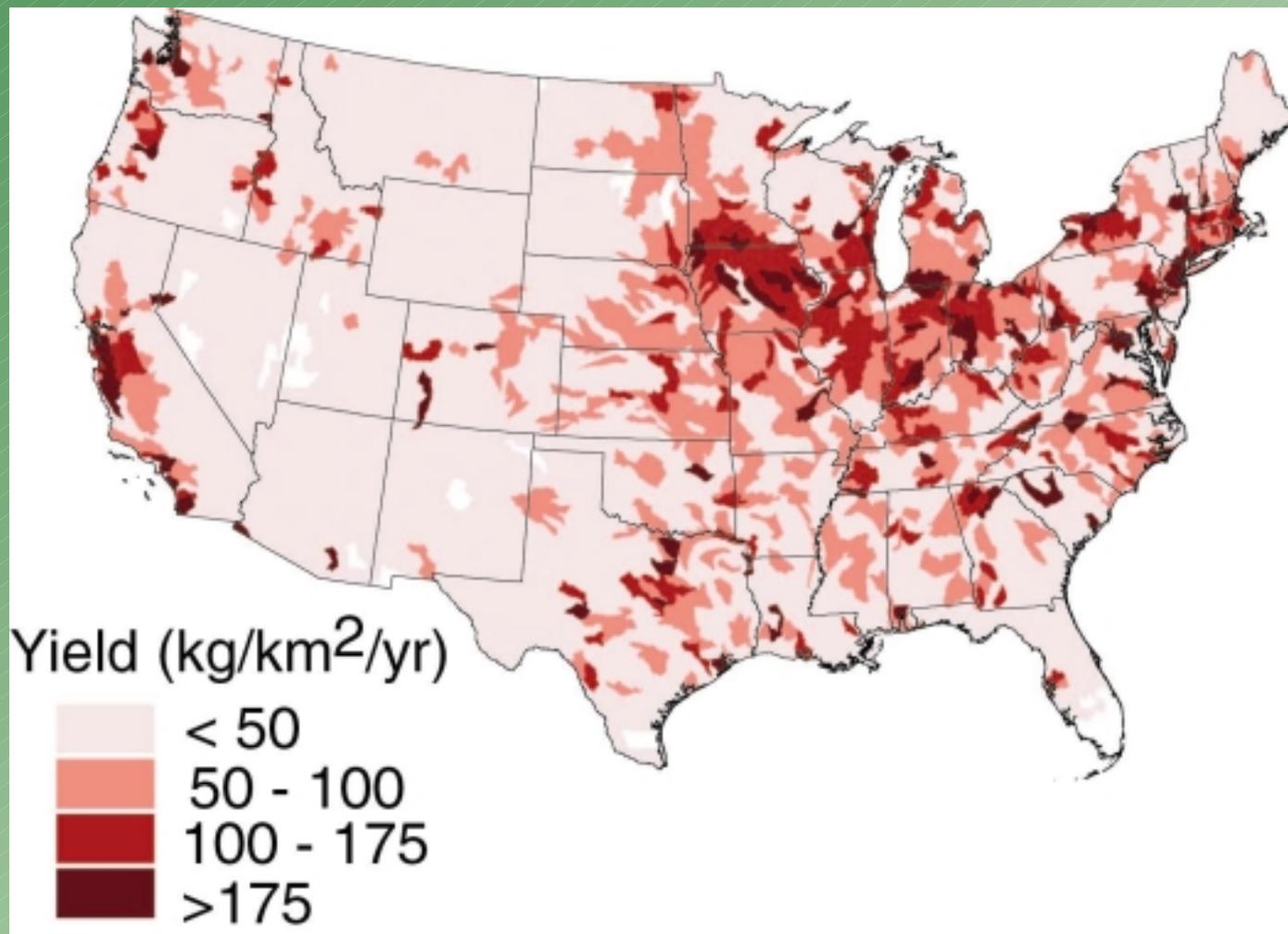
Blue < 500

Green 500 to 1,500

Red 1,500 to 10,000

Purple > 10,000

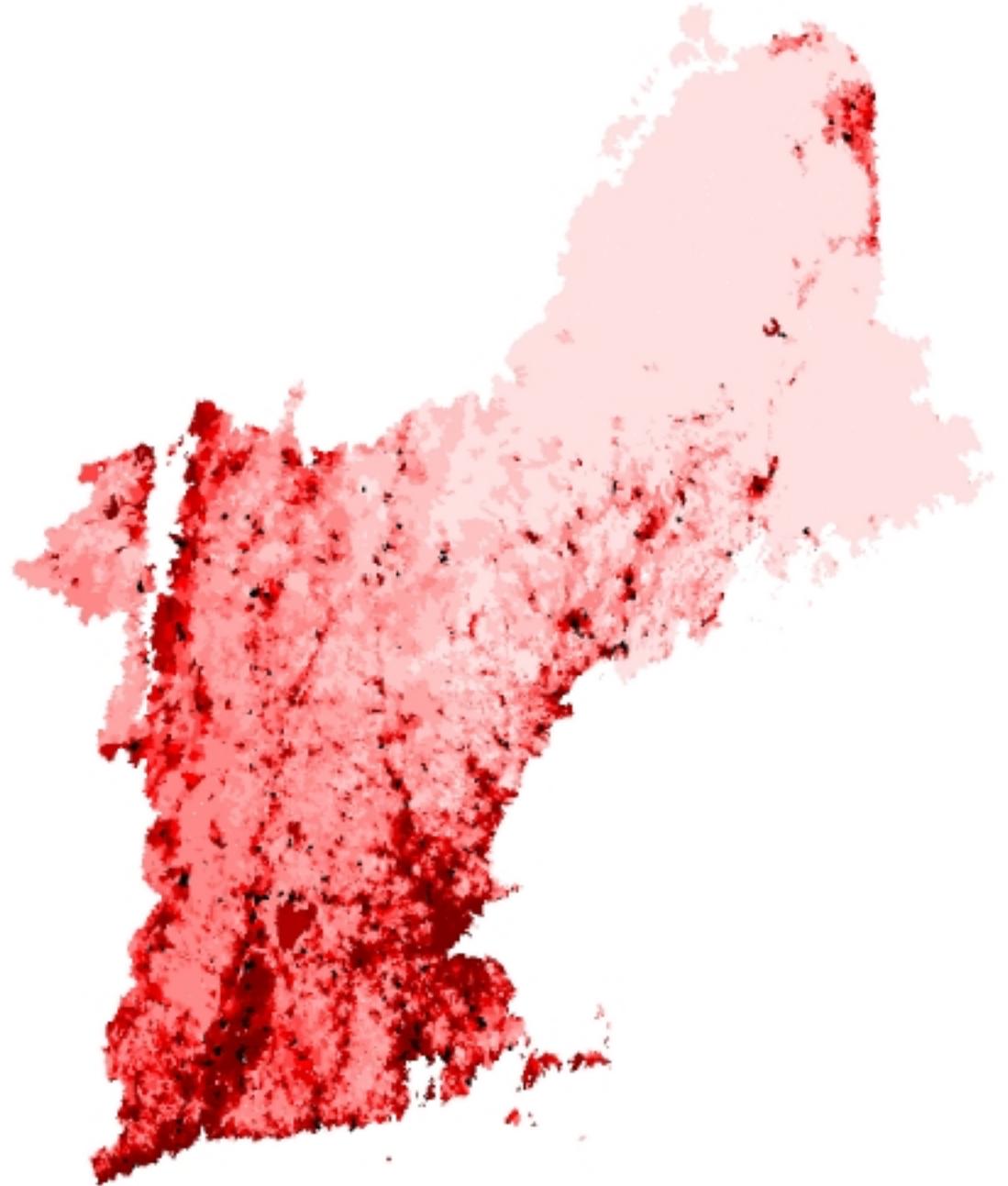
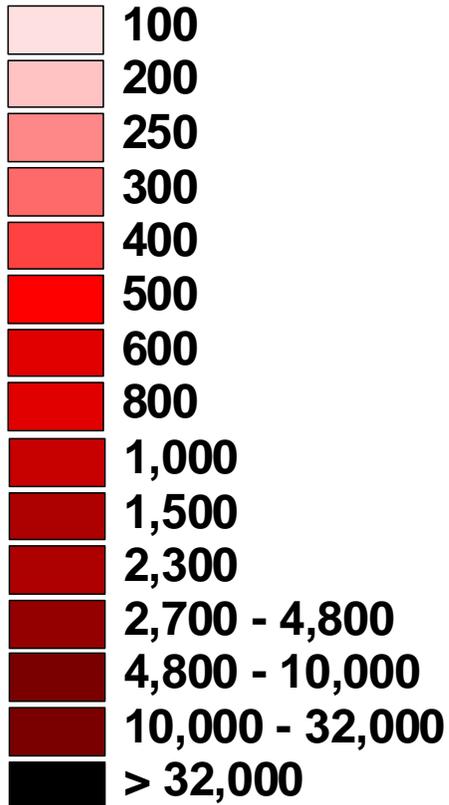
# TOTAL PHOSPHORUS Predictions in Hydrologic Units



# SPARROW

## Predicted Nitrogen Yield

Catchment Yield (kg / sq km)



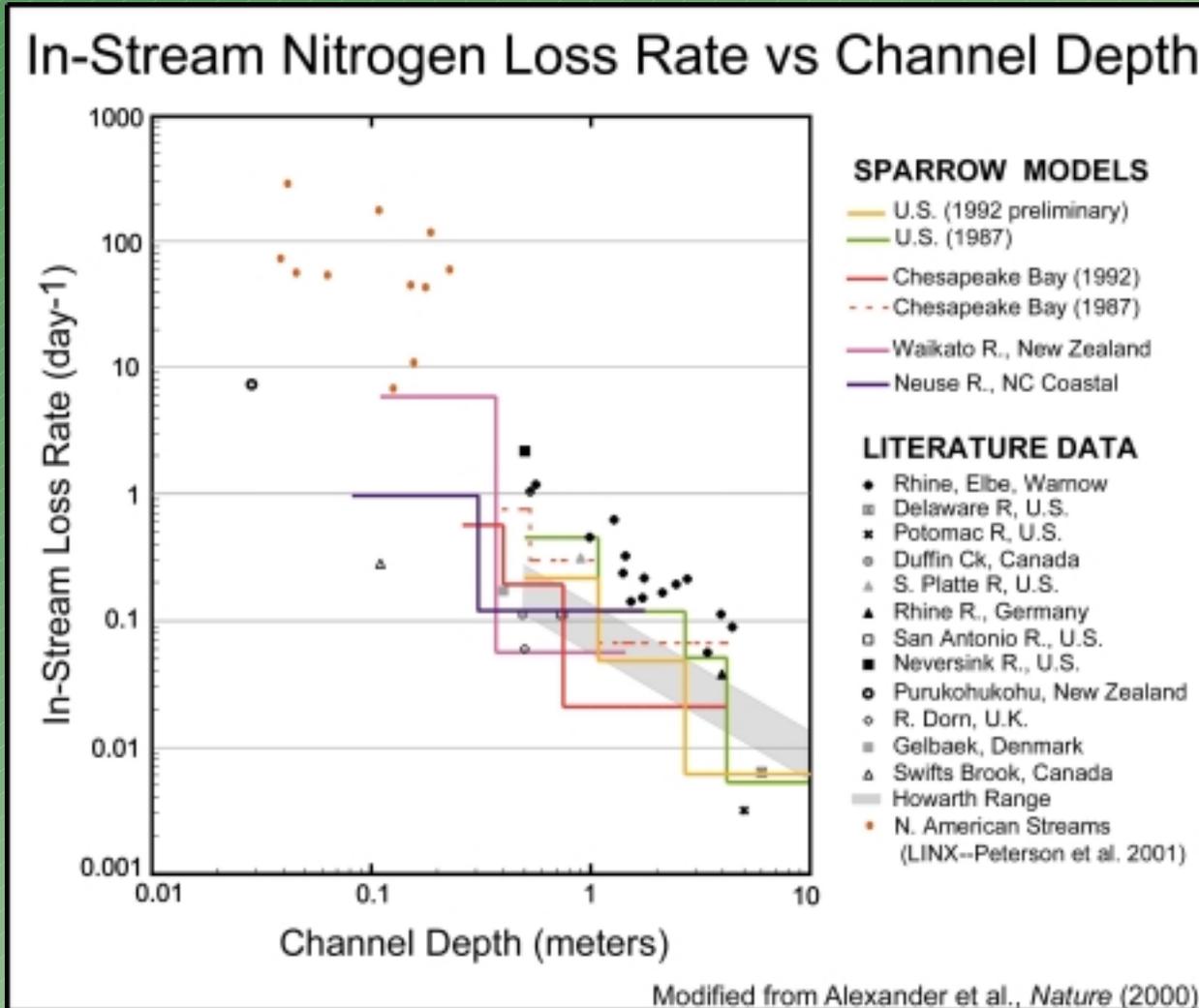
# SPARROW Prediction Statistics

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# National and Regional SPARROW Models

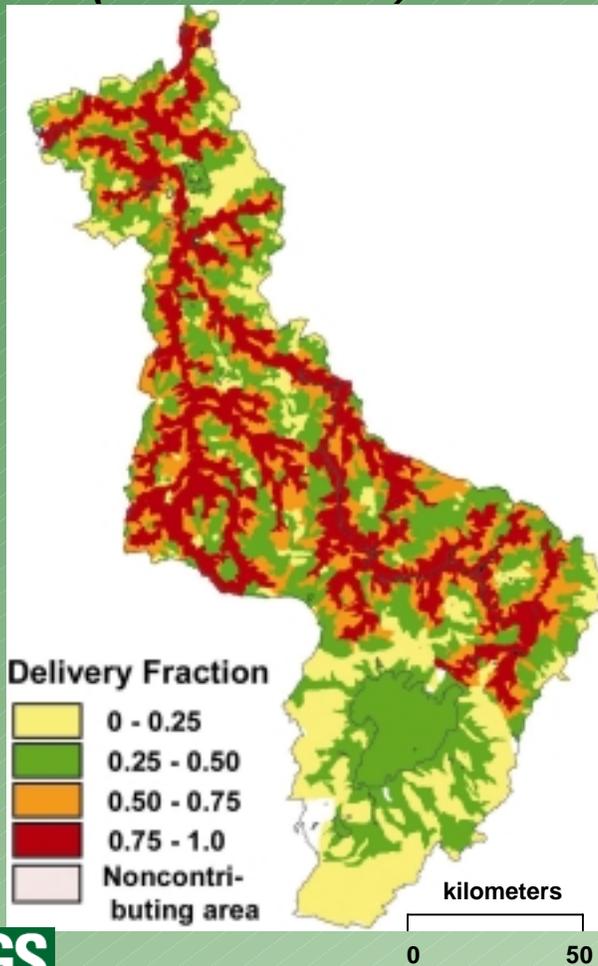


In-stream routing of contaminants performed as a function of 1<sup>st</sup>-order decay ( $e^{-kt}$ ) and water time of travel or channel length estimated for a range of stream sizes

# Fraction of In-Stream Nitrogen Delivered to Watershed Outlet

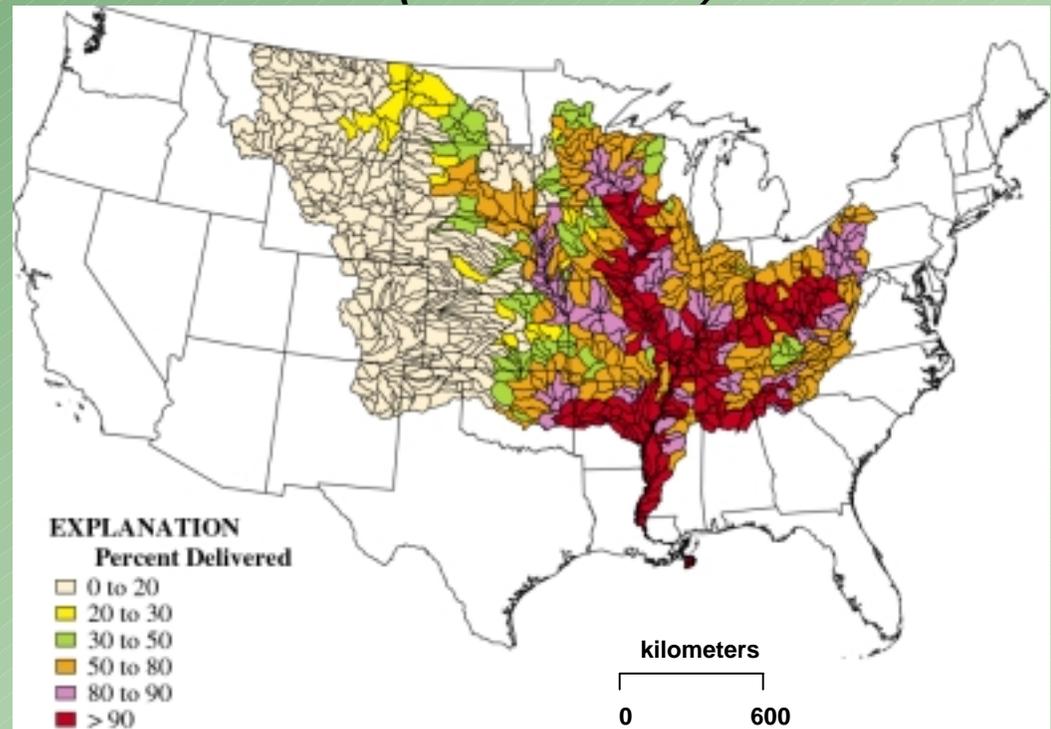
## Waikato R. Basin, N.Z.

( $1.4 \times 10^4 \text{ km}^2$ )



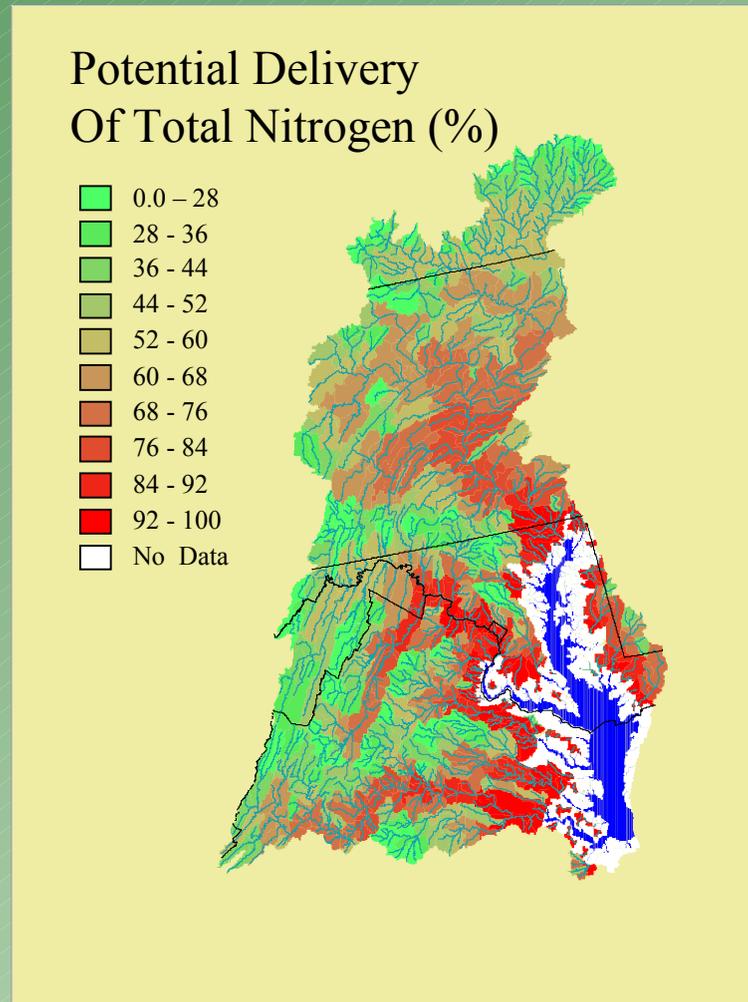
## Mississippi R. Basin

( $2.9 \times 10^6 \text{ km}^2$ )



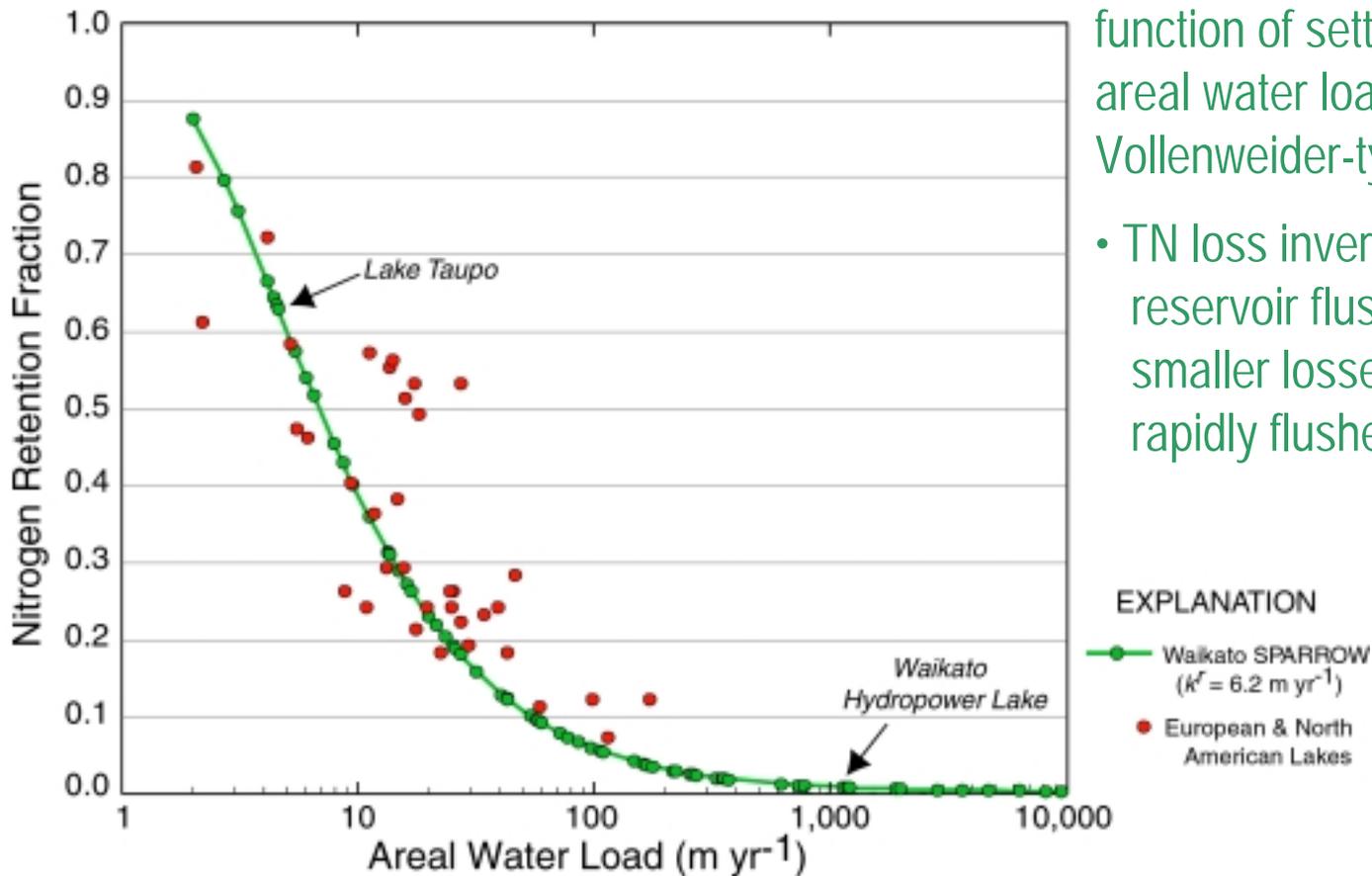
from Alexander et al. (2000; *in press*)

# Chesapeake Bay Watershed



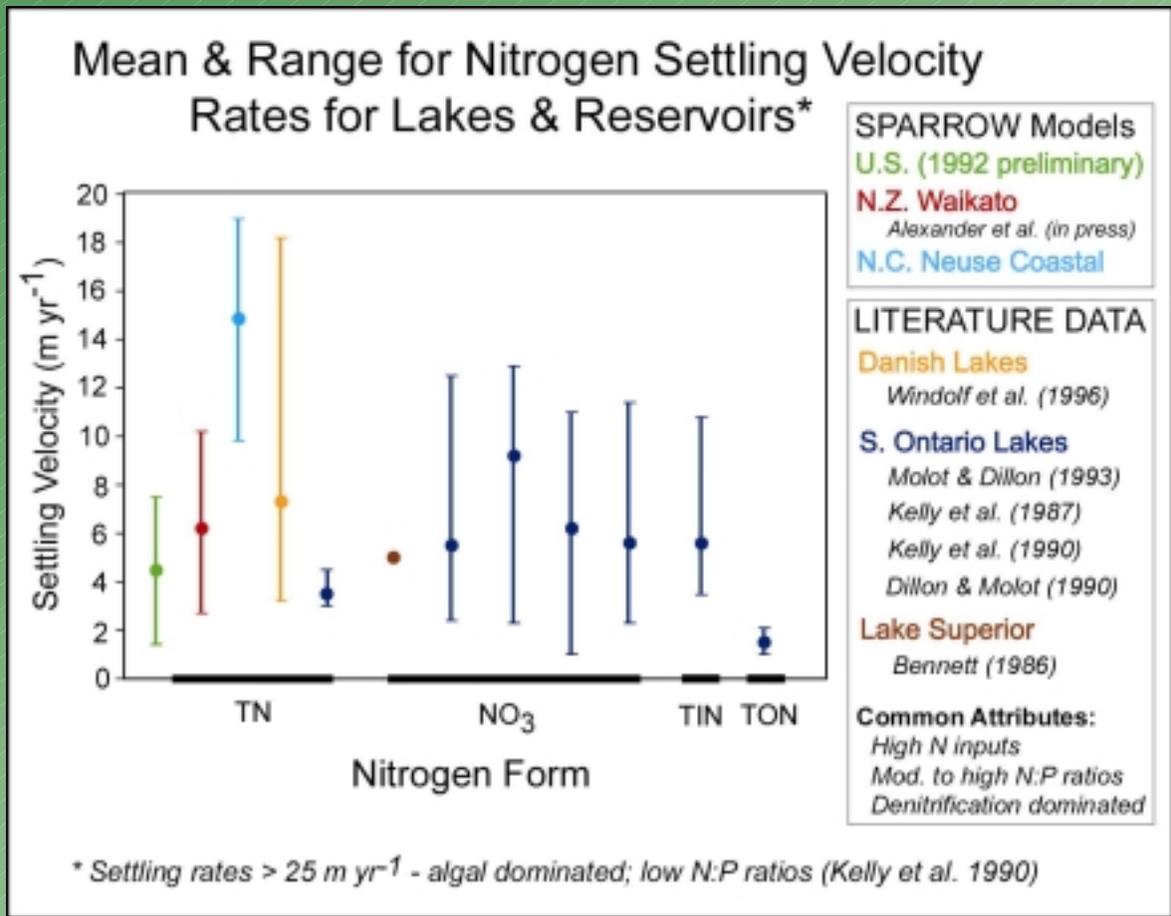
# Reservoir Routing of Total N

## Reservoirs of the Waikato River Basin, New Zealand



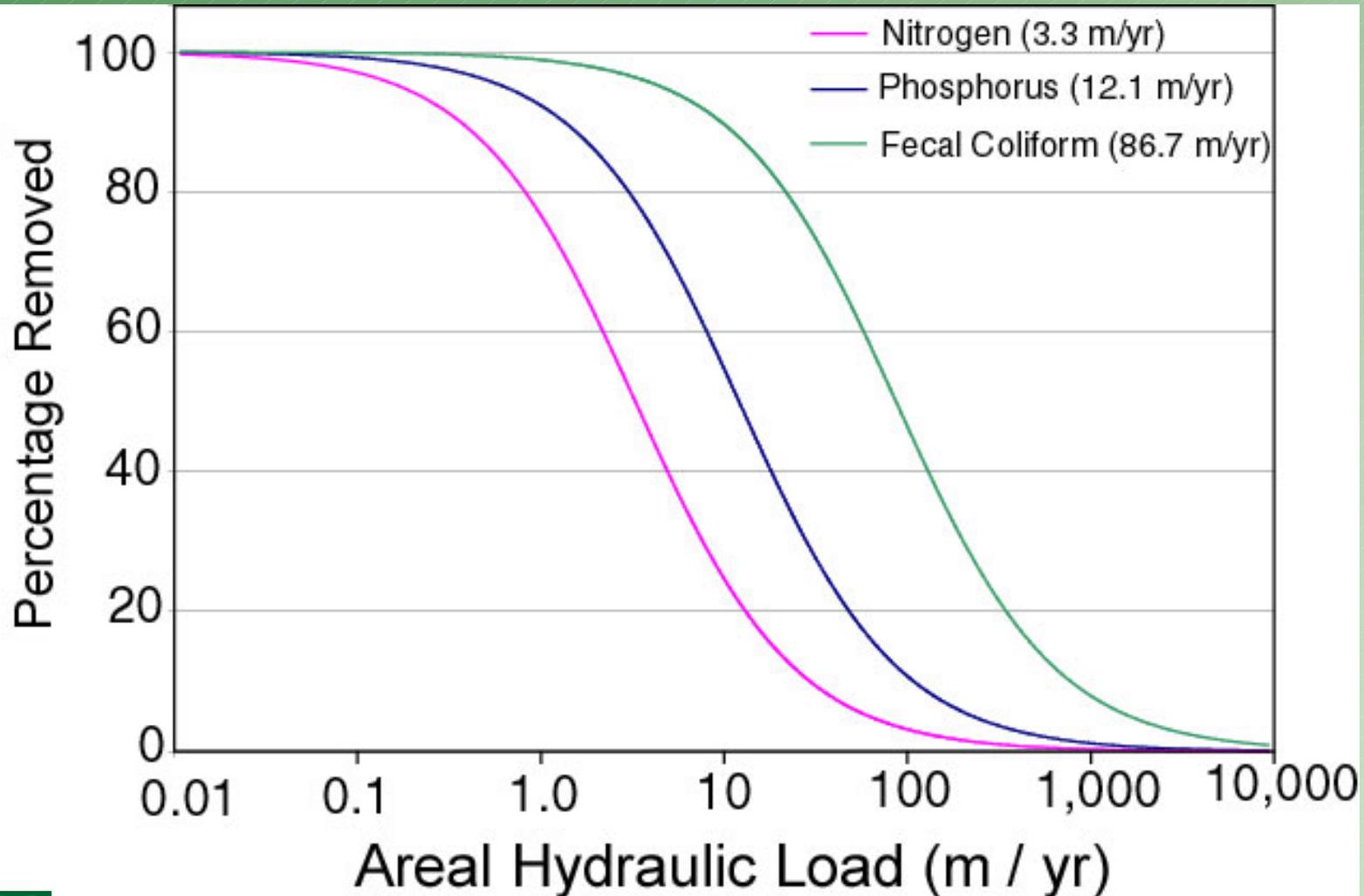
- Empirically estimated transport function of settling velocity and areal water load (based on Vollenweider-type models)
- TN loss inversely related to reservoir flushing rate—i.e., smaller losses occur in more rapidly flushed reservoirs

# SPARROW Estimates of Nitrogen Loss in Reservoirs

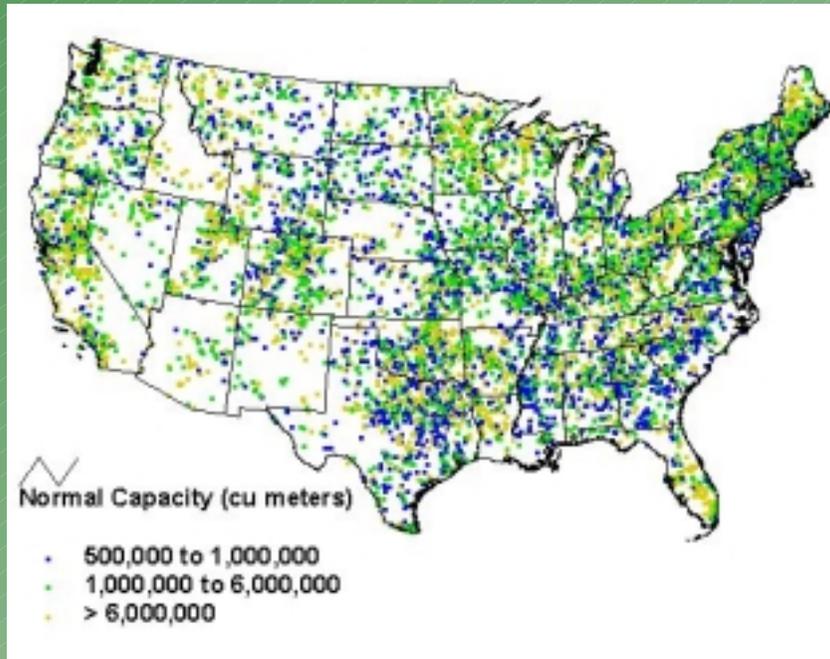


- SPARROW settling rates compare favorably with literature
- Magnitude of SPARROW rates suggest denitrification (rather than algal uptake and particulate burial) may be a dominant long-term loss process in reservoirs

# SPARROW Predictions of Nutrient and Fecal Bacteria Loss in Lakes and Reservoirs

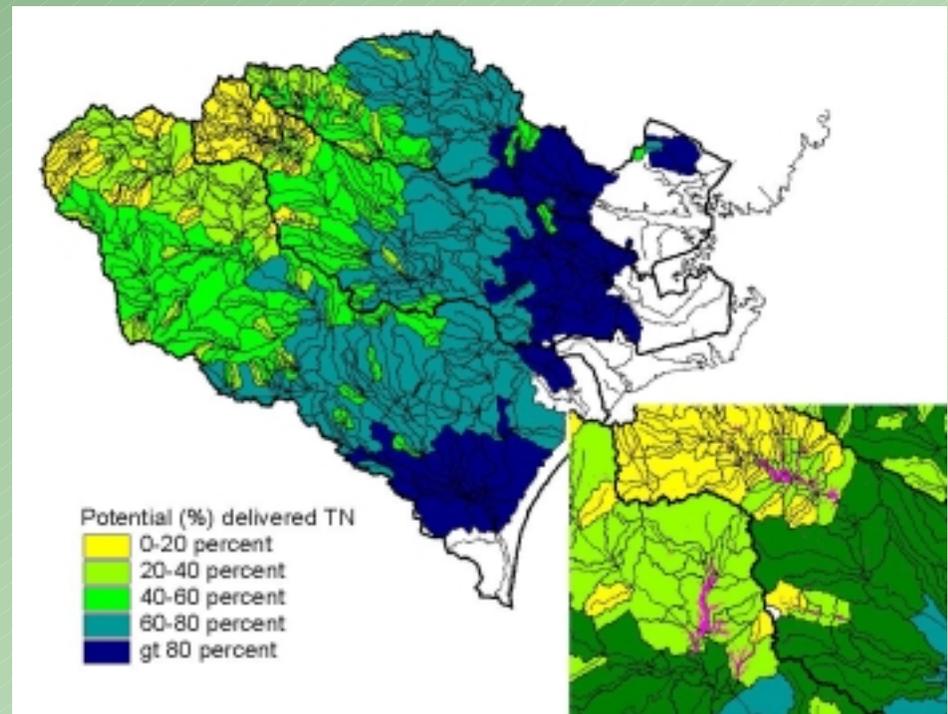


## Reservoirs, Lakes, Ponds National Inventory of Dams (NID)



Impoundments are prominent features of U.S. landscape (> 70,000)—their location and size may be important to understanding contaminant fate in watersheds

## North Carolina Coastal SPARROW



# SPARROW Prediction Statistics

## (Mean & Percentiles)

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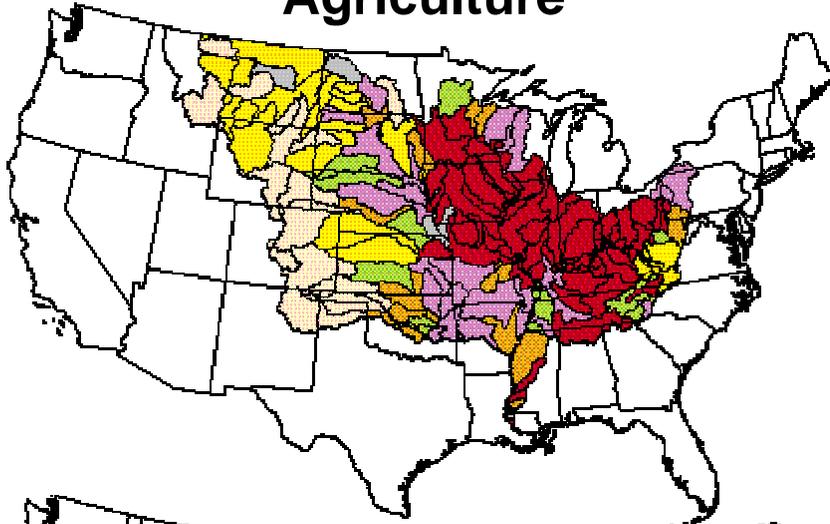
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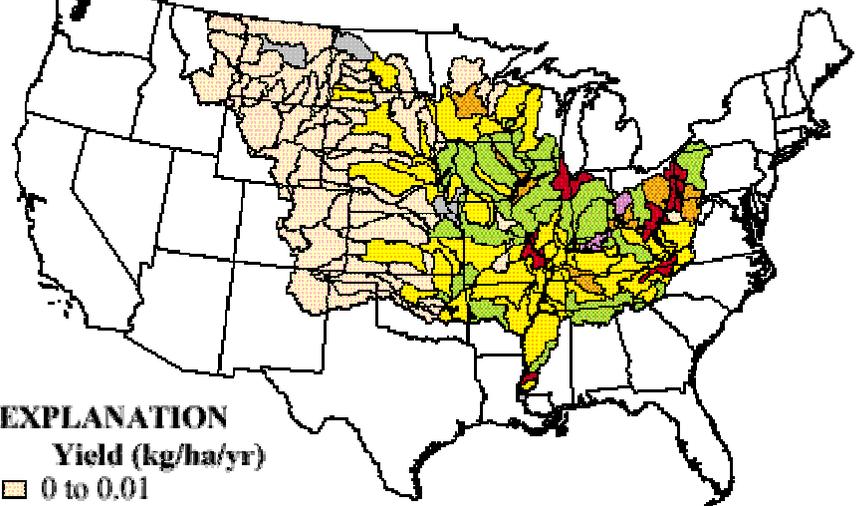
# Nitrogen Delivery to the Gulf of Mexico

# SPARROW Estimates of Delivered TN Yield

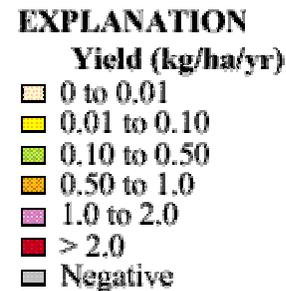
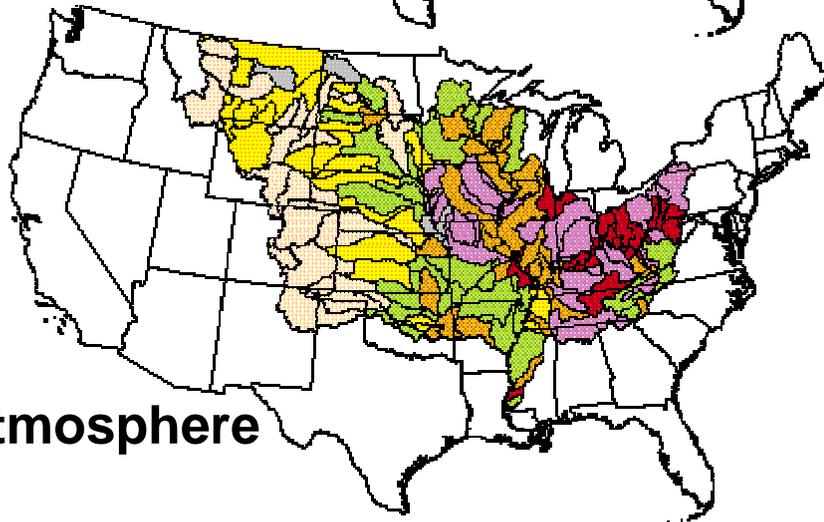
## Agriculture



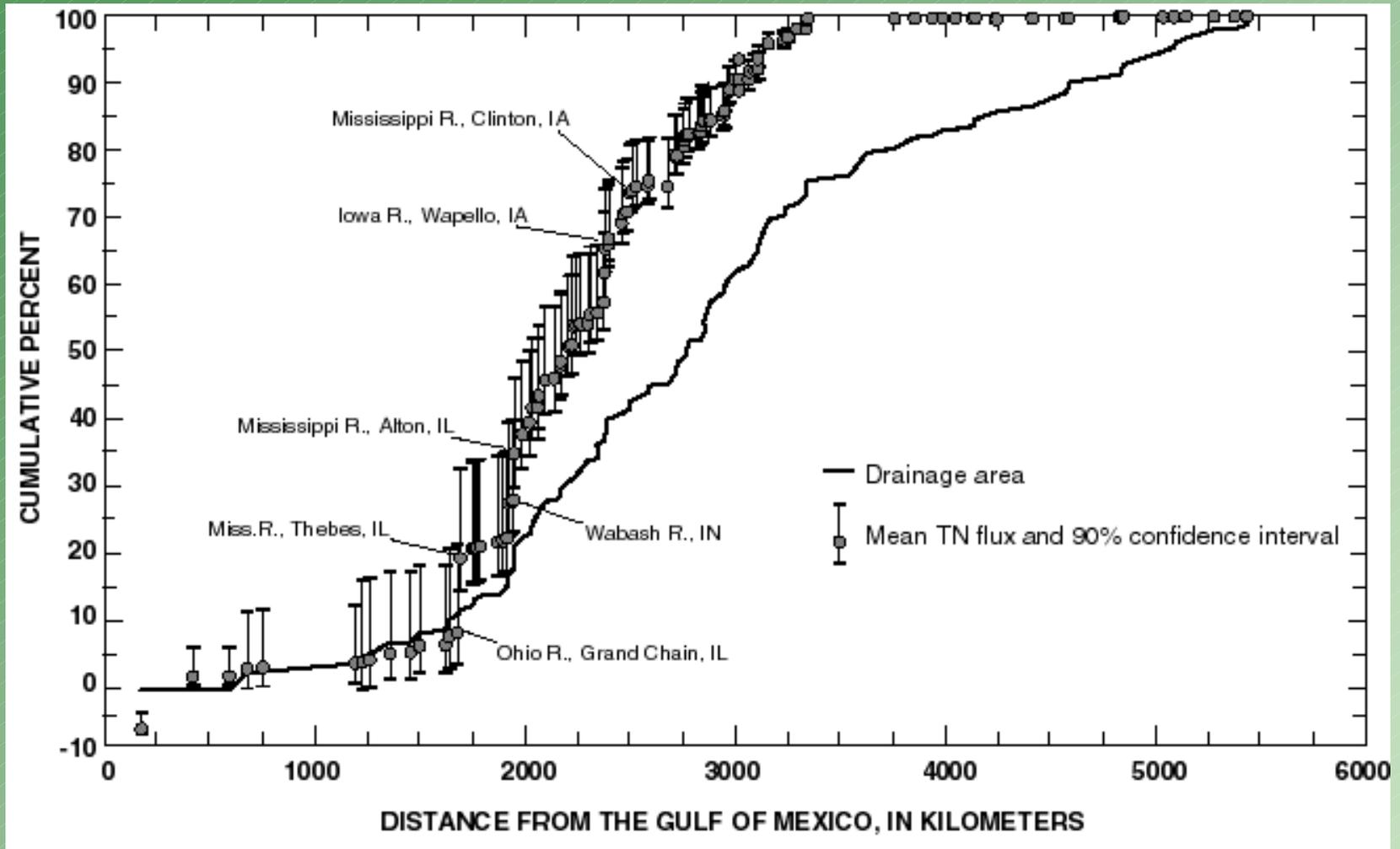
## Point Sources



## Atmosphere



# Cumulative Percentage of TN Flux Delivered to Gulf from Intervening Watersheds of Monitoring Stations

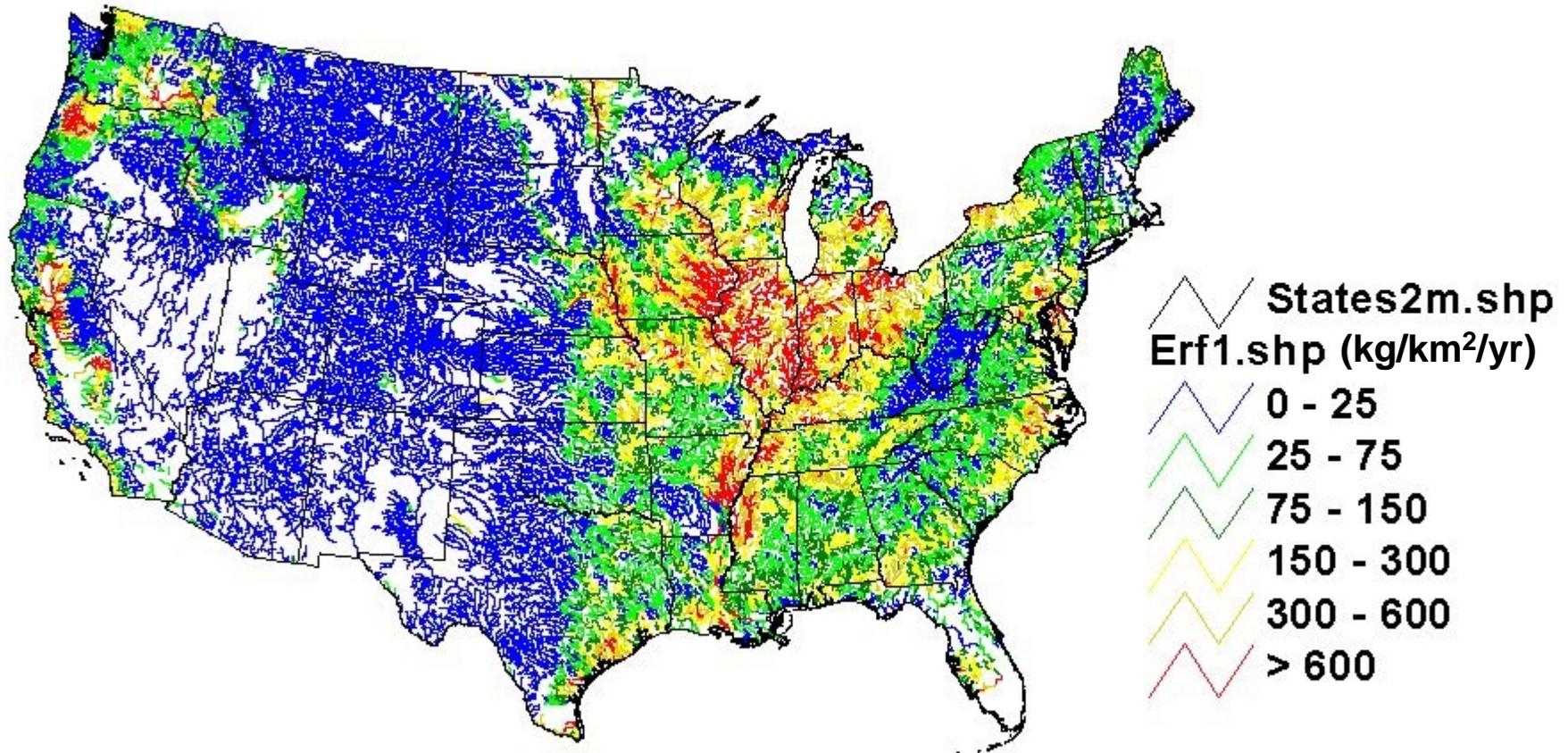


(based on model data from Alexander et al. 2000)

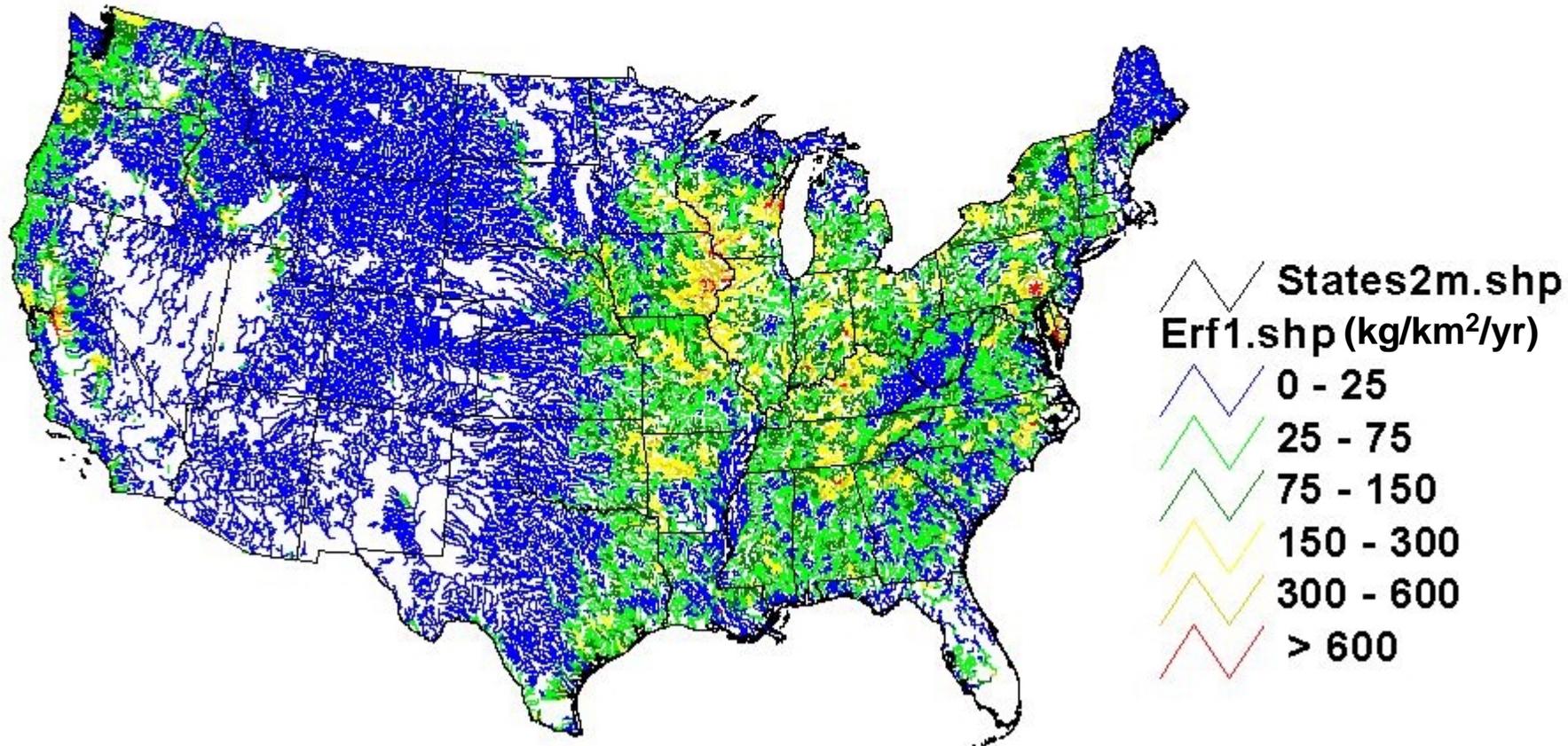
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# Nitrogen Delivery to the U.S. Coastal areas

# Fertilizer Nitrogen Delivered Yield

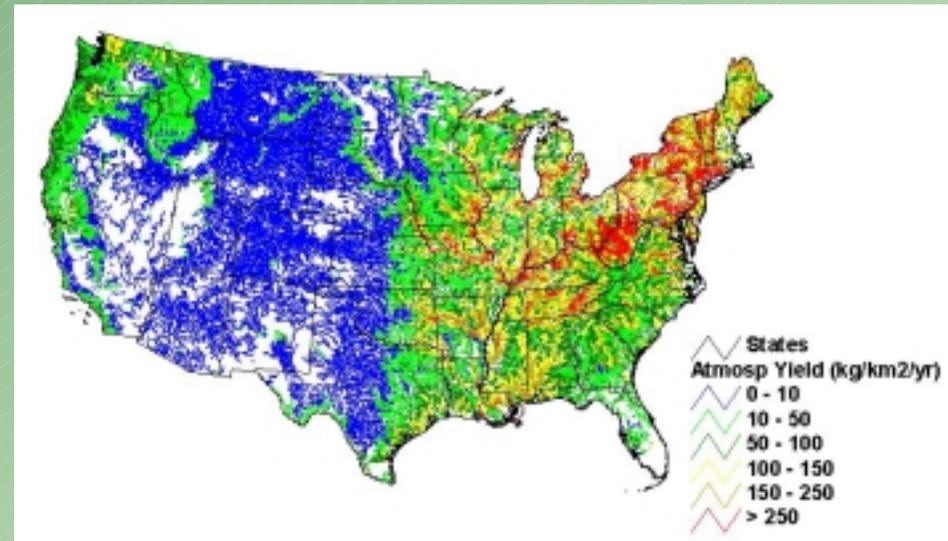
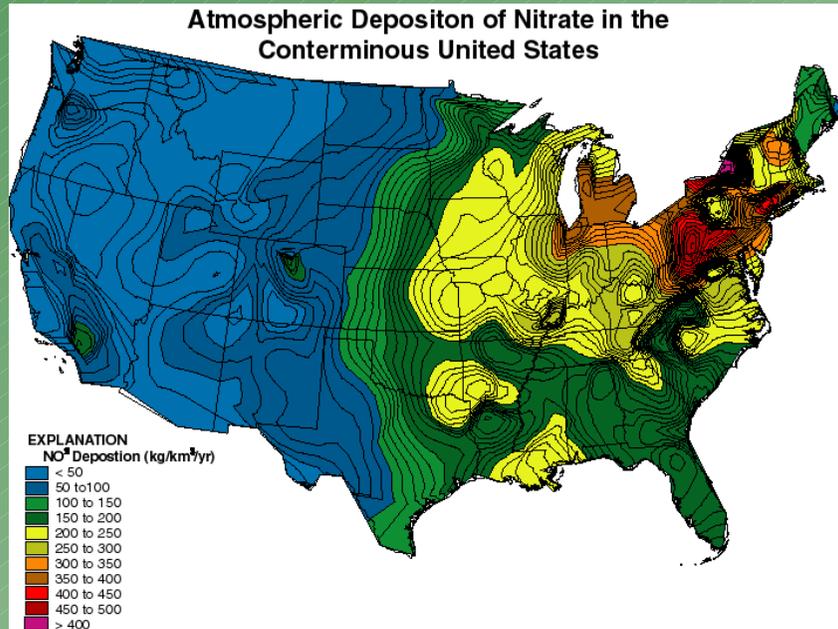


# Livestock Waste Nitrogen Delivered Yield



# SPARROW Predictions

## Atmospheric Nitrogen Delivered to Estuaries in comparison to Deposition Inputs



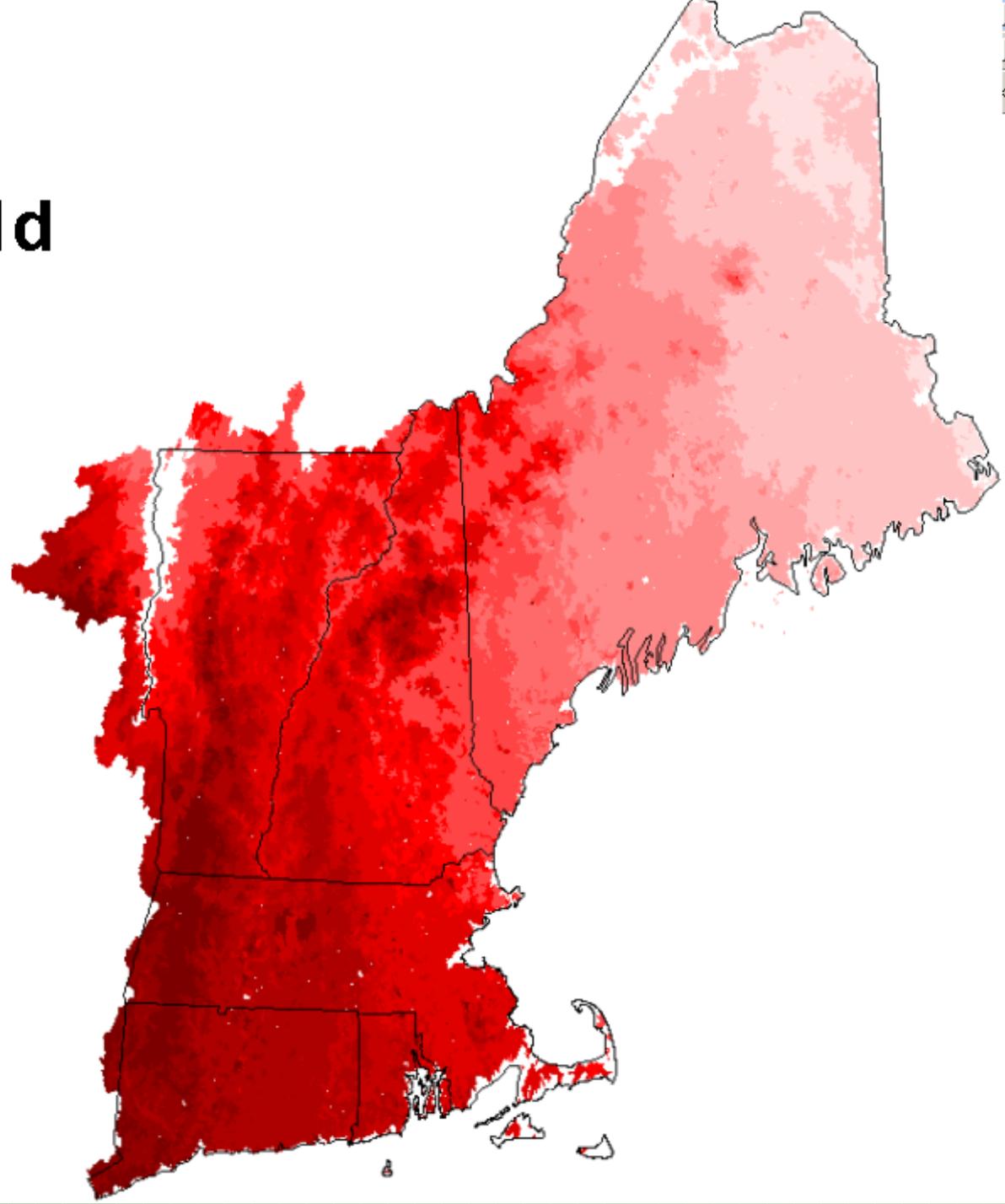
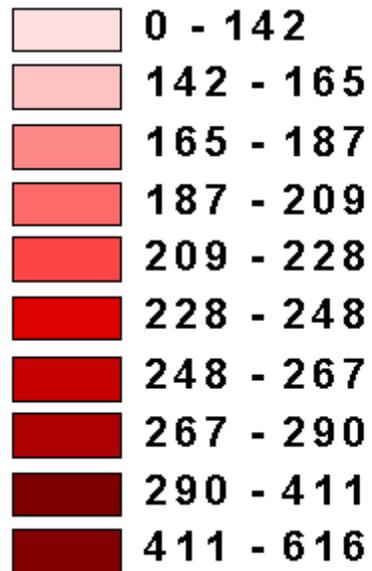
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# Nitrogen Delivery to the New England Coastal areas

# SPARROW

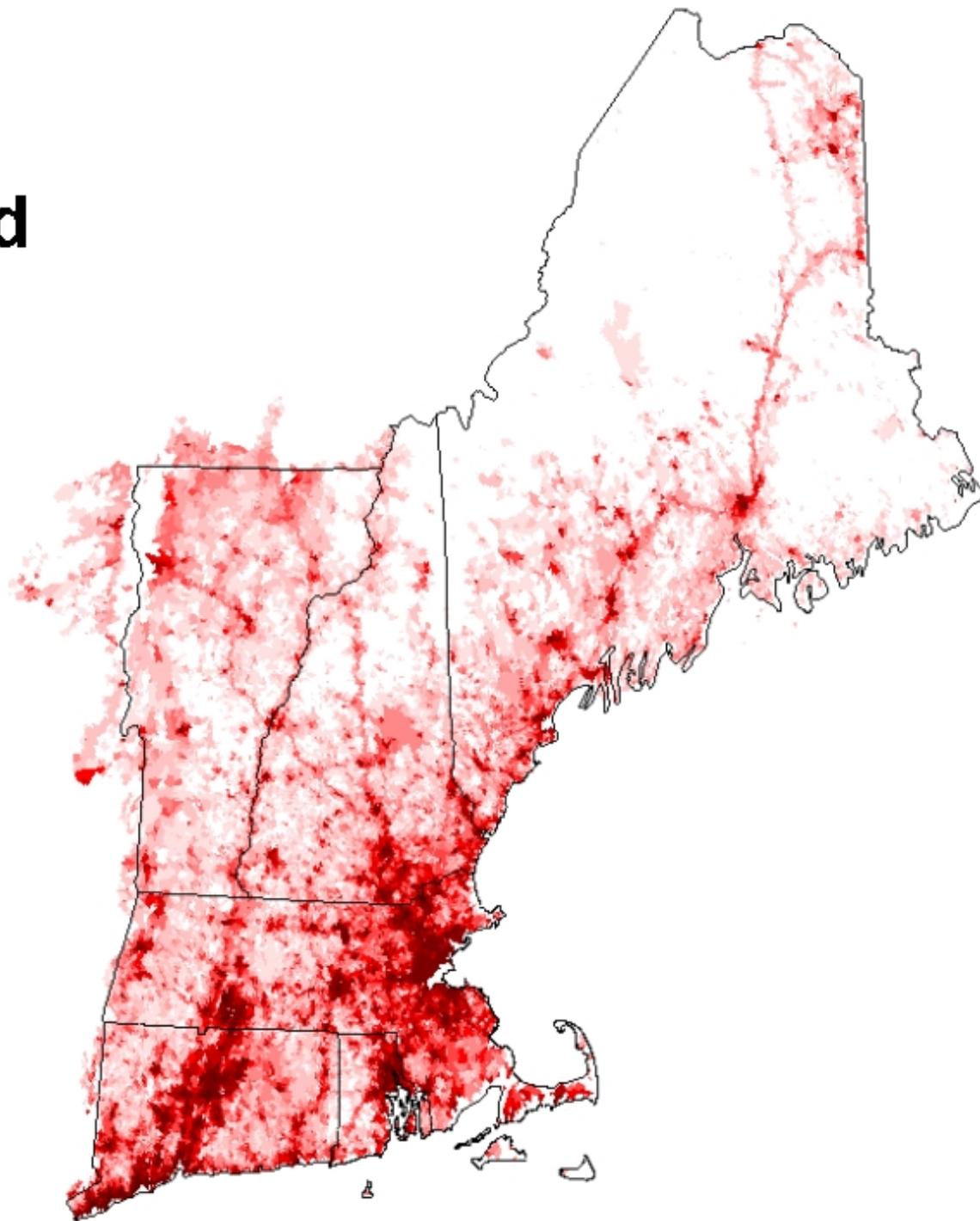
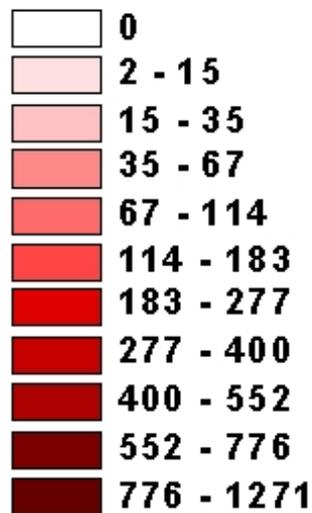
## Predicted Nitrogen Yield Atmospheric Deposition

Catchment Yield  
(kg / sq km)



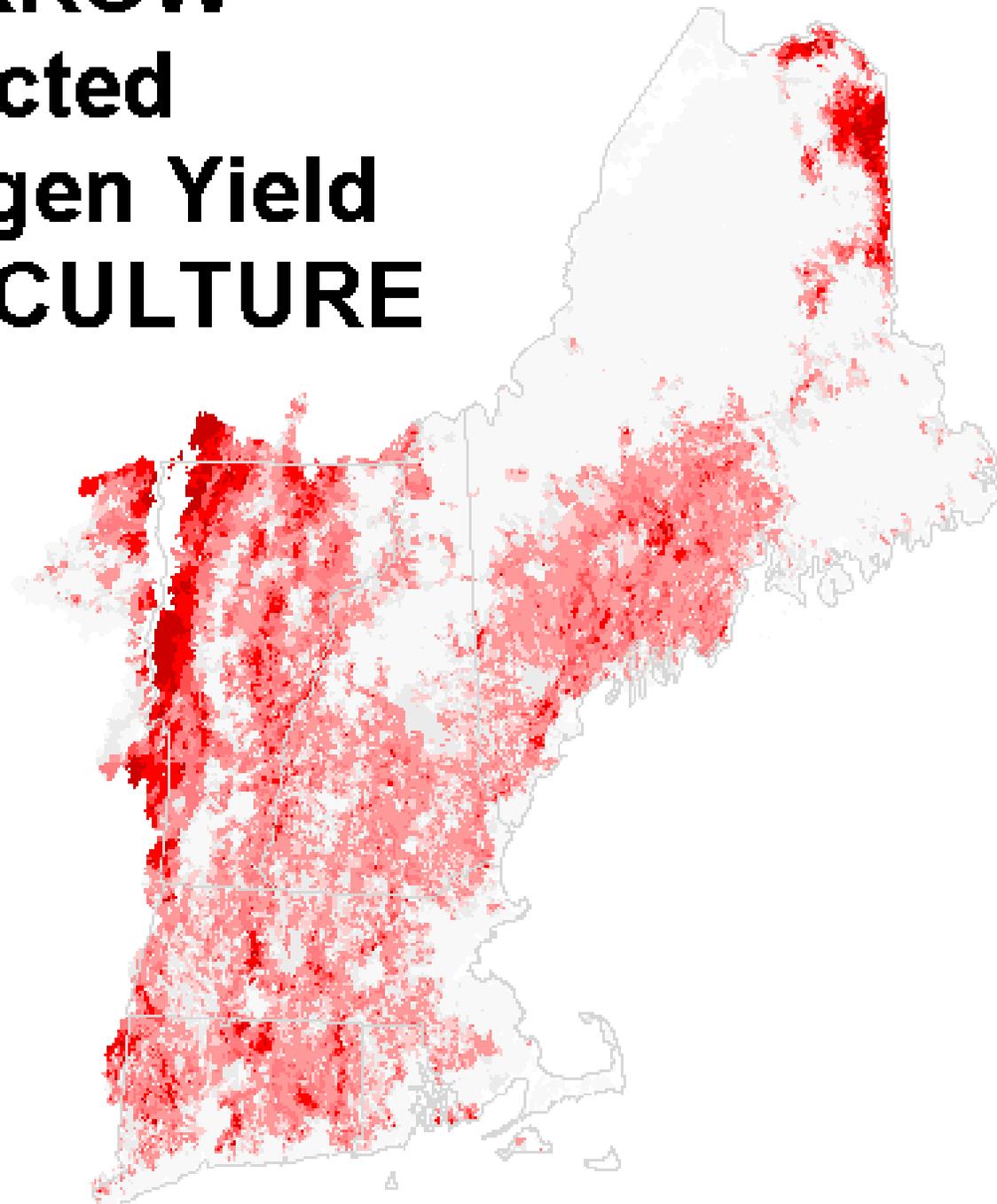
# SPARROW Predicted Nitrogen Yield URBAN Sources

Catchment Yield  
(kg / sq km)

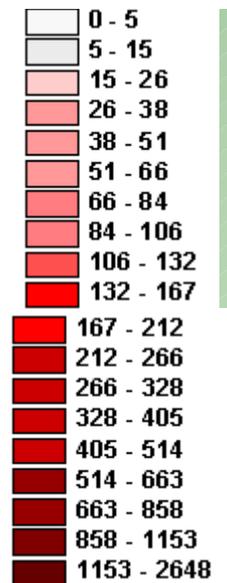


# SPARROW

## Predicted Nitrogen Yield AGRICULTURE



(kg / sq km)

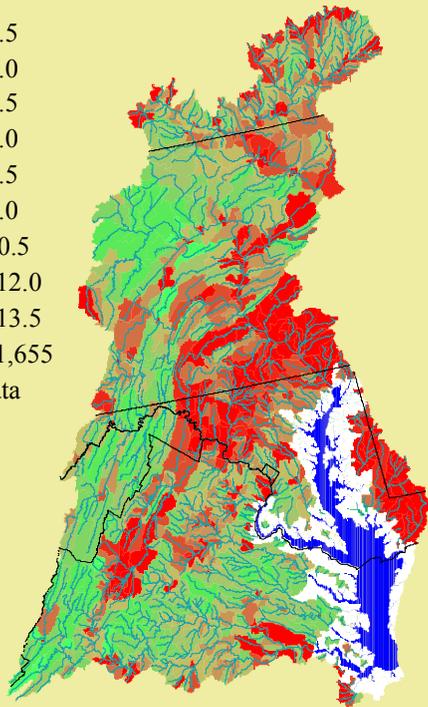


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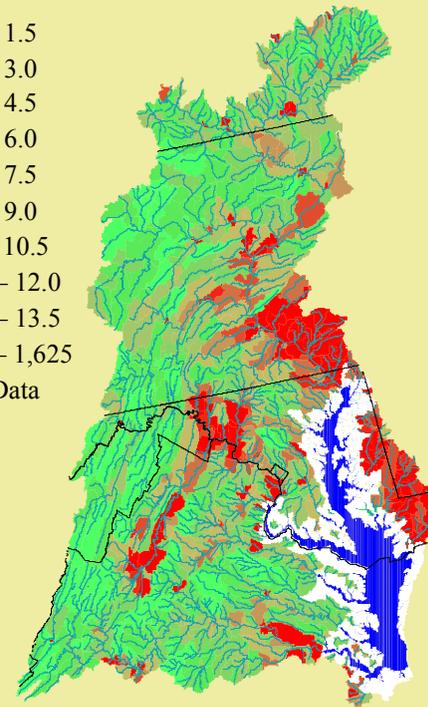
# Nitrogen Delivery to the Chesapeake Bay

# Chesapeake Bay Watershed Nitrogen Yield (kg/ha-yr)

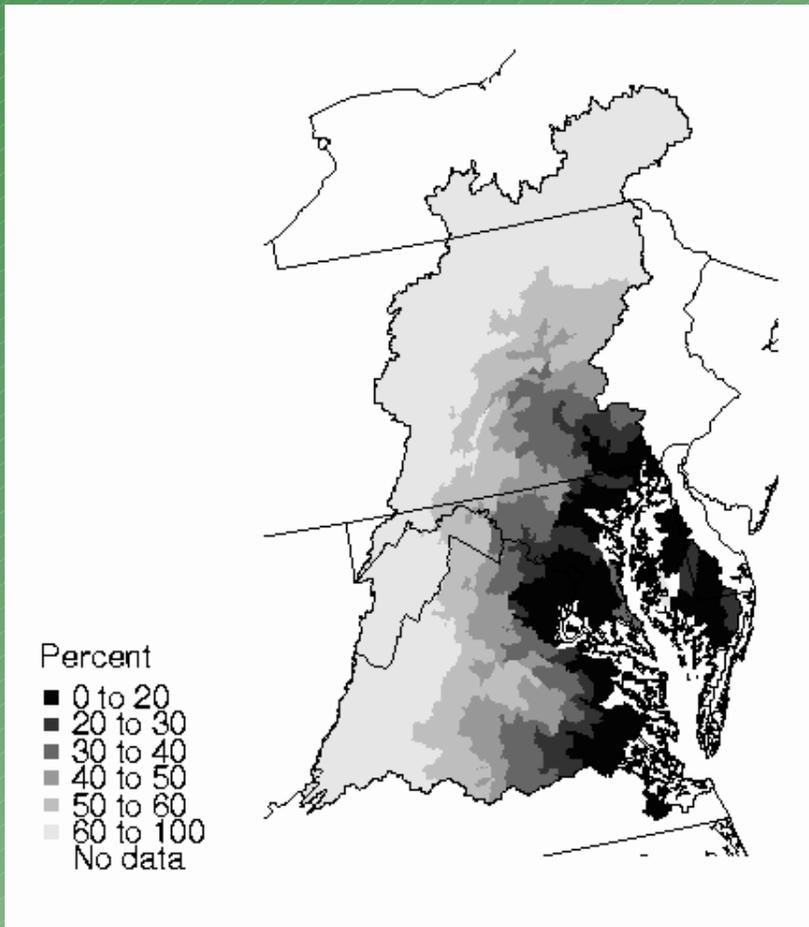
## Incremental Yield



## Delivered Yield



a



b

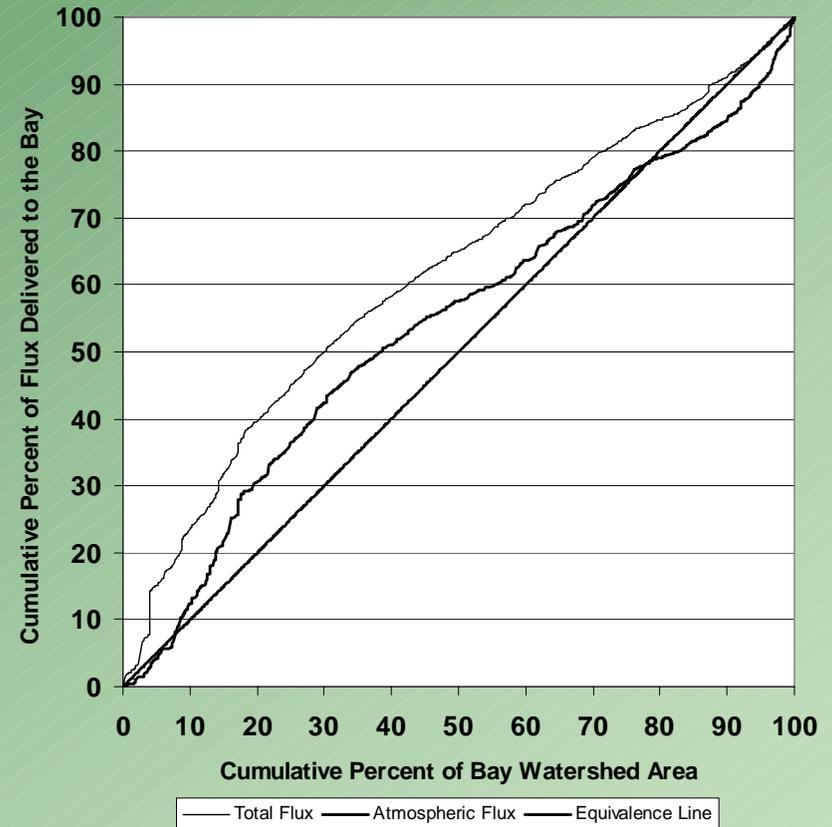
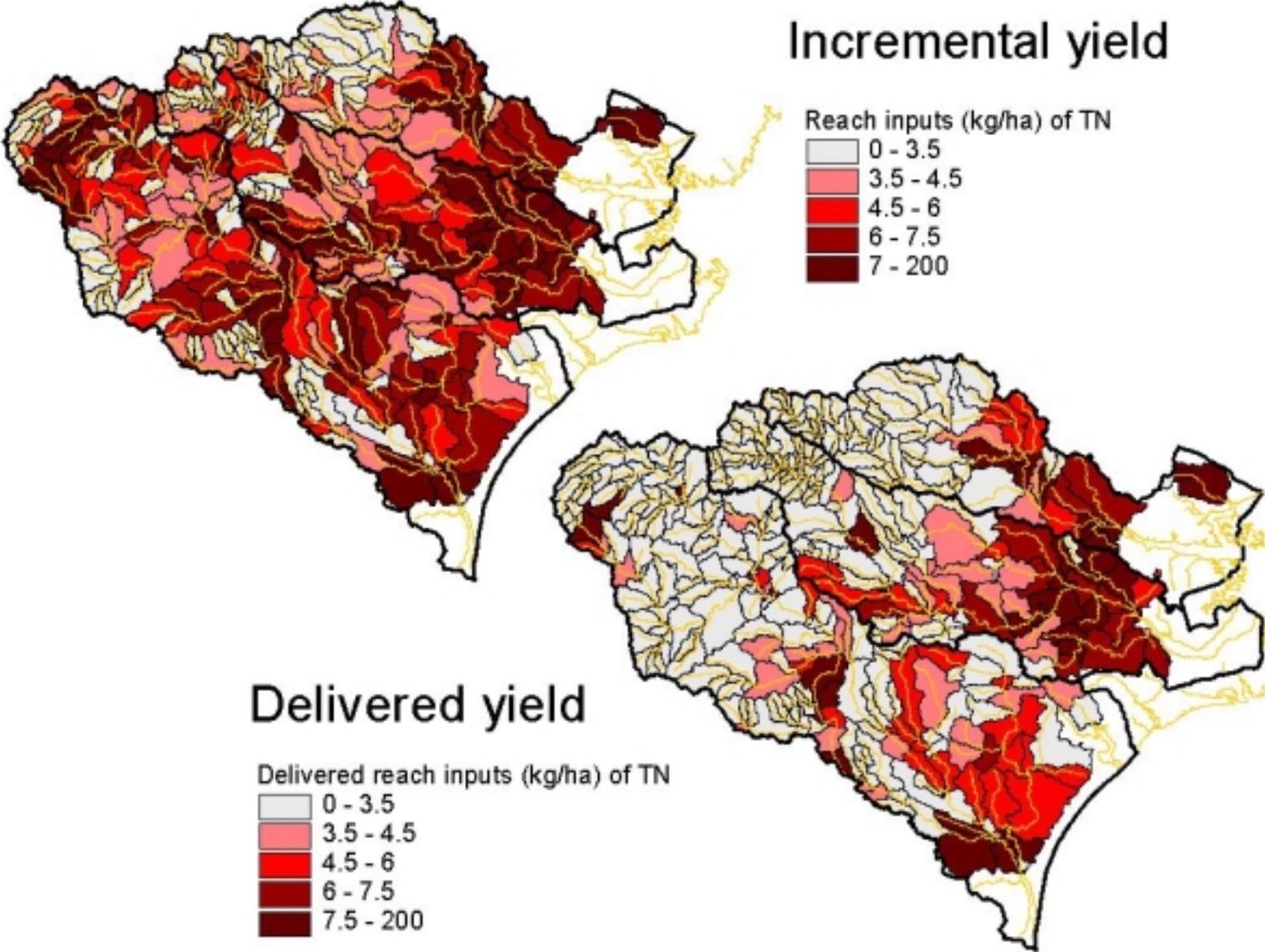
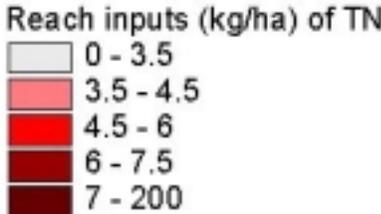


Figure 10. Cumulative percentage of the stream nitrogen delivered to the Chesapeake Bay from interior watersheds as a function of river channel distance from the Bay: (a) map of atmospheric nitrogen by watershed; (b) total and atmospheric flux in relation to watershed area.

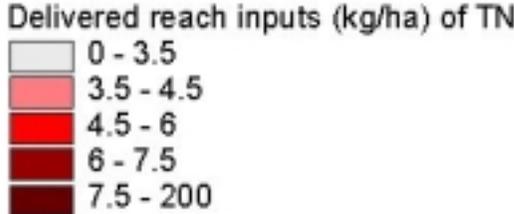
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# Nitrogen Delivery to Coastal North Carolina

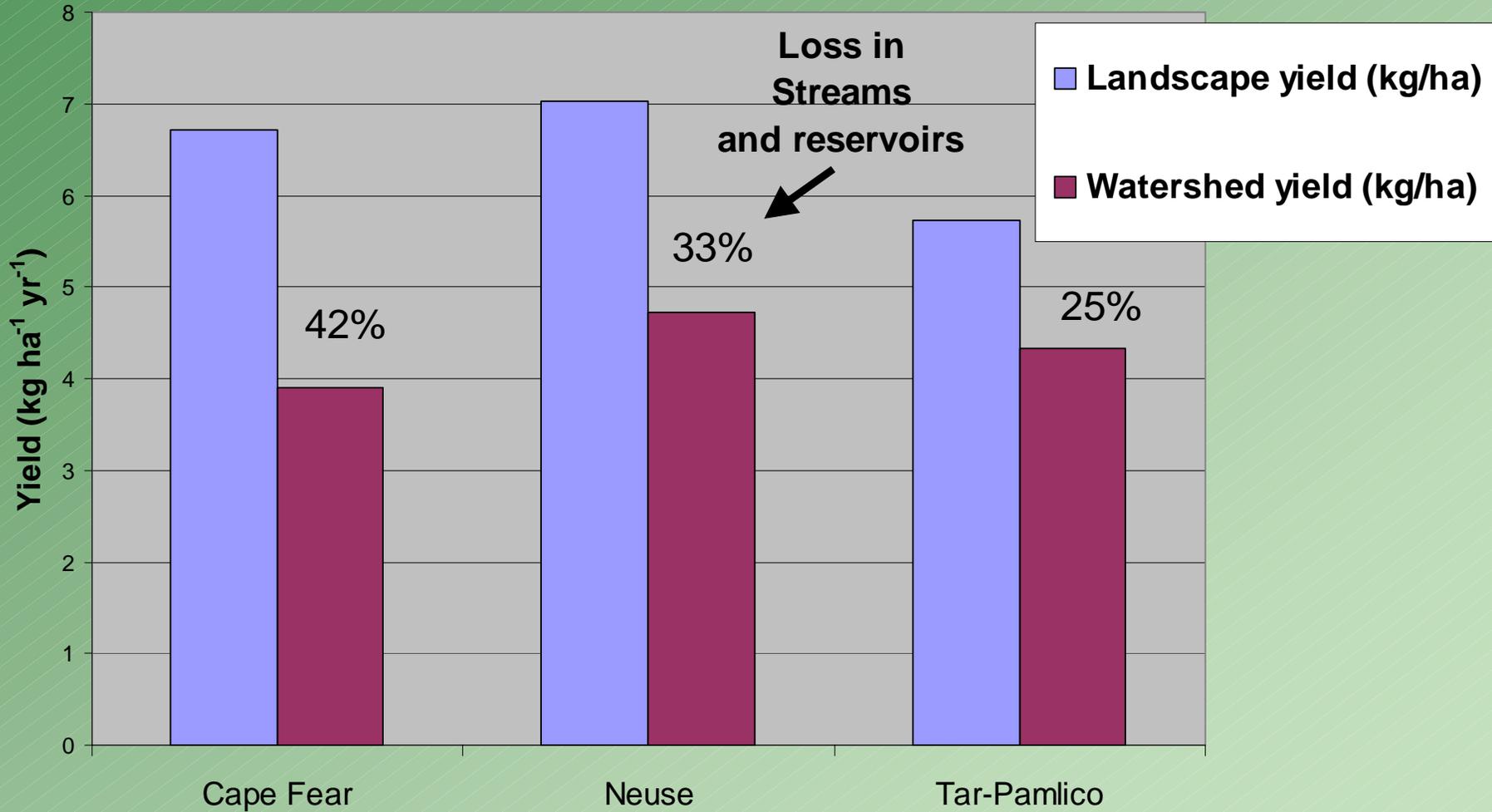
# Incremental yield



# Delivered yield



# NC SPARROW TN yield (kg/ha) at edge of stream and at watershed outlet



# SPARROW Prediction Statistics

## (Mean & Percentiles)

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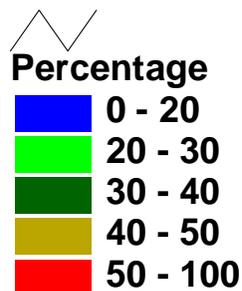
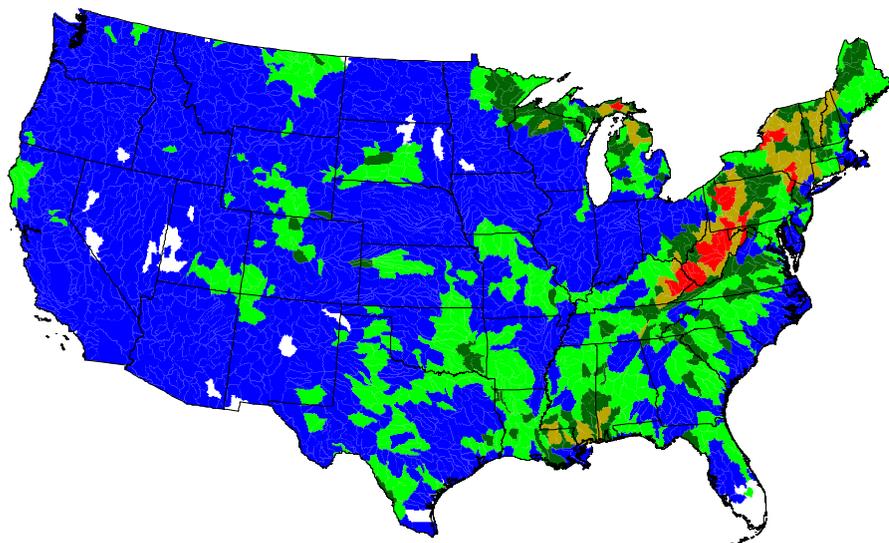
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# Contaminant sources and budgets contiguous U.S.

# Nutrient Sources in U.S. Watersheds\*

## Atmospheric Contributions to Total Nitrogen Export



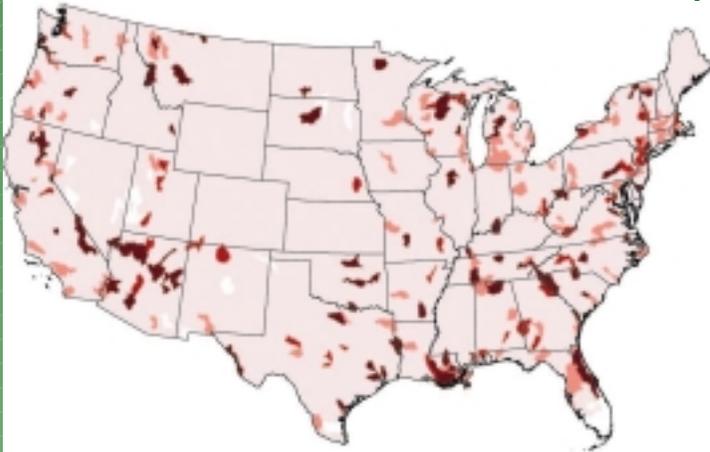
- Nutrient management conference
- Useful general summary of sources
- Results for TN and TP
- Tabulated by cataloging unit
- Gives budgets at outlets of units
- Differ from budgets based on inputs
- Accounts for variations in delivery among sources and watersheds

\* Smith and Alexander, 2000

# SPARROW TP Intensive-Source Model

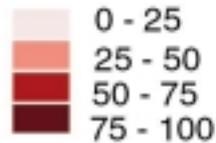
## URBAN POINT AND DIFFUSE

SEWERED POPULATION (4%)

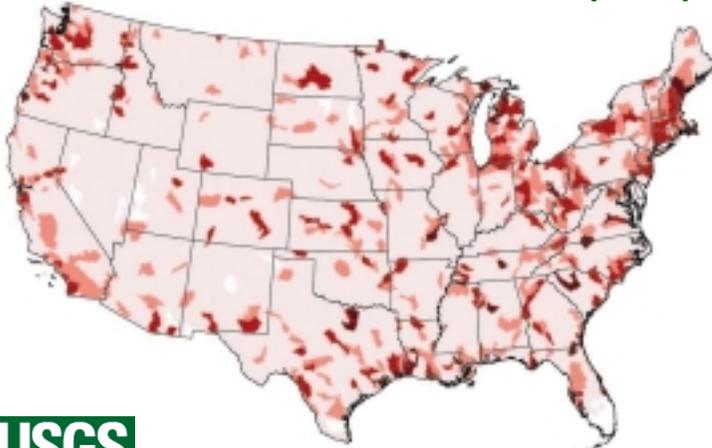


*Percent of  
Total Flux In  
All Watersheds*

PERCENT  
CONTRIBUTION



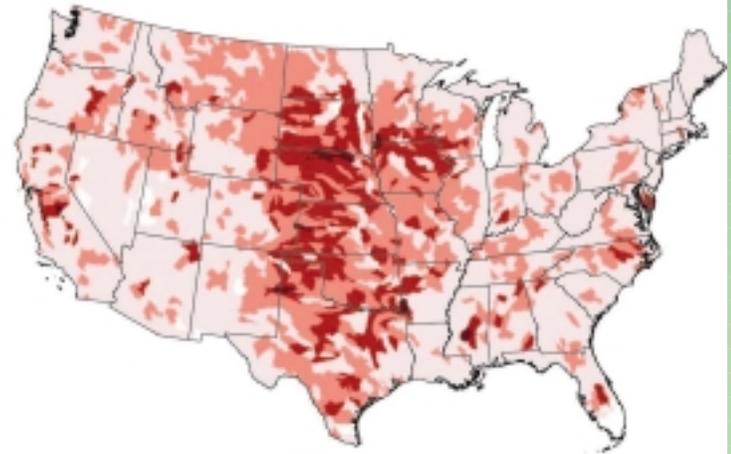
URBAN DIFFUSE (13%)



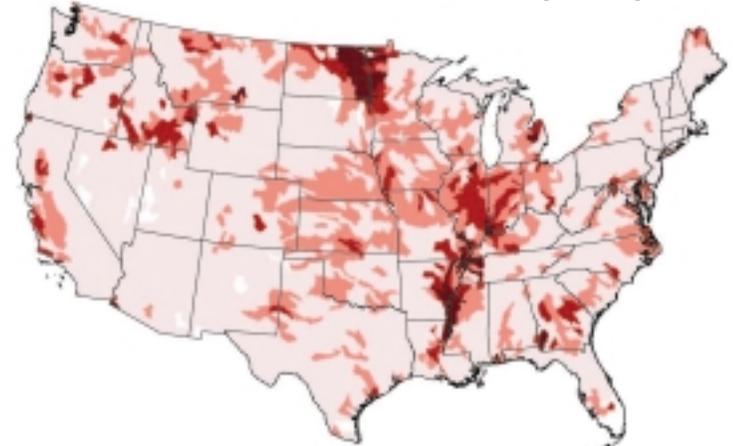
Forest = 19%  
Shrub = 5%

## AGRICULTURAL

LIVESTOCK WASTE (34%)

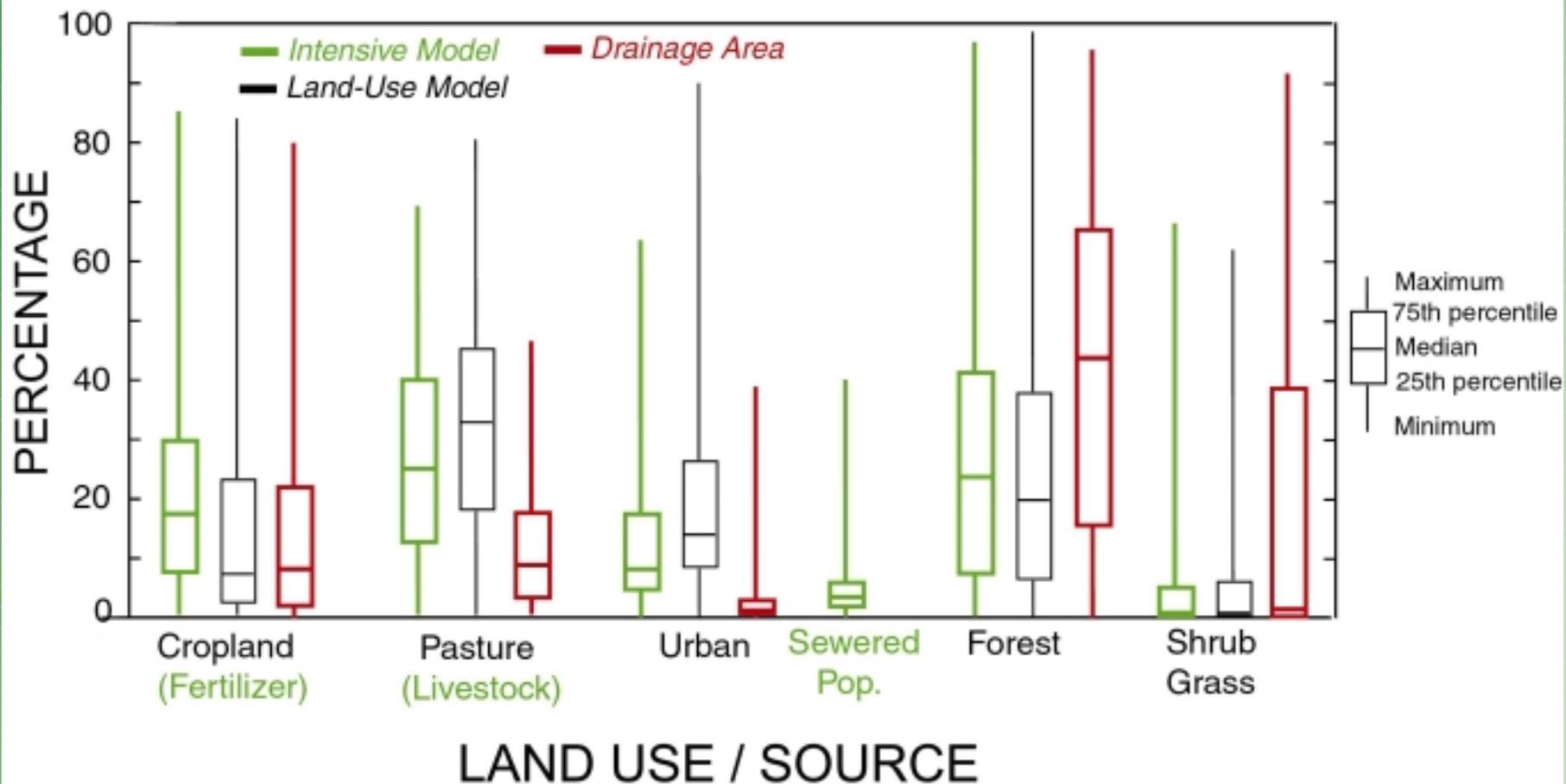


FERTILIZER (26%)

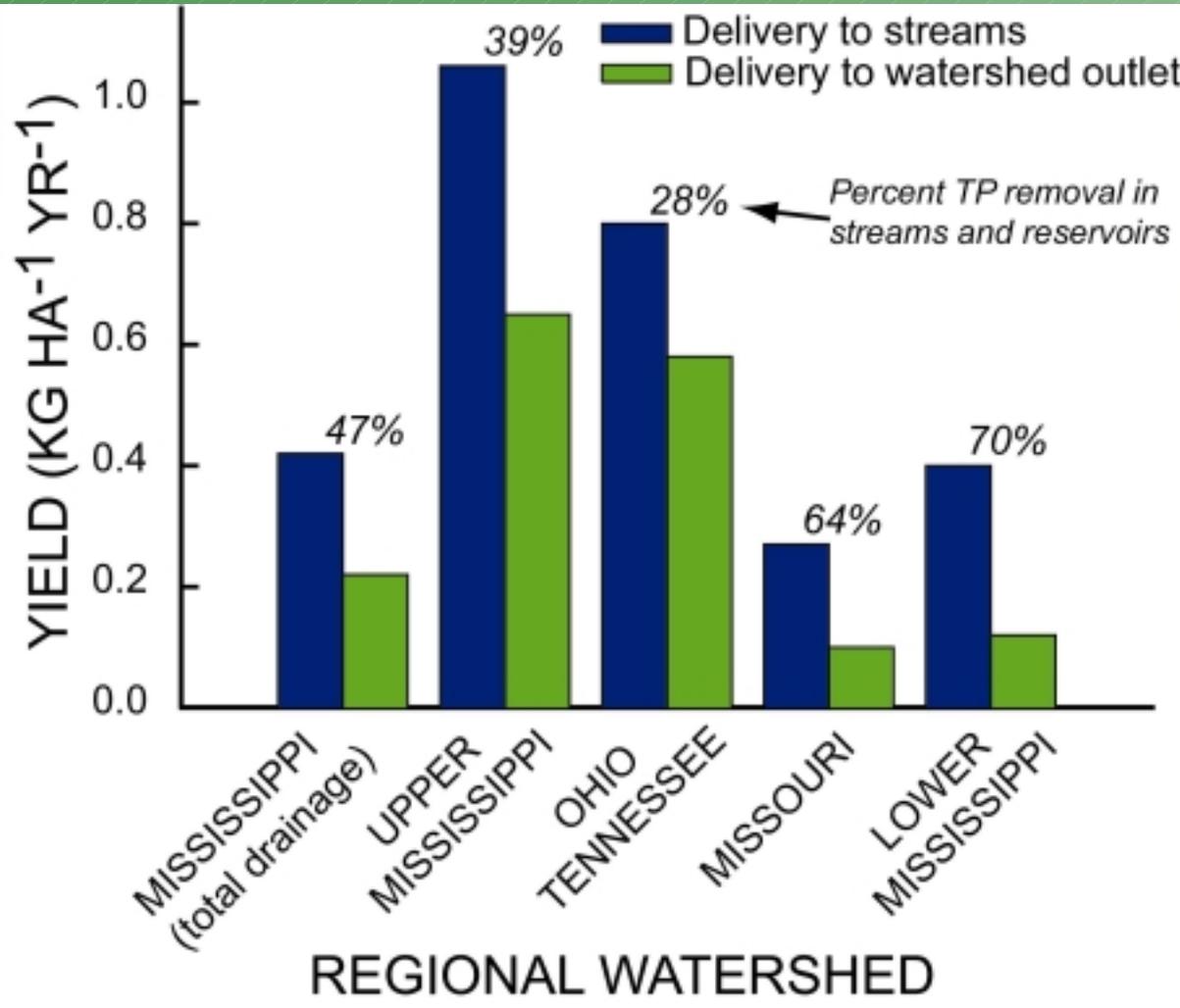


# Sources of Total Phosphorus by Land Use at 336 Stream Monitoring Stations

## *Land-Use vs. Intensive-Source Models*

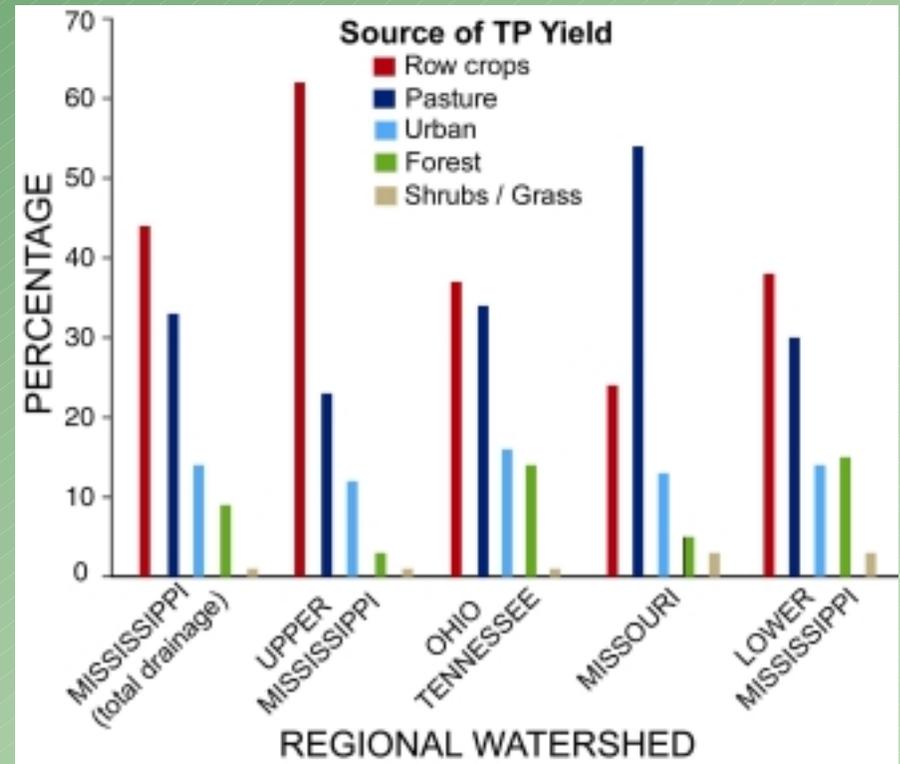
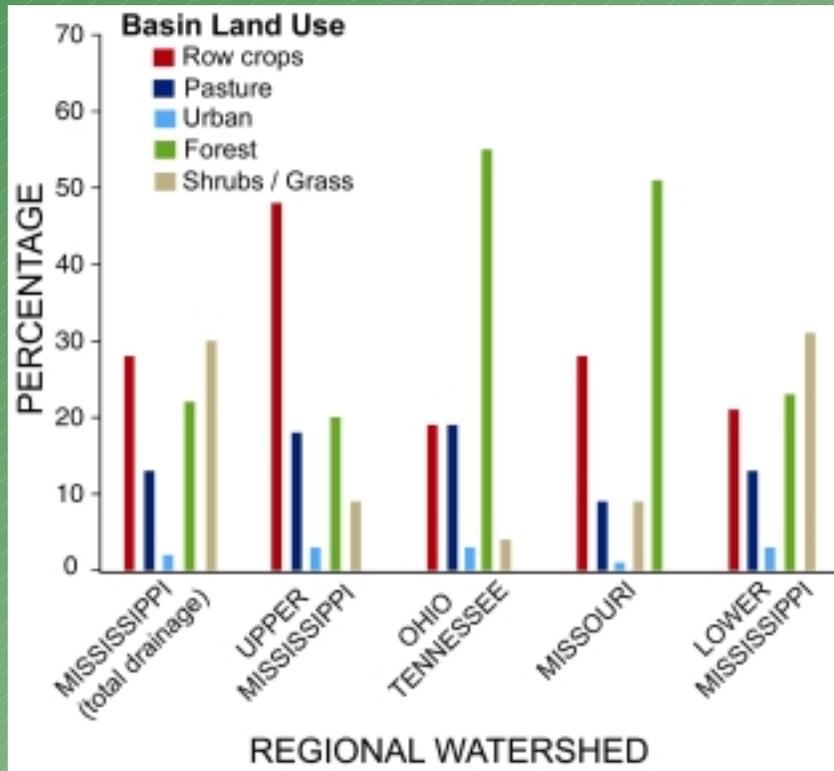


# Mississippi River Basin Total Phosphorus Yield



# Mississippi River Basin

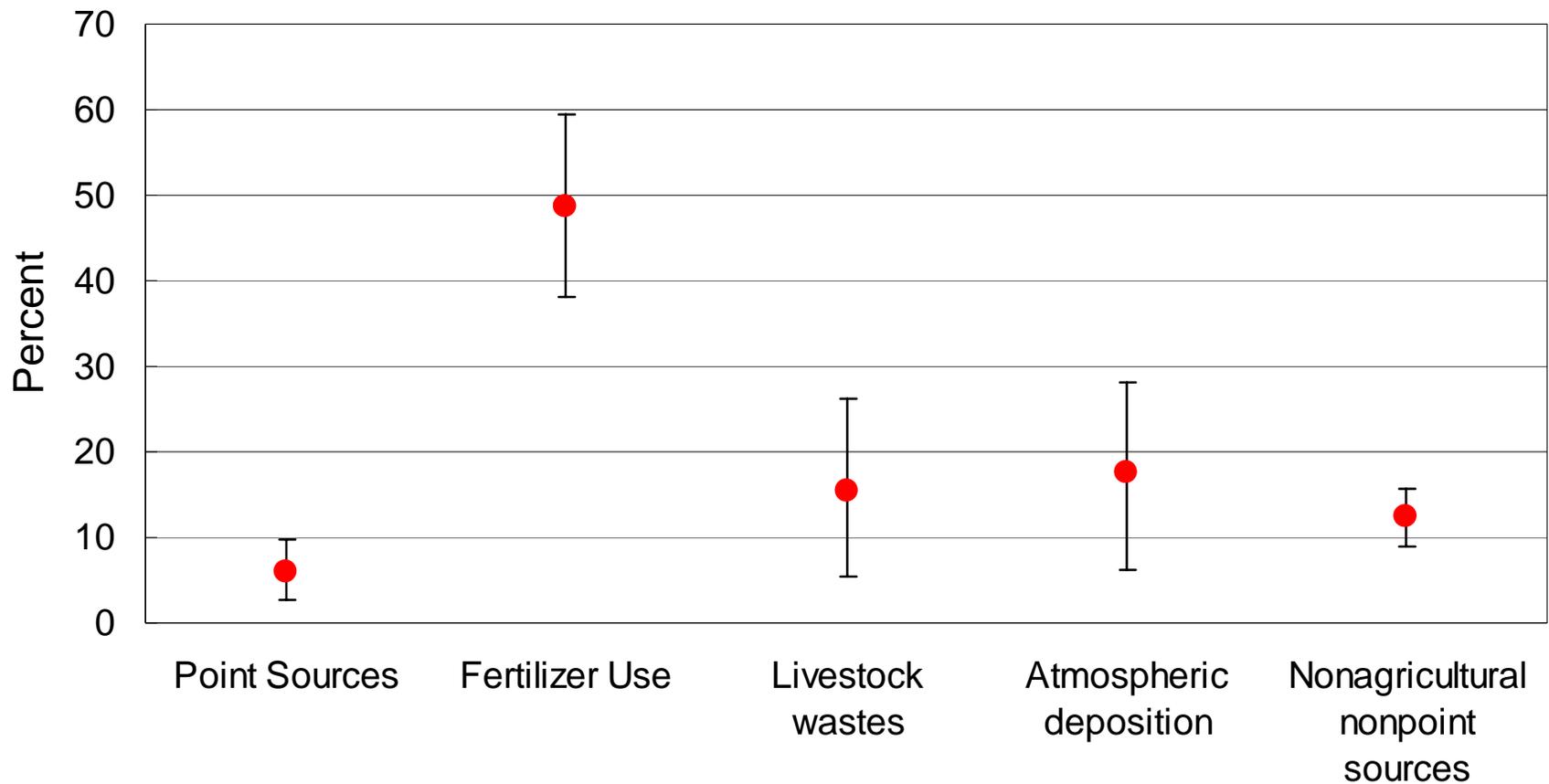
## Watershed Land Use and Source Percentages



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# Contaminant sources and budgets Mississippi River basin

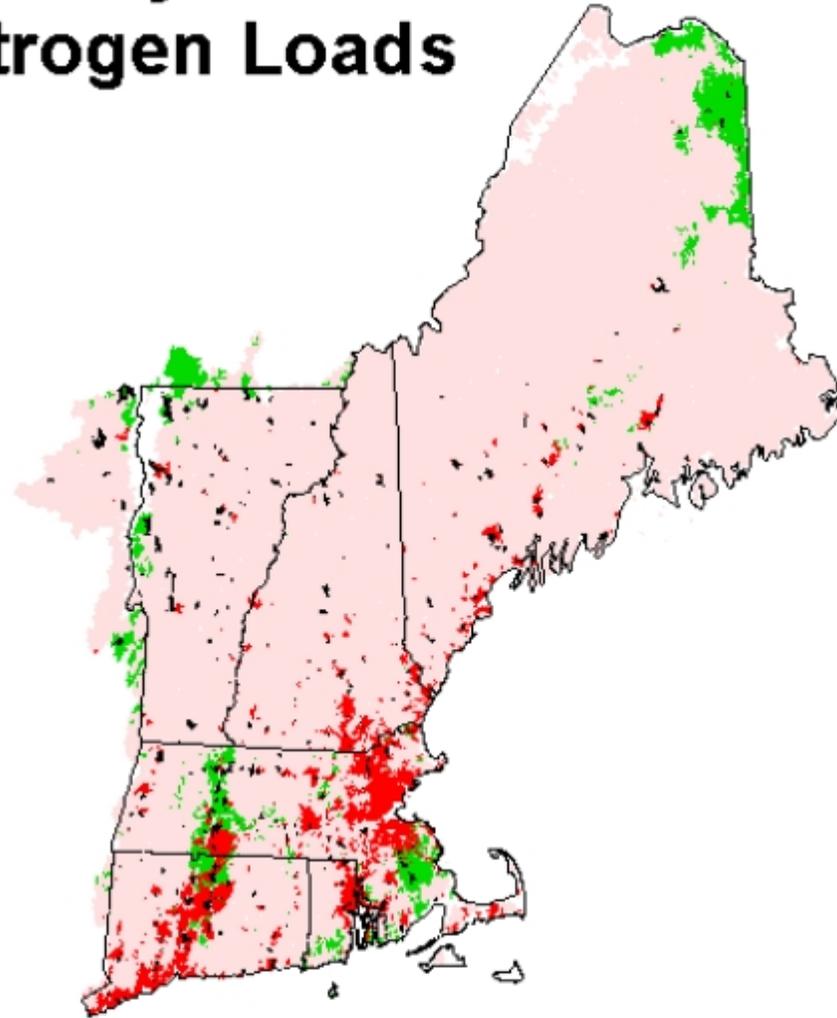
# Sources of Total Nitrogen at the Mississippi River Outlet to the Gulf



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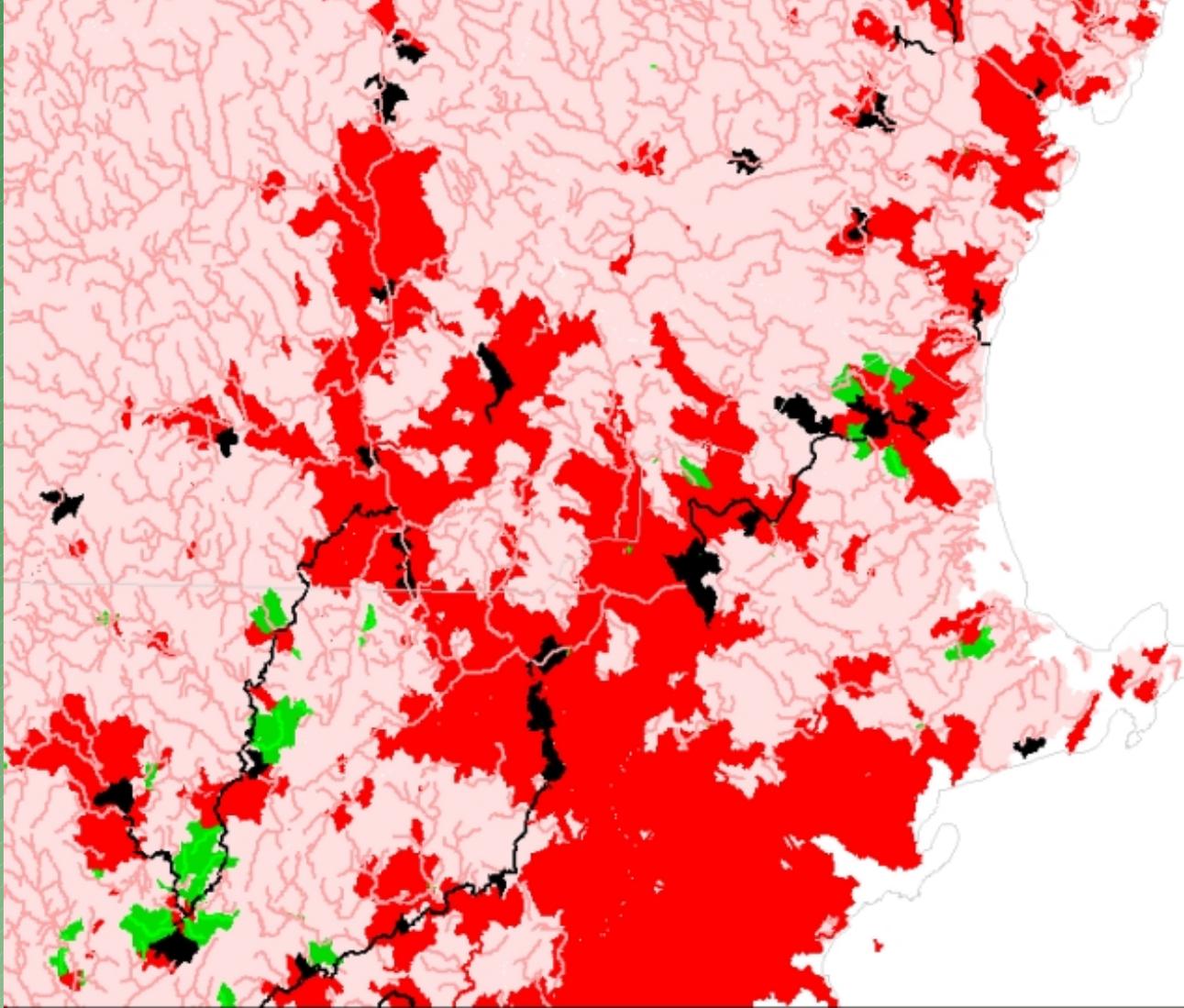
# Contaminant sources and budgets New England Coastal basins

# Primary Sources of Nitrogen Loads



## Primary Source

-  Atmospheric
-  Urban
-  Agriculture (fertilizer)
-  Point Source (sewered)



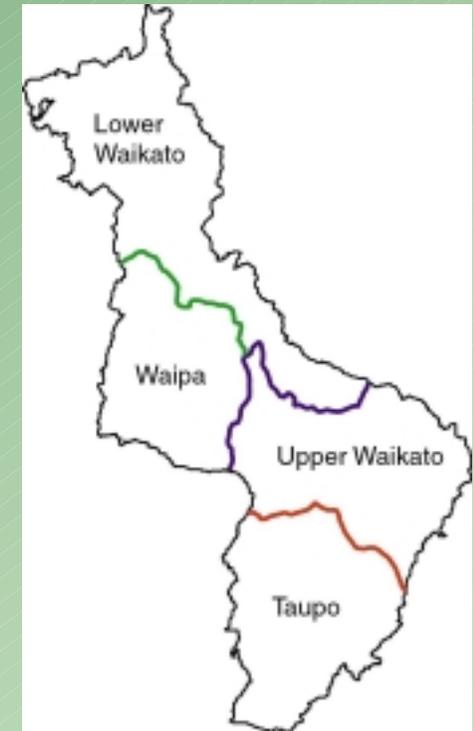
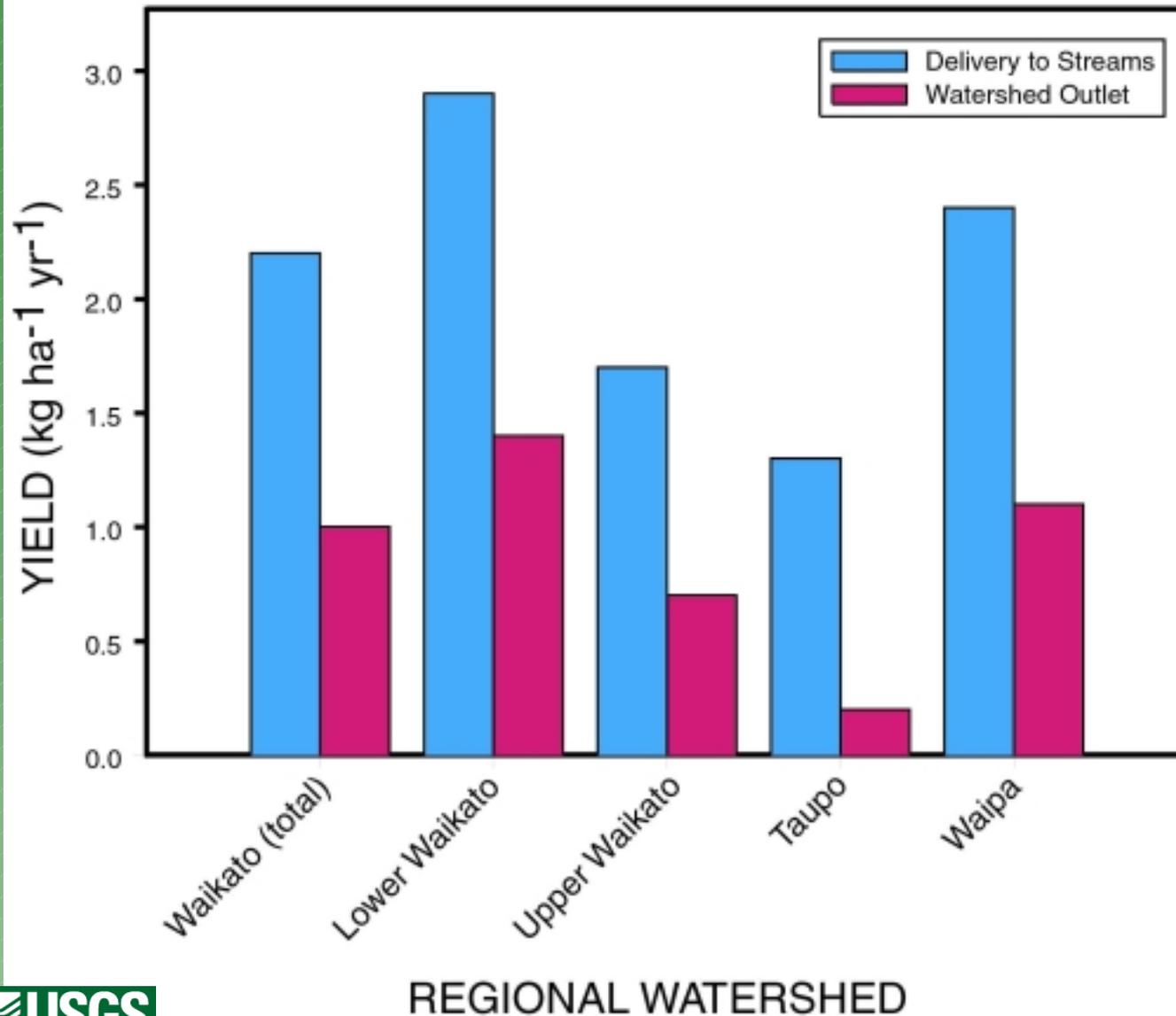
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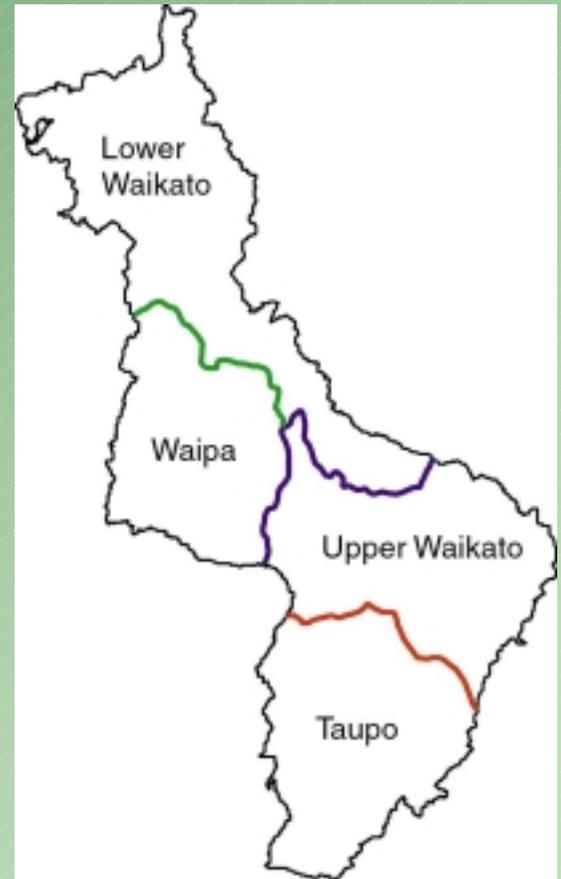
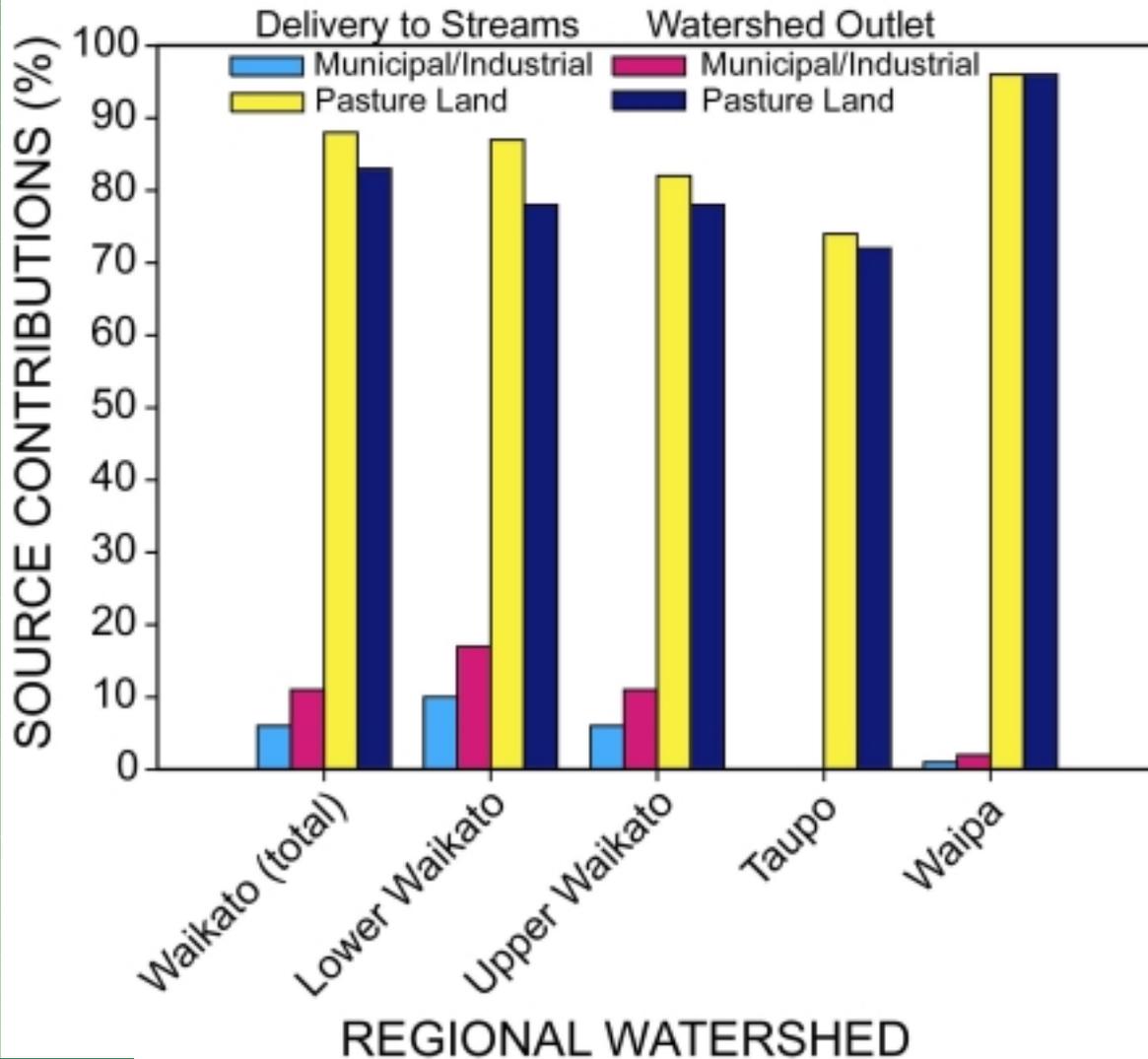
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# Contaminant sources and budgets New Zealand

# Waikato River Basin Total Phosphorus Budget



# Waikato River Basin Total Nitrogen Sources

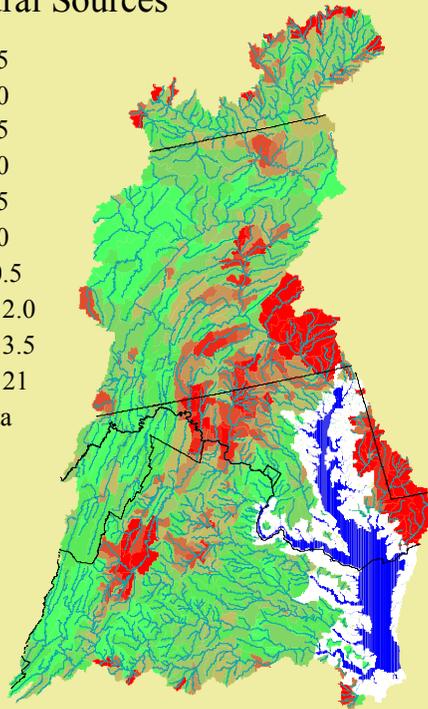
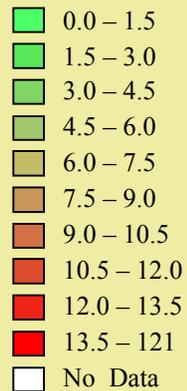


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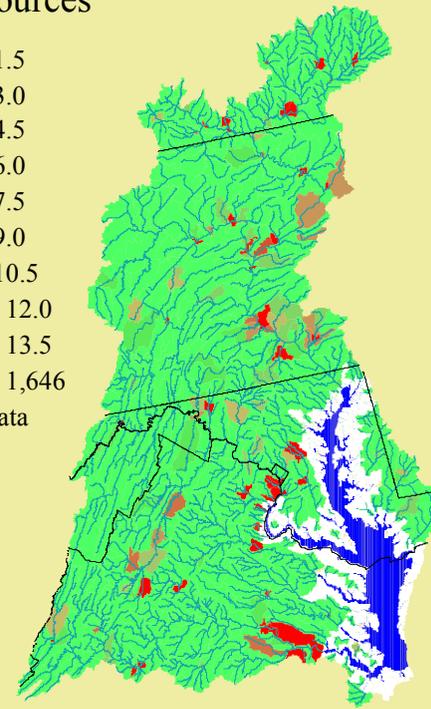
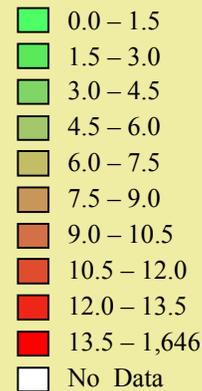
# Contaminant sources and budgets Chesapeake Bay

# Chesapeake Bay Watershed Nitrogen Yield (kg/ha-yr)

Incremental Yield Due to  
Agricultural Sources

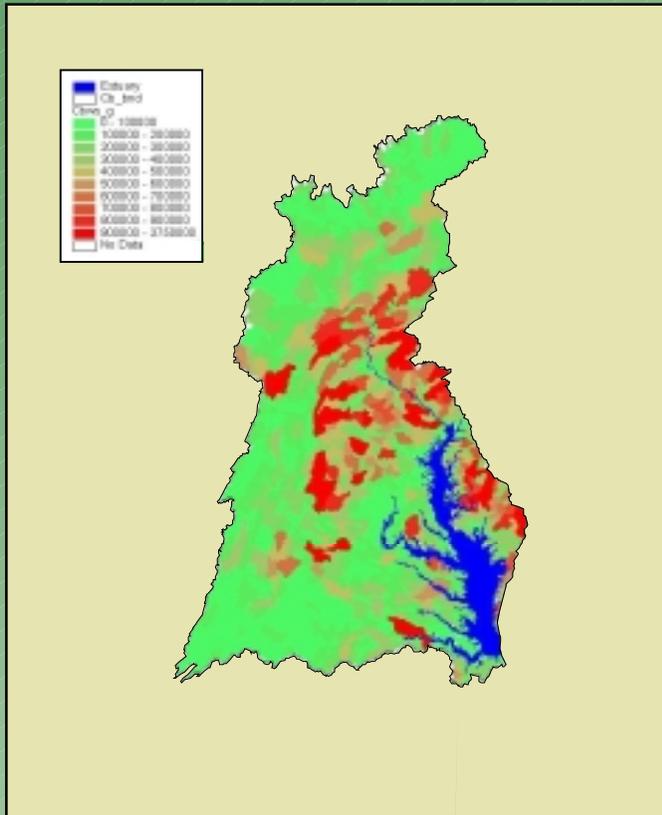


Incremental Yield Due to  
Point Sources

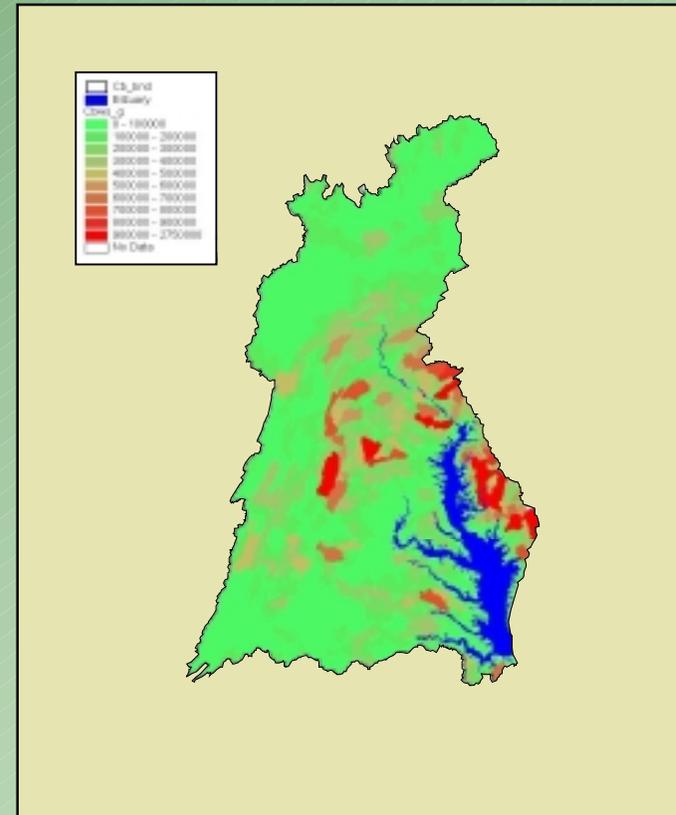


# Fertilizer Nitrogen Data Sets

## SPARROW Version I

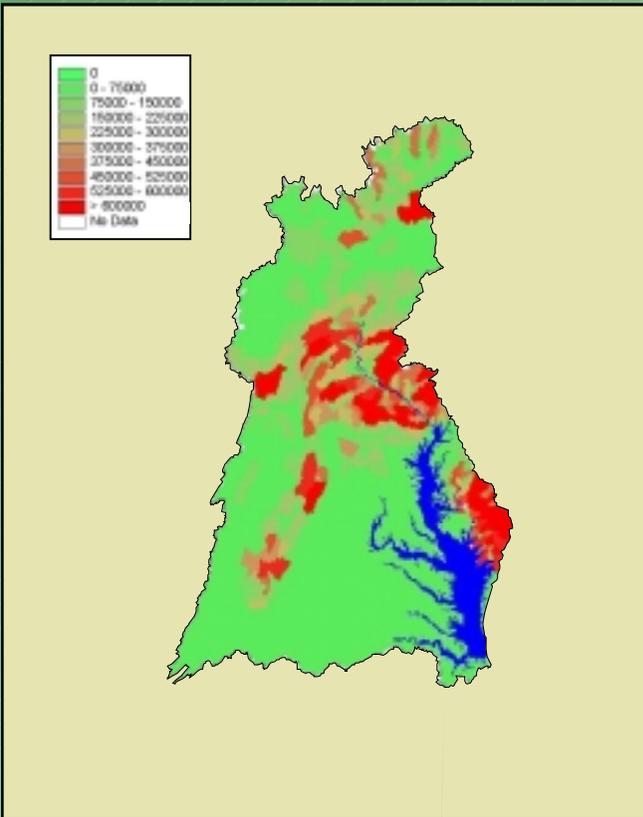


## Fertilizer Sales

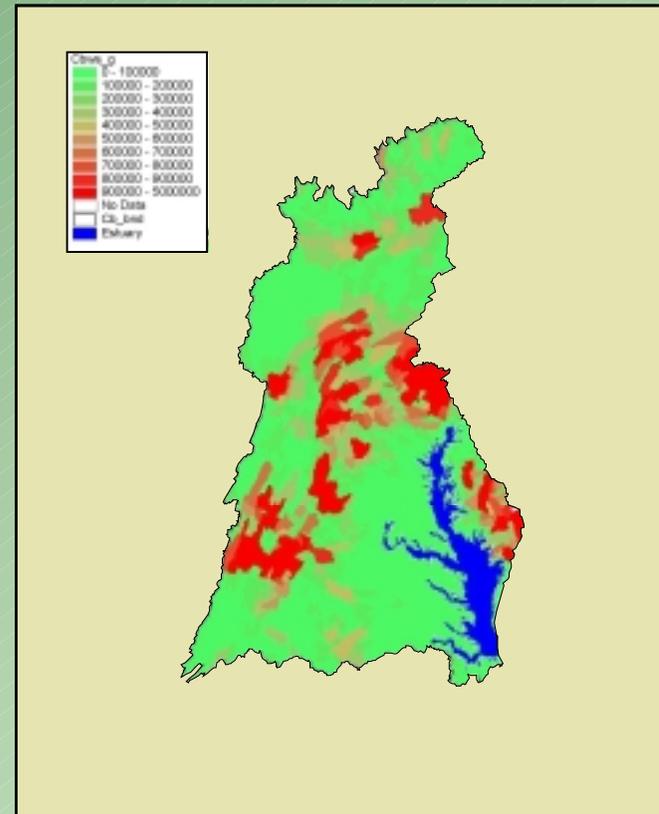


# Manure Nitrogen Data Sets

## SPARROW Version I



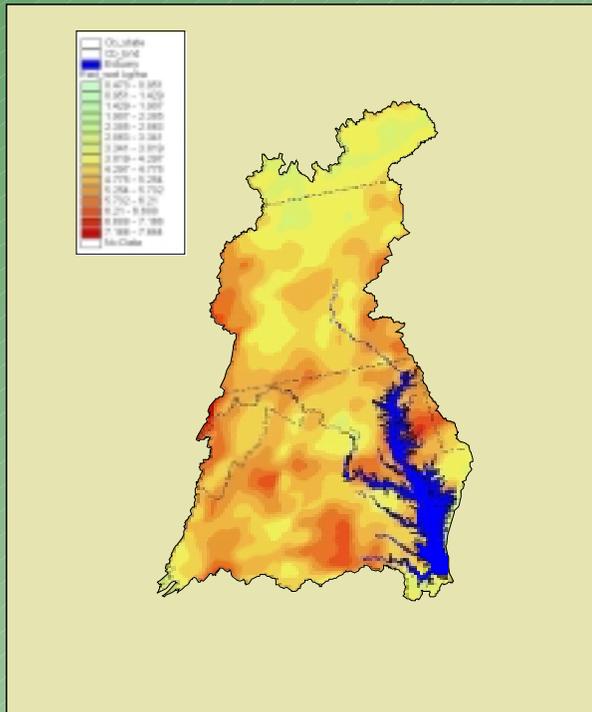
## Census of Agriculture



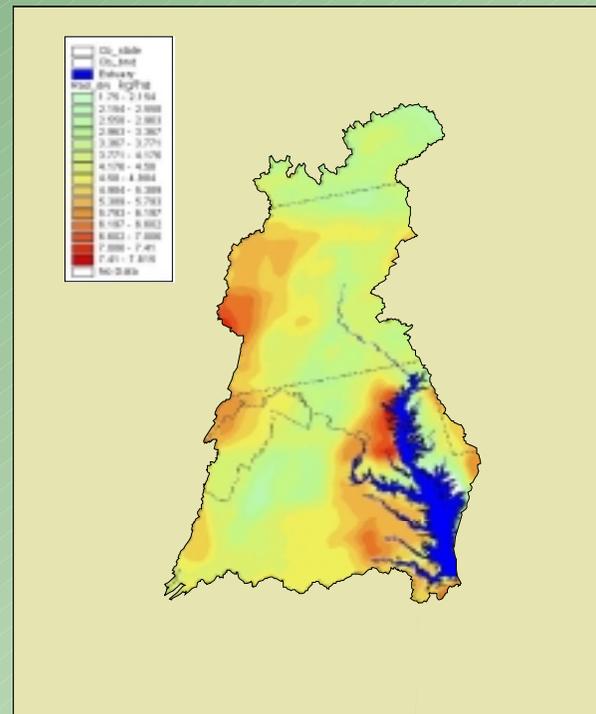


# RADM Wet / Dry Nitrate Deposition Data Sets

Wet  
Deposition

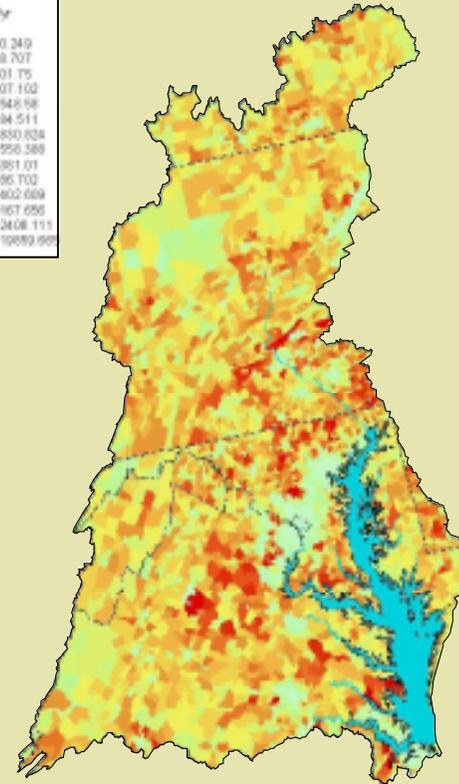


Dry  
Deposition

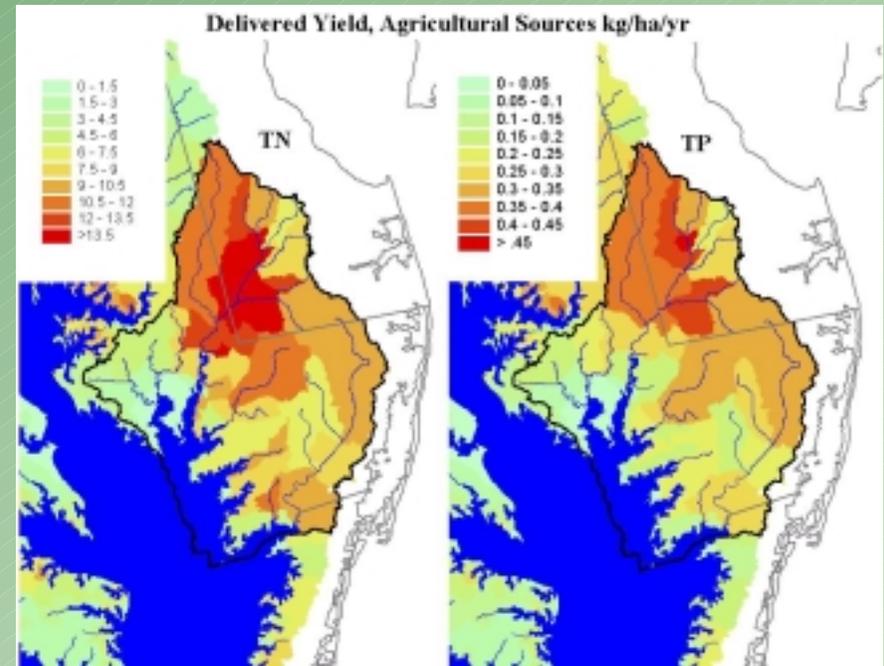
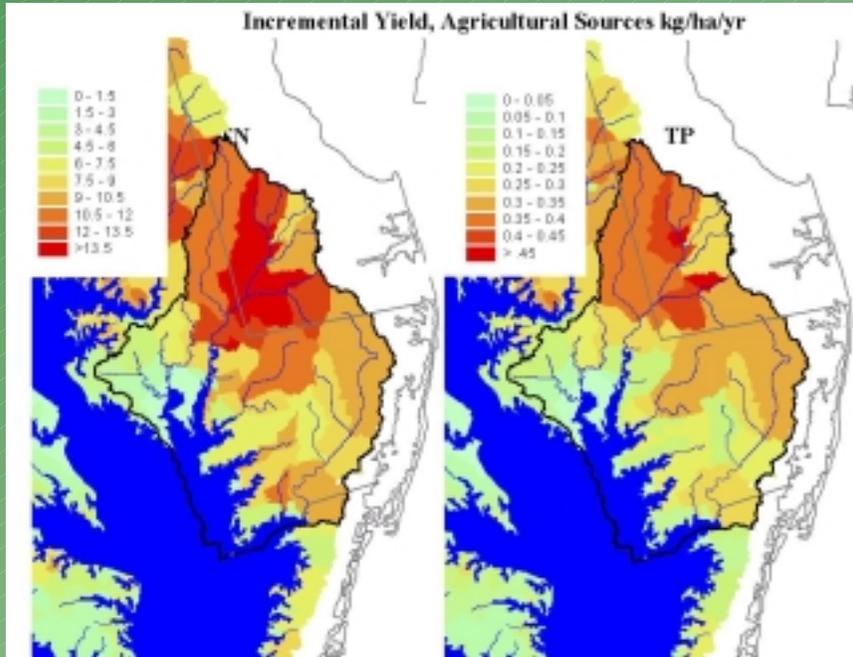


# Septic Tank Loading Data

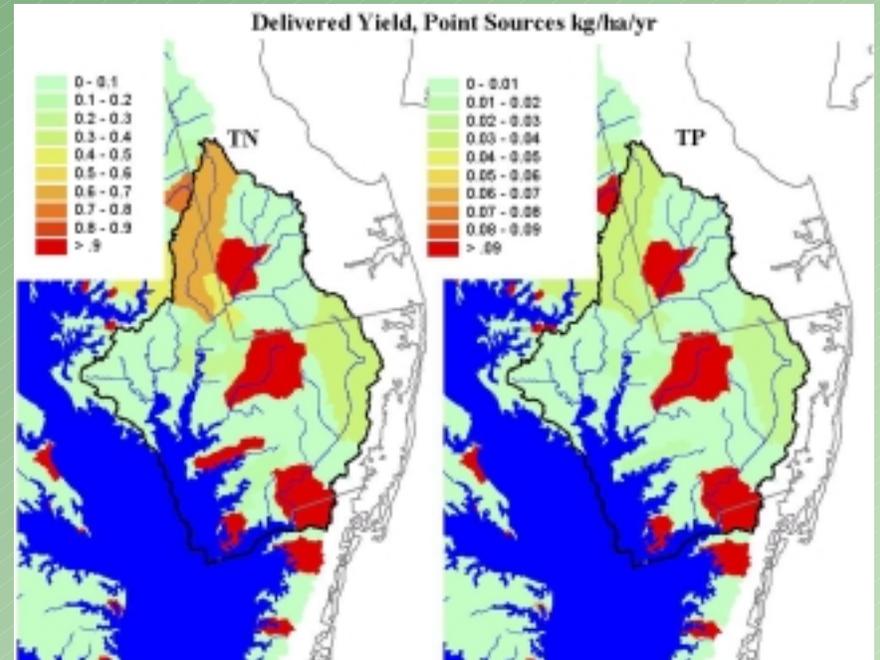
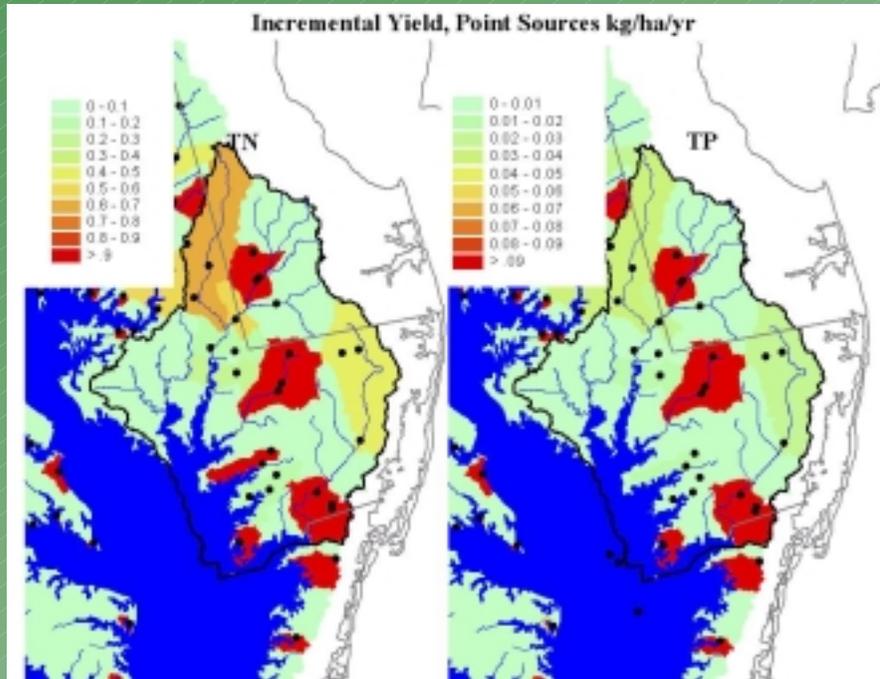
Derived  
From  
Census Information



# Agricultural Yields



# Point Source Yields



# SPARROW Prediction Statistics

## (Mean & Percentiles)

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- Loads/yields exported from watersheds
- Contaminant losses in streams and reservoirs
- Loads/yields delivered to downstream sites (e.g., estuaries, reservoirs)
- Contaminant sources and budgets
- **Concentration**
- Probability of exceeding environmentally relevant load/concentration thresholds

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# Predicting concentration Coastal North Carolina

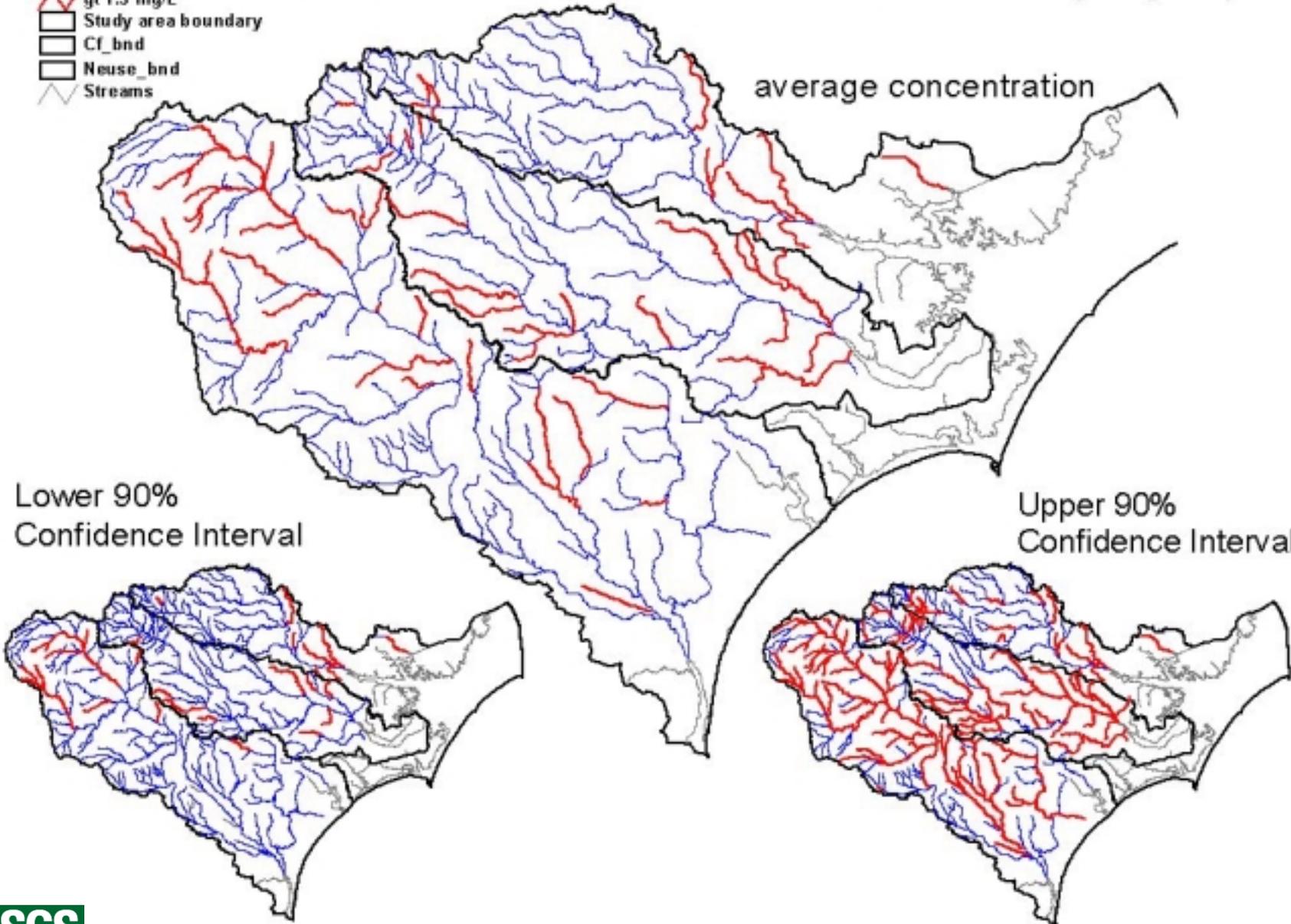
# Predicted TN concentration (mg/L)

- avg\_tn\_concentration
- 0 - 1.5 mg/L
- gt 1.5 mg/L
- Study area boundary
- Cf\_bnd
- Neuse\_bnd
- Streams

average concentration

Lower 90% Confidence Interval

Upper 90% Confidence Interval



# SPARROW Prediction Statistics

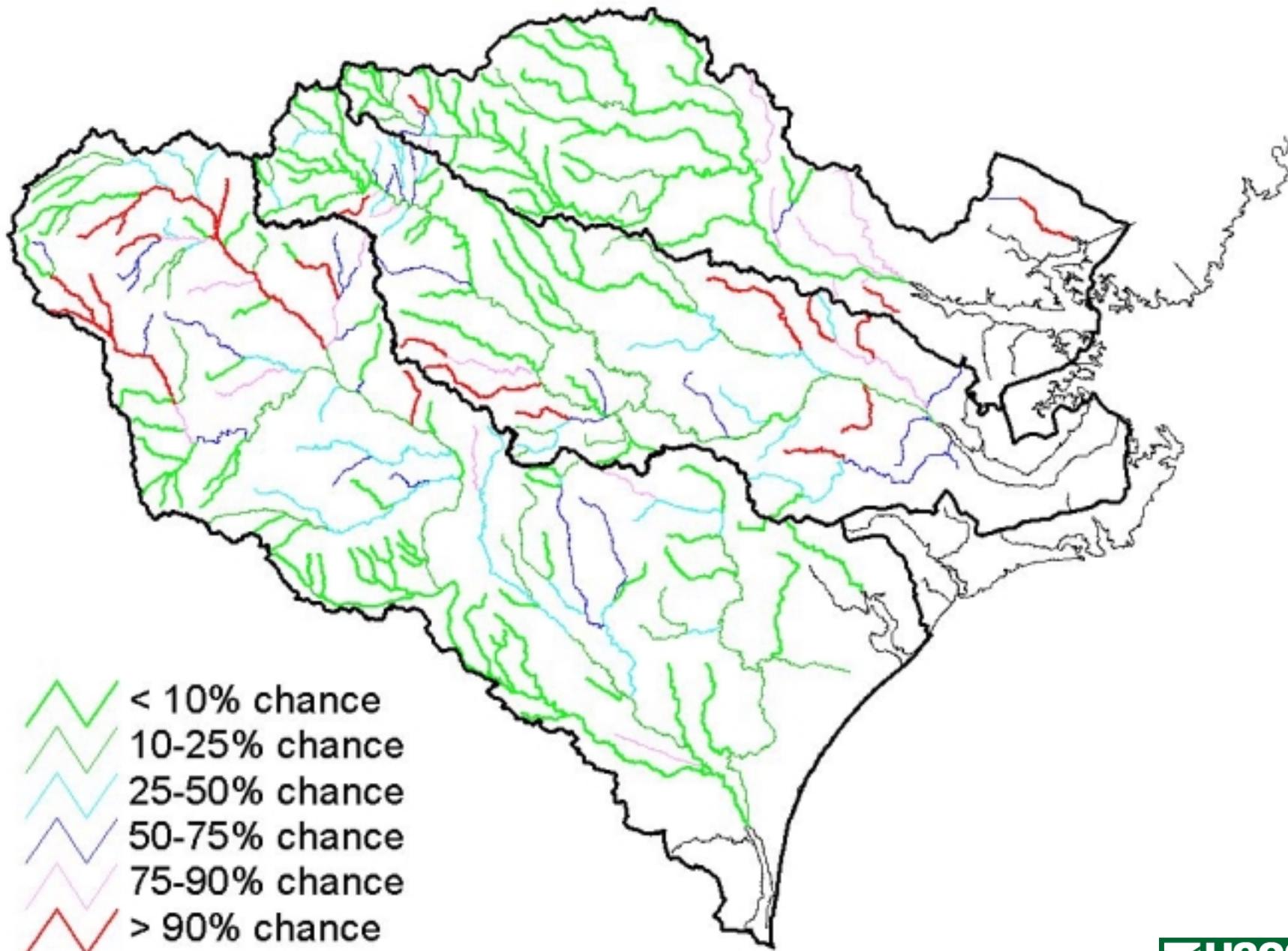
## (Mean & Percentiles)

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- Concentration
- Probability of exceeding environmentally relevant load/concentration thresholds

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# Probability of exceeding thresholds Coastal North Carolina



# SPARROW Management Applications

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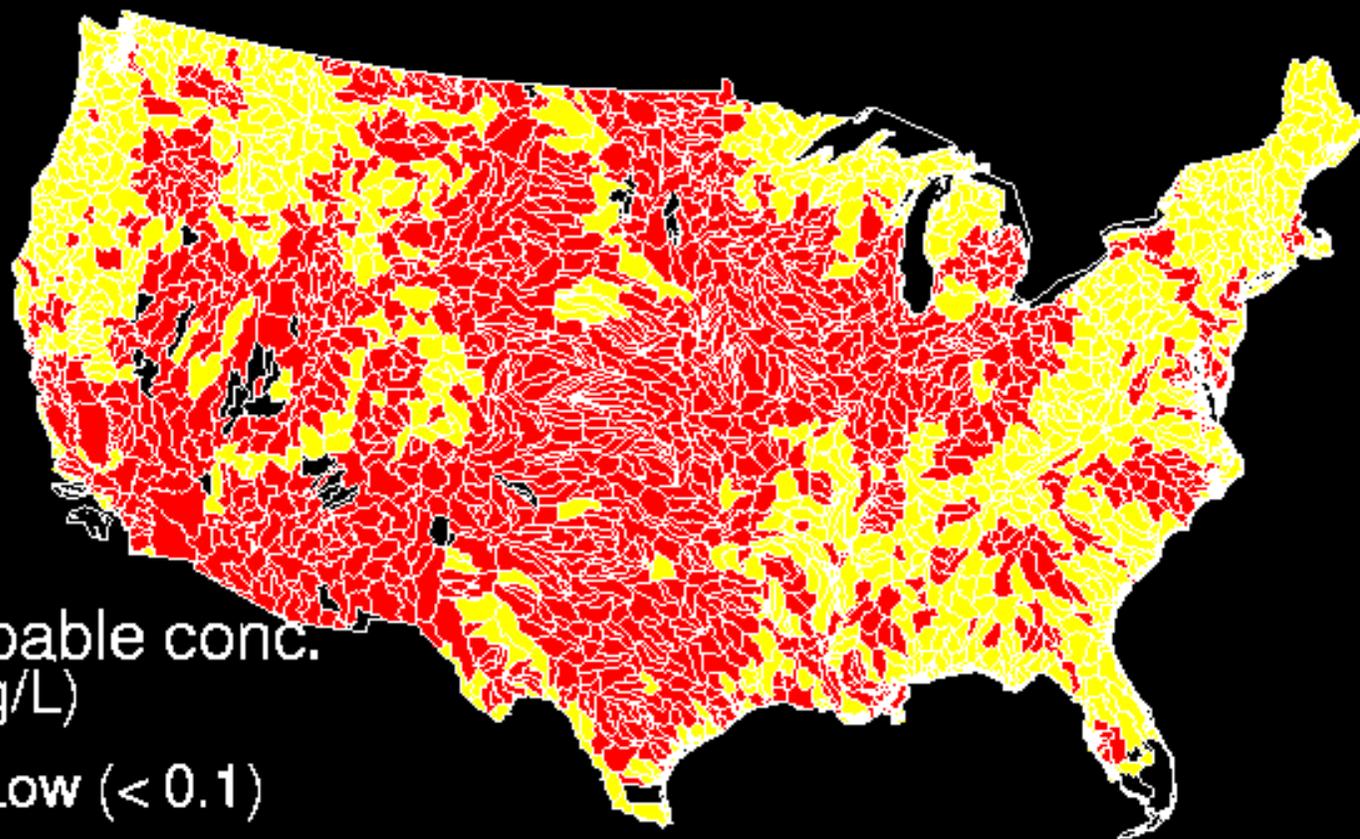
- 305-b Water Quality Assessment
- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking water quality
- Network design

---

## 305b Water Quality Assessment

Estimating proportion of watersheds  
satisfying water quality criteria

# CLASSIFICATION OF PREDICTED TP CONCENTRATION IN HUCs



Probable conc.  
(mg/L)

- Low (< 0.1)
- High (> 0.1)
- No data

# Proportion of Hydrologic Units with TP Concentration < 0.1 mg/L TP Criterion

---

<b>Region</b>	<b>No. HUCs</b>	<b>Proportion</b>	<b>Lower 90% CI</b>	<b>Upper 90% CI</b>
U.S.	2048	0.39	0.37	0.42
New England	52	0.84	0.75	0.90
Mid. Atlantic	88	0.60	0.53	0.67
Upper Miss.	131	0.19	0.15	0.23

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# SPARROW Management Applications

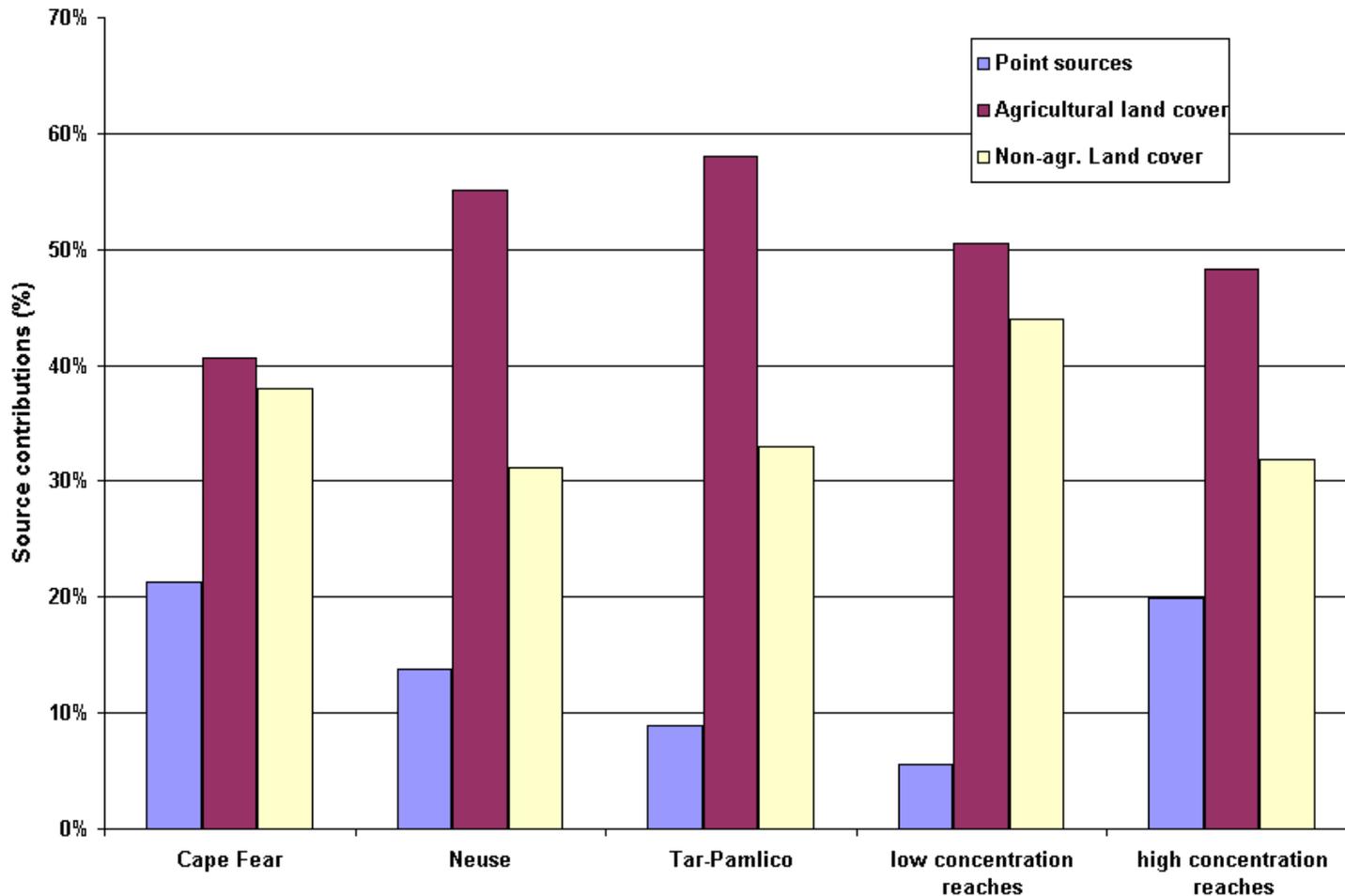
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- 305-b Water Quality Assessment
- TMDL
- Studying change over time
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- Natural background
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- Network design

---

**TMDL**  
**Baseline TN loads**  
**Coastal North Carolina**

# Understanding baseline nitrogen source contributions

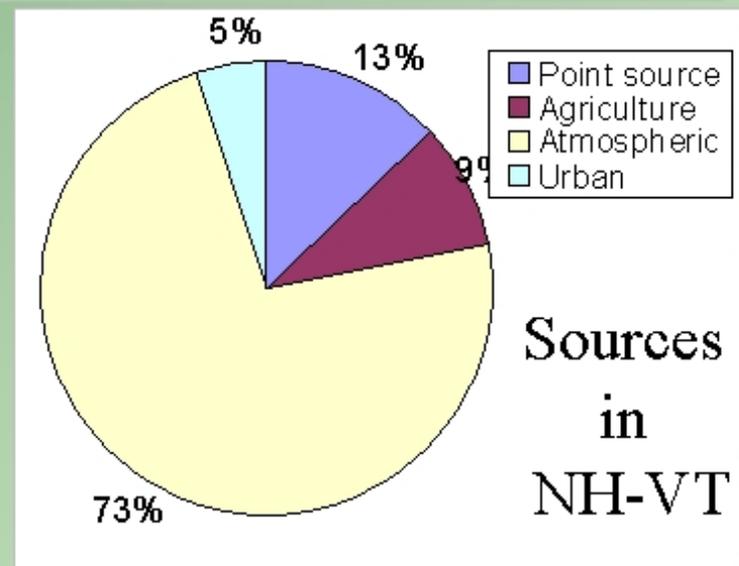
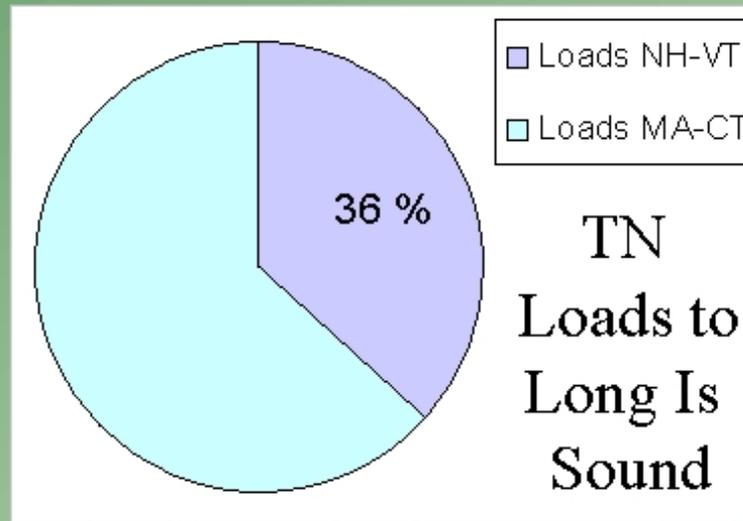
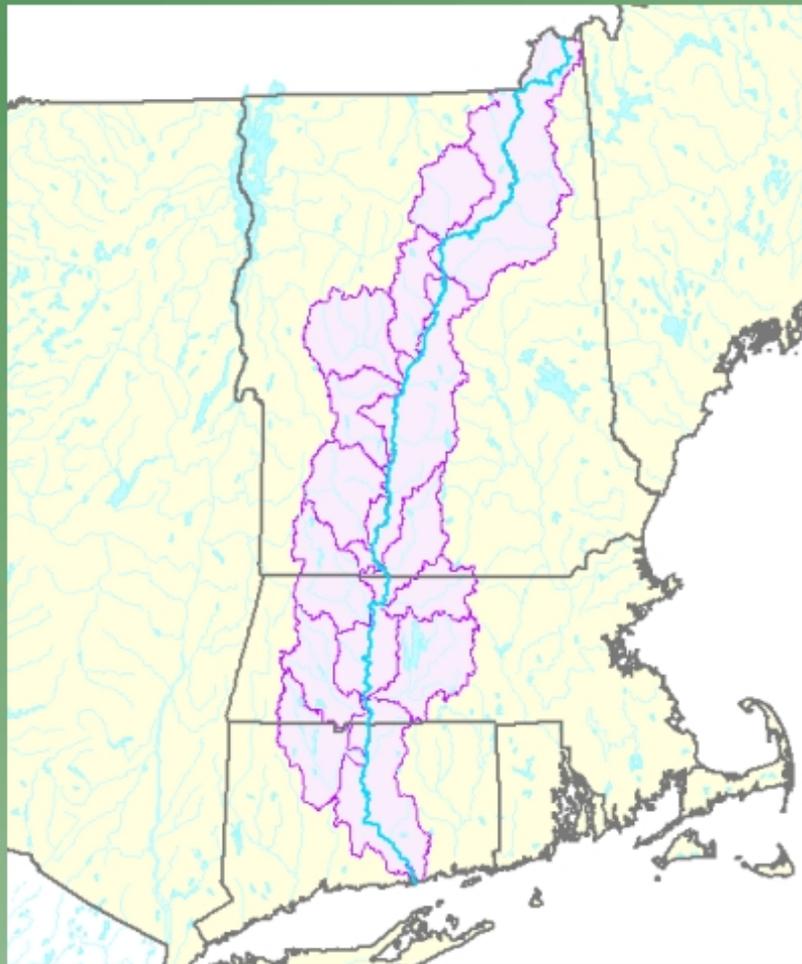


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**TMDL**  
**Baseline TN loads**  
**New England Coastal basins**

# Utility of New England SPARROW Model

## Results for TMDL Applications – An Example from the Connecticut River Basin



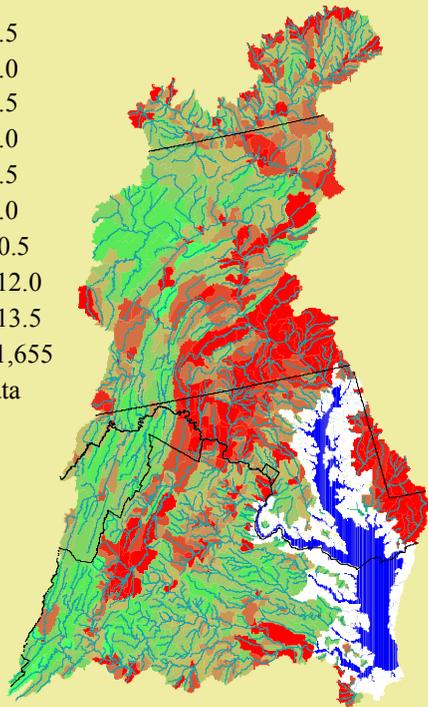
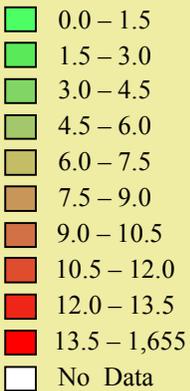
# SPARROW Management Applications

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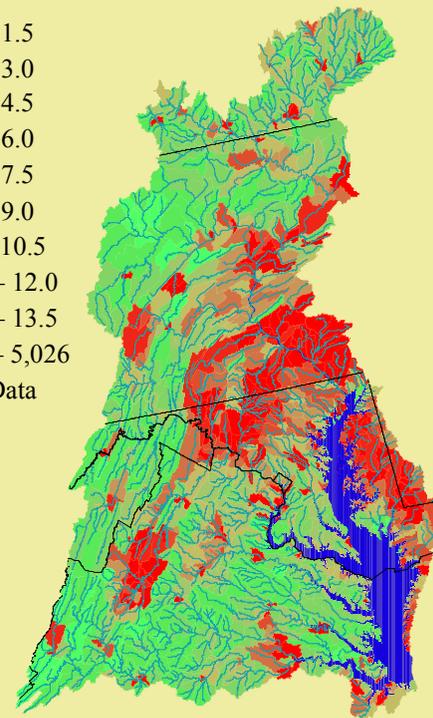
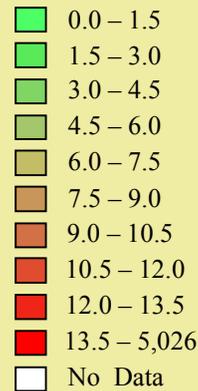
- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking water quality
- Network design

# Chesapeake Bay Watershed Total Nitrogen – Incremental Yield (kg/ha-yr)

Version I - 1987



Version II - 1992



# SPARROW Management Applications

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- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking water quality
- Network design

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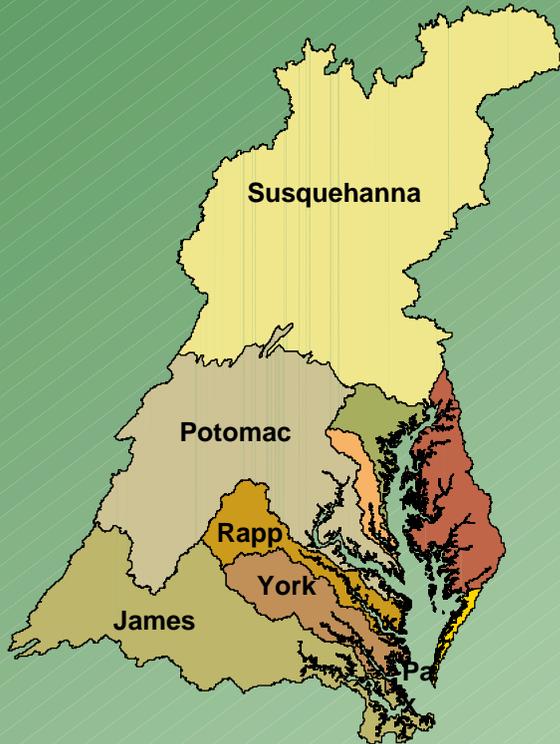
# Chesapeake Bay

Establishing Nutrient-Load Allocations

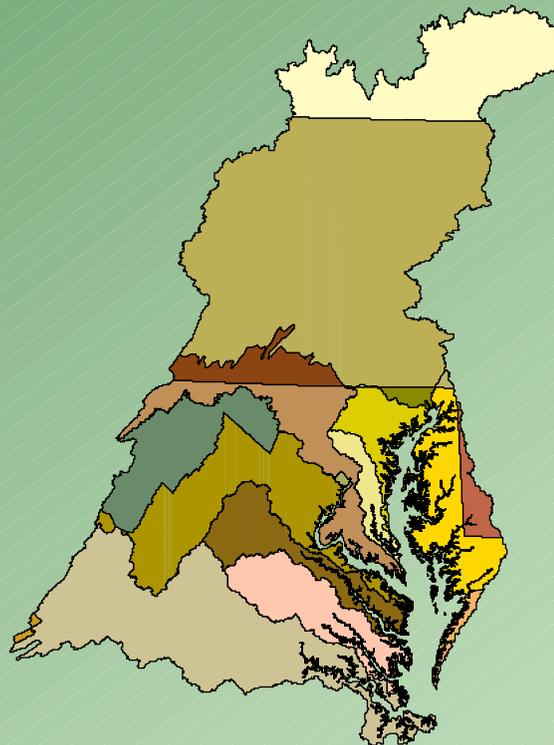
Joint Application of SPARROW and HSPF

# Setting Load Allocations

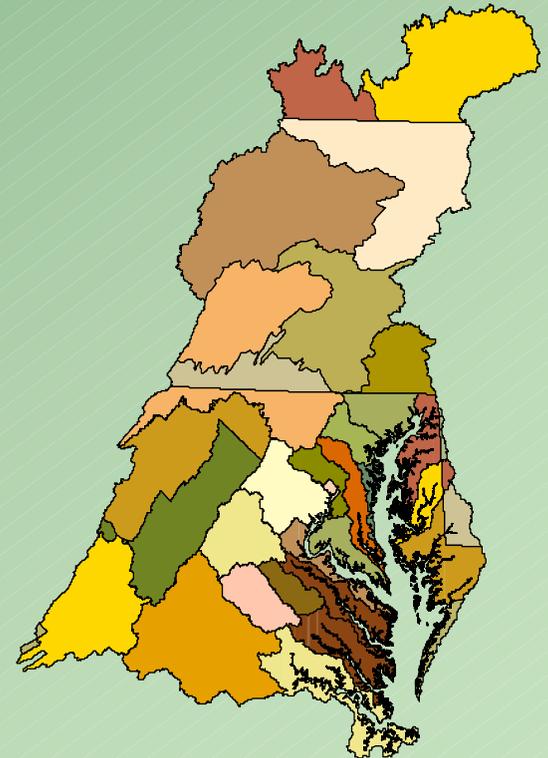
Allocate Loading Caps to the 9 Major Basins



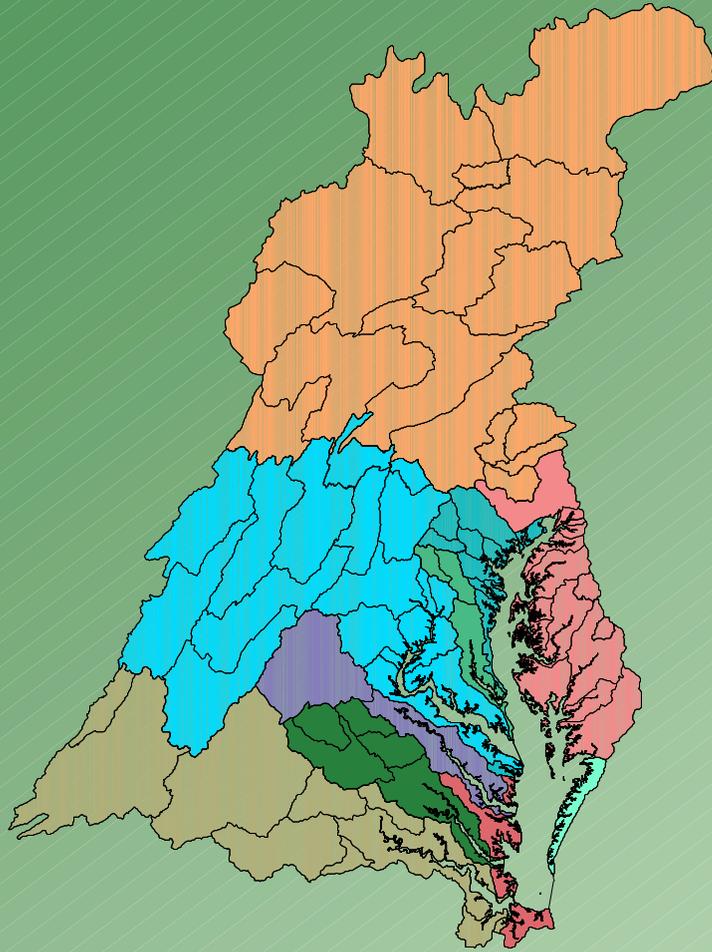
Further allocate cap load responsibilities to each state



Further allocate major tributary basin load caps to 37 state defined sub-basins



# Chesapeake Bay Program Watershed Model - HSPF



## Description of Modeling Framework

- Deterministic
- Process Oriented
- Spatially and Temporally Defined
- Temporally Detailed

## Chesapeake Bay Application

- Deliver Nutrient and Sediment Loads to Separate Estuarine Water-Quality Model
- Establish Nutrient and Sediment Allocations by Drainage Area and Land Use Type
- Develop Stream Load Predictions for Various Scenarios of Management-Practice Implementation

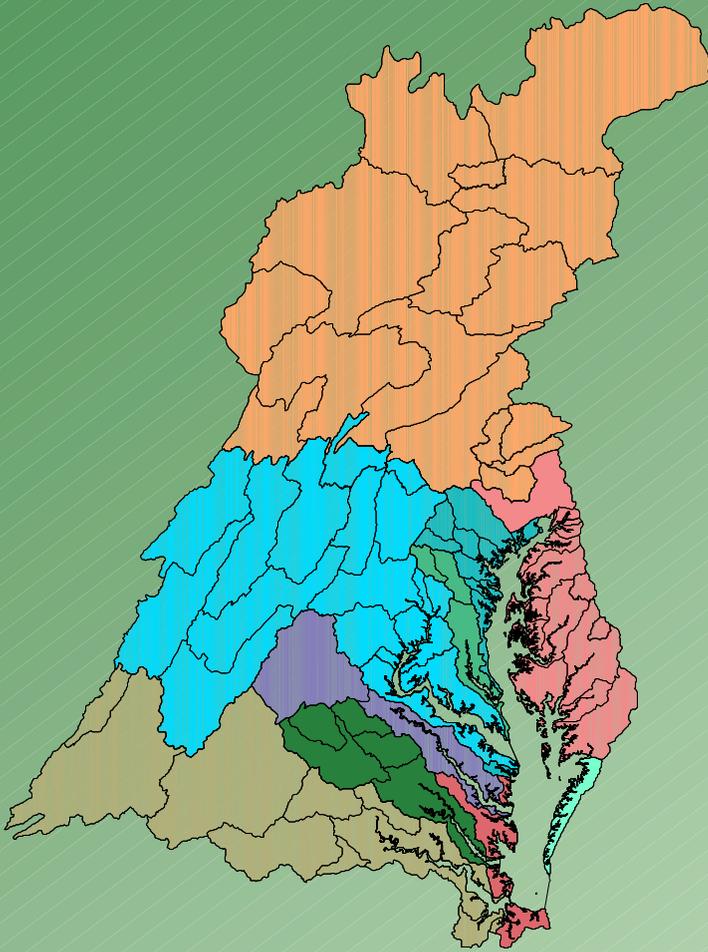
# Chesapeake Bay Program Watershed Model - HSPF

## Limitations of Modeling Framework

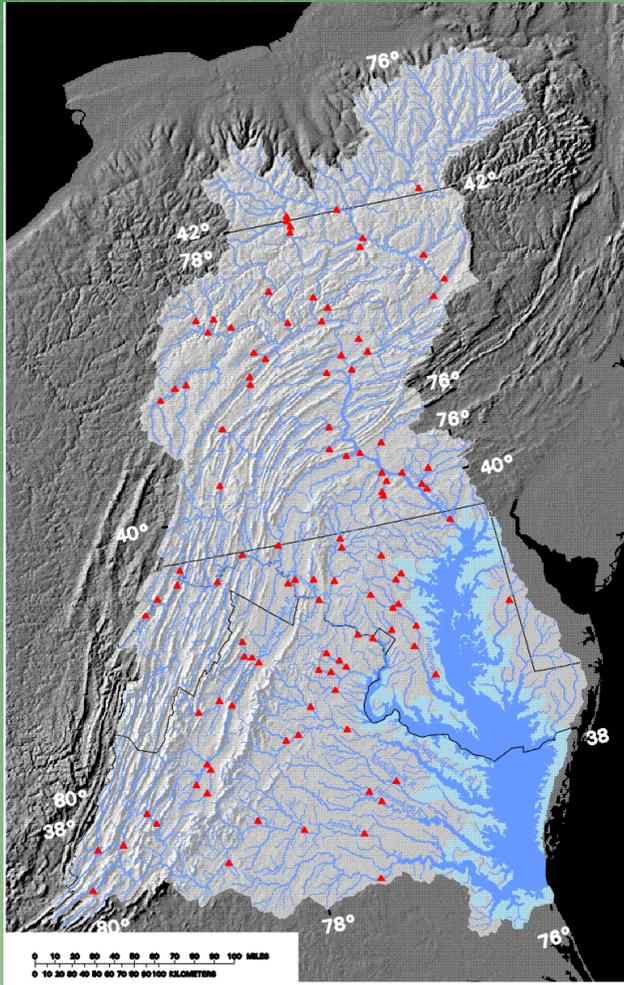
- Over-Parameterized
- Labor-Intensive Manual Calibration
- Spatial Coarseness
- No Systematic Method of Assessing Error

## Why is HSPF Necessary?

- Designed for Studying the Relations of Human Activities on the Landscape to Nutrient and Sediment Loads of Streams
- Allows Simulation of “ALL” Human Activities that Affect Stream Loads
- Allows the Simulation of Management-Practices to Assess Their Effectiveness and Optimize the Efficient Use of Resources



# U.S. Geological Survey - SPARROW



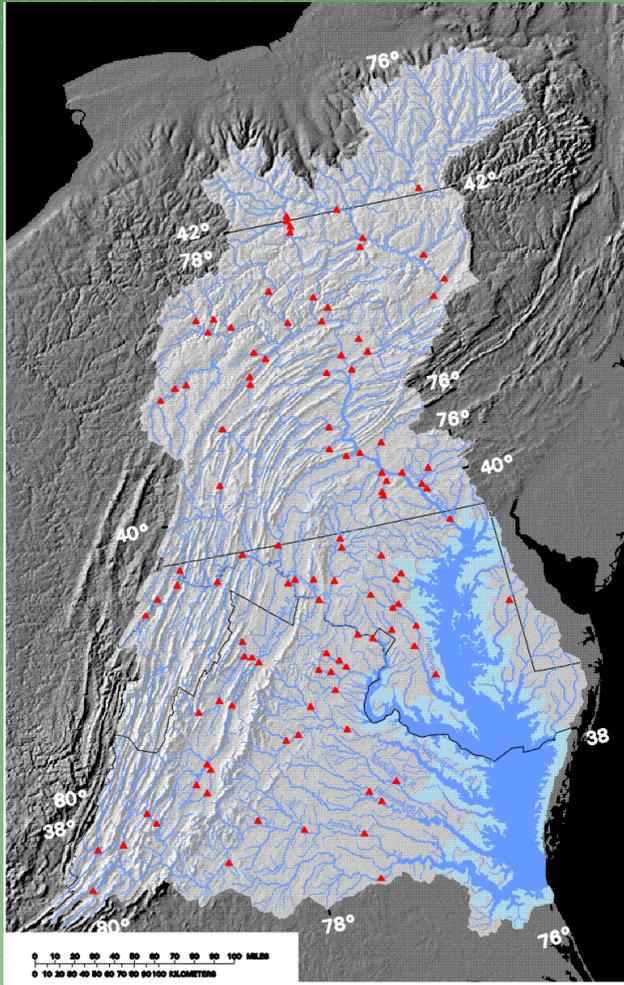
## Description of Modeling Framework

- Statistical
- Designed to Define Spatial Relations Between Contaminant Sources and Stream Loads
- Spatially Defined Only
- Spatially Detailed

## Chesapeake Bay Application

- Provide Framework for Relating Various Types of Detailed Geographic Data to Stream Nutrient Loads
- Statistically Identify the Environmental Factors that are Most Closely Related to Stream Loads
- Provide Spatially Detailed Estimates of Stream Load for Targeting and Other Uses

# U.S. Geological Survey - SPARROW



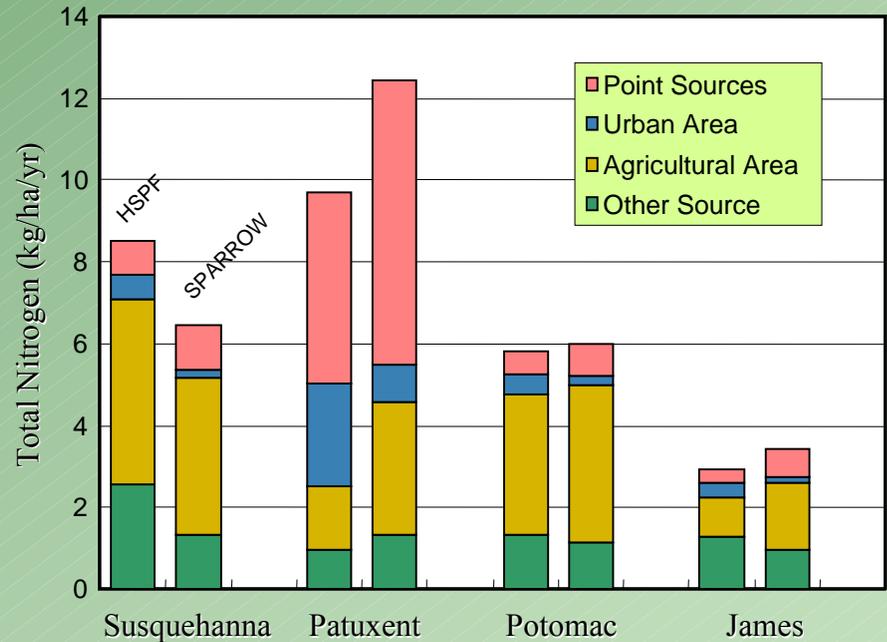
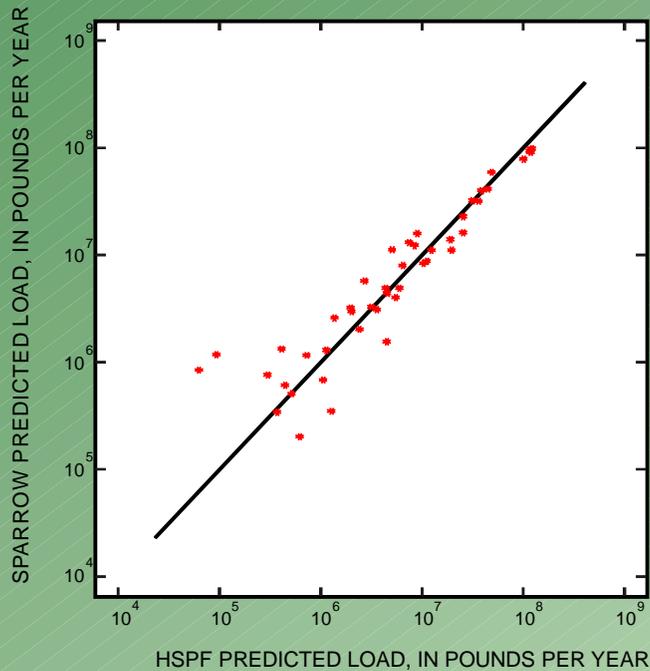
## Limitations of SPARROW

- No Temporal Definition
- Extremely Data Intensive
- Predictions Based Only on Statistically Significant Variables

## Why is SPARROW Useful?

- Provides a Statistical Basis for Watershed Modeling and Estimates of Error Associated With All Predictions
- Provides Spatially Detailed Predictions of Stream Loads
- Provides a Basis for Spatially Detailed Assessment of the Relative Importance of Factors Affecting Stream Loads

# Chesapeake Bay Watershed SPARROW / HSPF Comparison

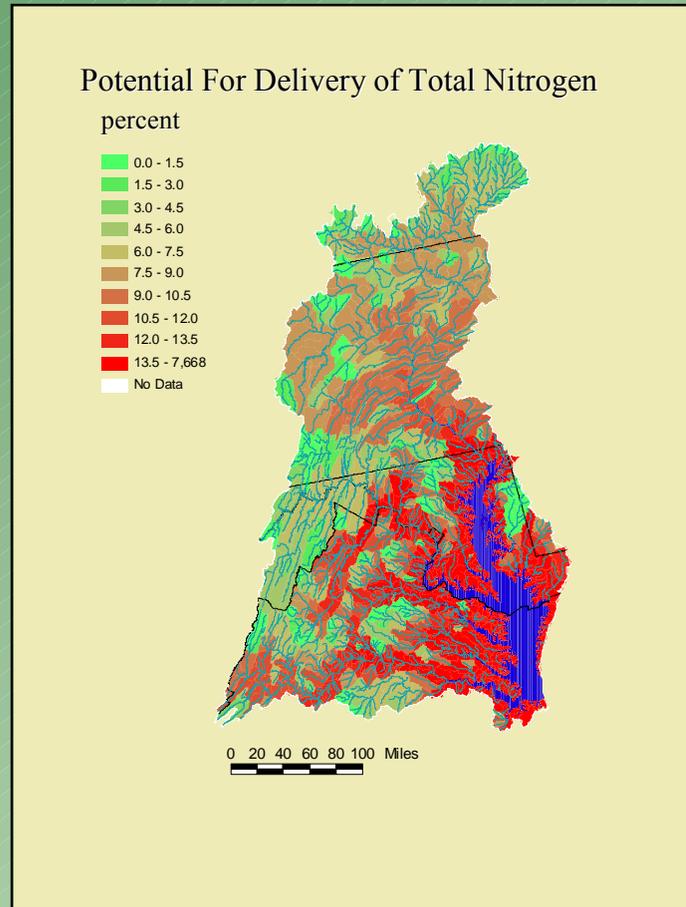


# Joint Application of SPARROW and HSPF in the Chesapeake Bay Watershed

1. Feedback Between SPARROW and HSPF
2. Use of SPARROW for Targeting / HSPF for Evaluating Tributary Specific Management Plans
3. Use of SPARROW for Targeting / HSPF for Evaluating Load Allocations Among Large Basins for Criteria Attainment

# Joint Application of SPARROW and HSPF

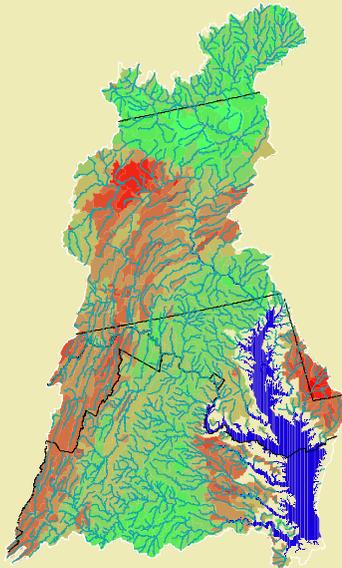
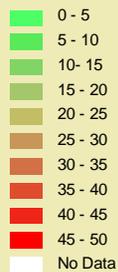
## Model Feedback - Instream Loss Rates



# Joint Application of SPARROW and HSPF

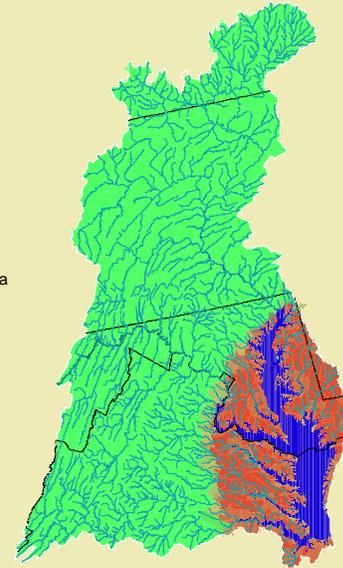
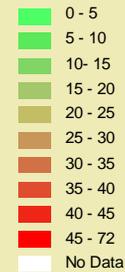
## Model Feedback – Identification of Significant Variables

Loss Associated With Soil Permeability  
percent



0 20 40 60 80 100 Miles

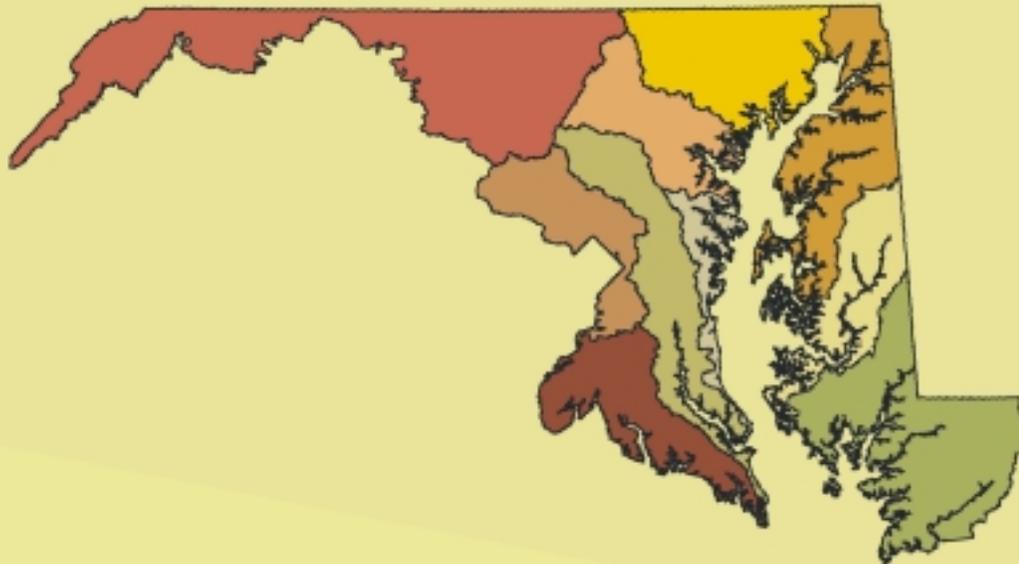
Loss Associated With Coastal Plain  
percent



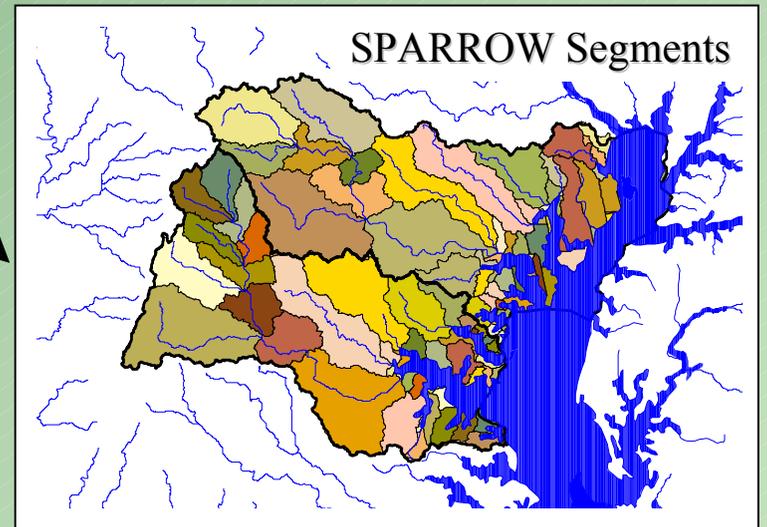
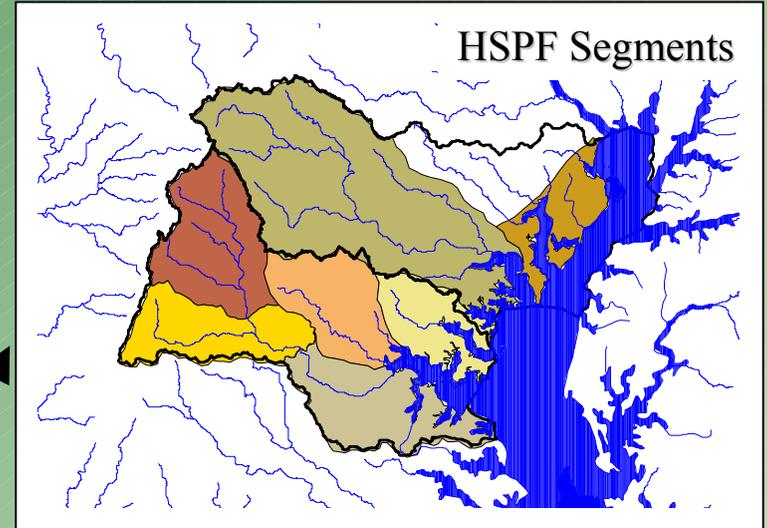
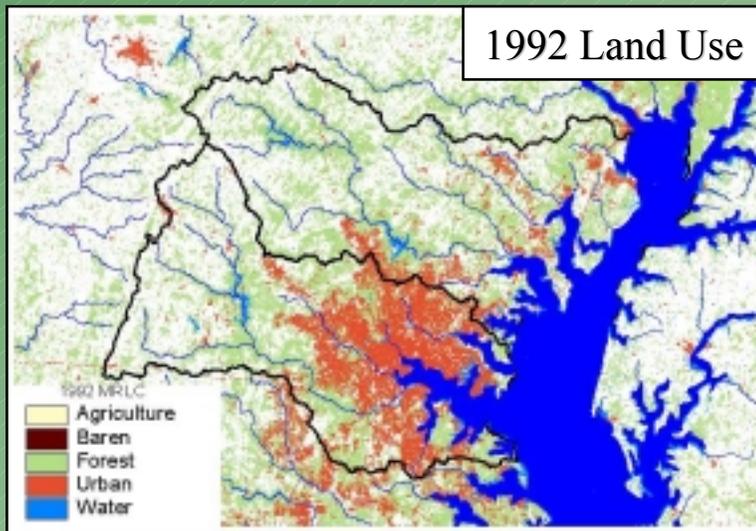
0 20 40 60 80 100 Miles

# Joint Application of SPARROW and HSPF Targeting – Area Specific Management Plans

Maryland Tributary Strategy Drainages

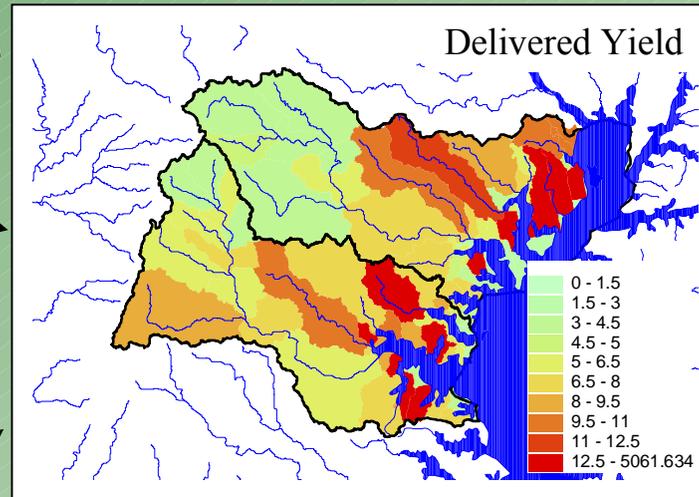
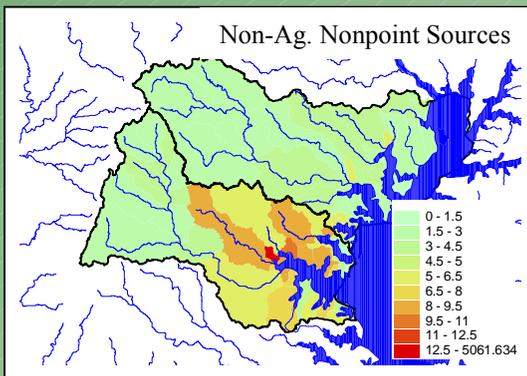
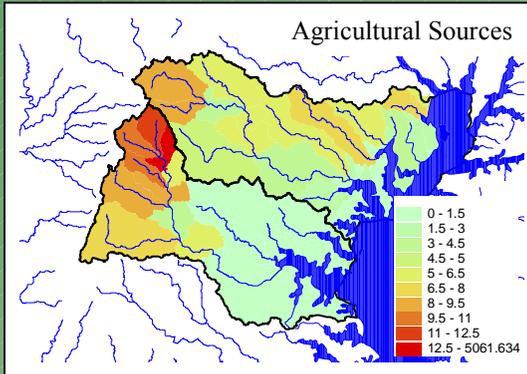
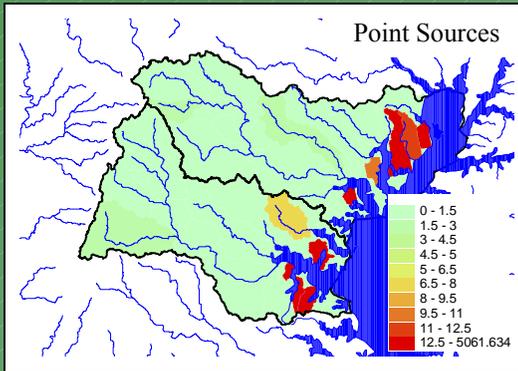


# Joint Application of HSPF and SPARROW Targeting – Area Specific Management Plans



# Joint Application of SPARROW and HSPF

## Targeting – Area Specific Management Plans



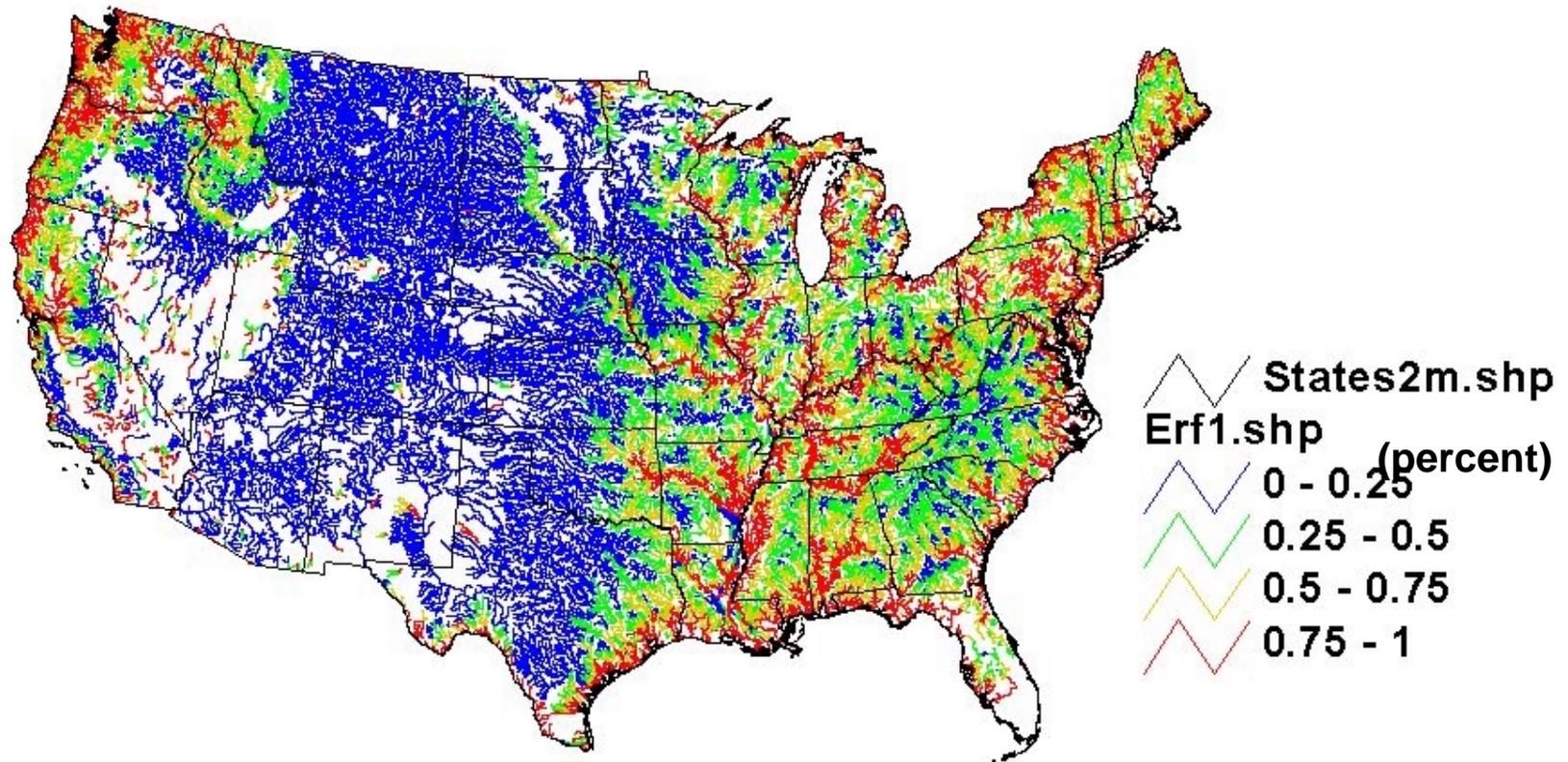
Management Scenario

Test With HSPF

---

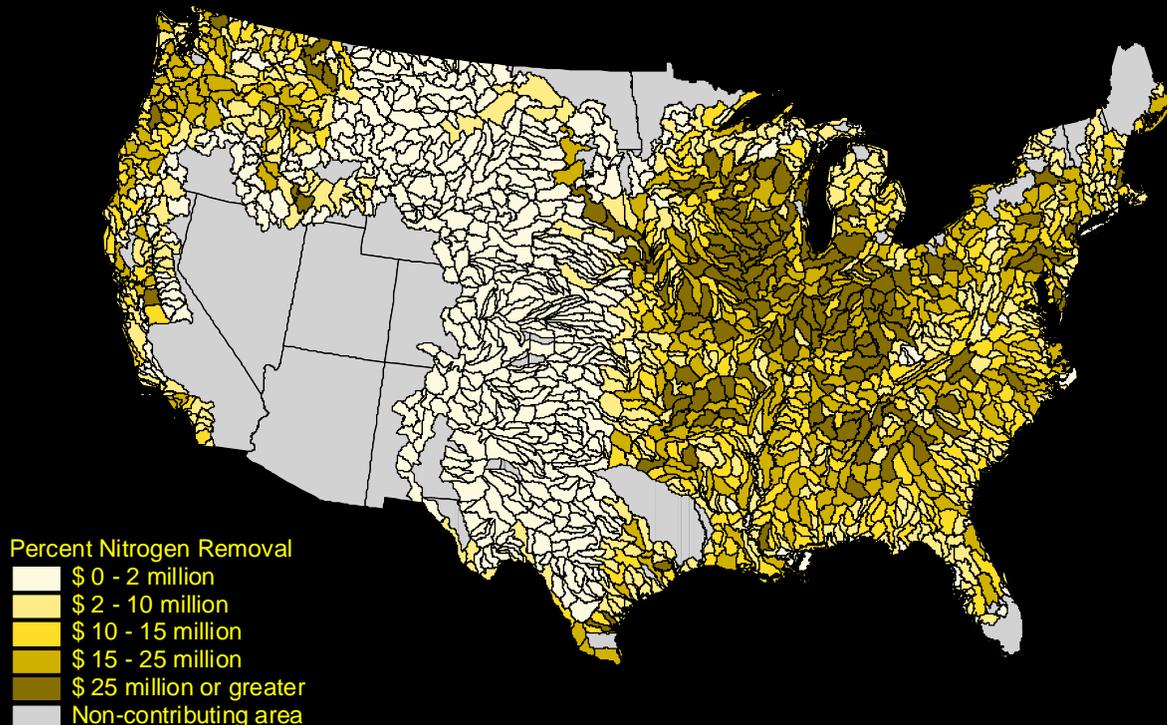
# Economically Efficient Targeting of Nutrient Controls

# Percentage of N Export Delivered to the Coast



# Application of SPARROW to Evaluate Control Strategies for Reducing Nitrogen Flux to Estuaries

## Cost of Optimal Nitrogen Removal in Hydrologic Units to Obtain a 40 Percent Reduction at Estuaries



Differences in in-stream decay rates make it more efficient to control watersheds near large rivers.

The cost of the optimal strategy is 40% less than the cost of a uniform strategy.

# SPARROW Management Applications

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- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking water quality
- Network design

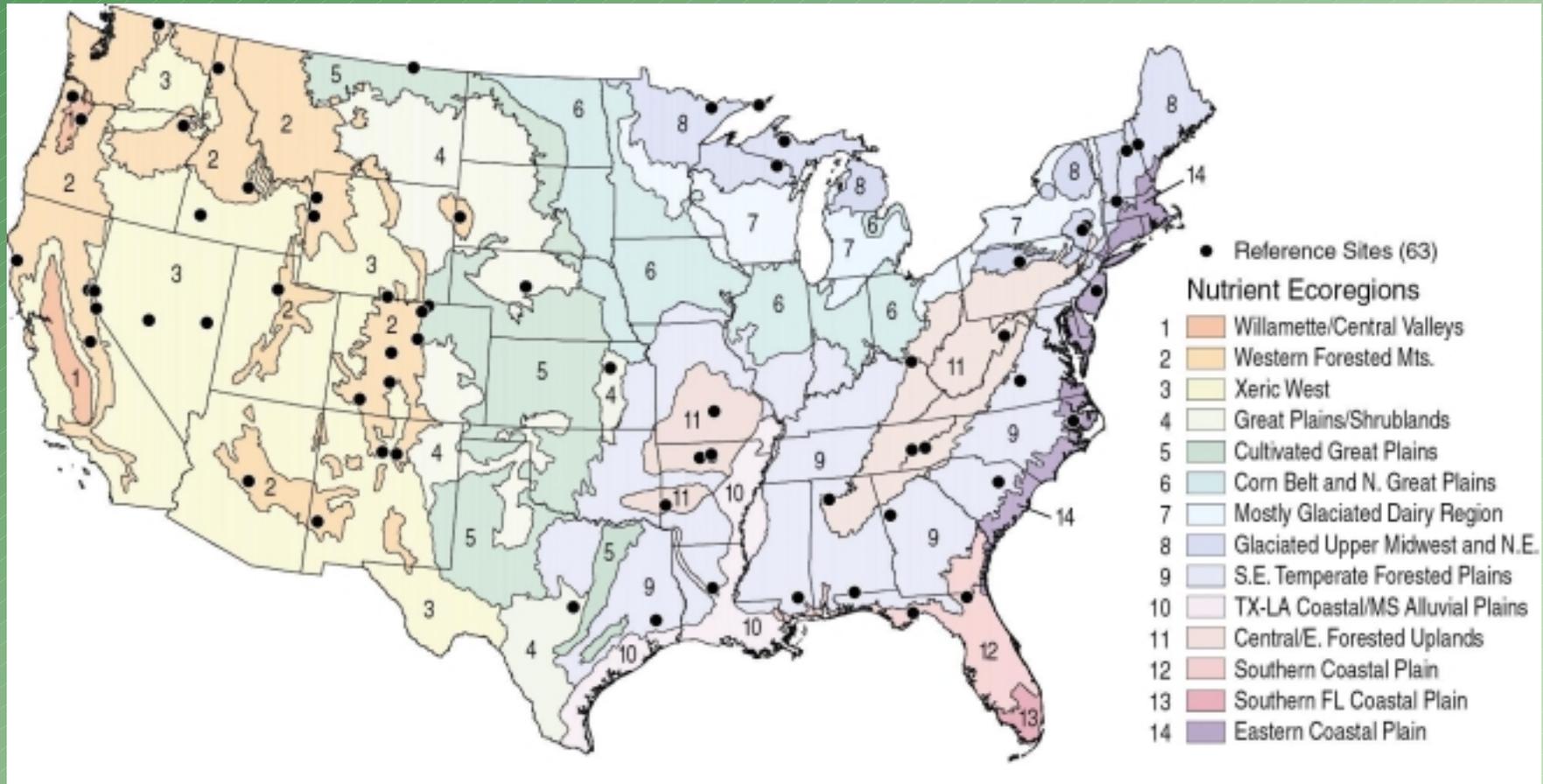
# **Objective: Develop models to correct for limitations of data from reference sites**

1. Few sites; none in some ecoregions
2. Effect of atmospheric deposition
3. Effect of natural factors, esp. runoff
4. Effect of stream size

# Approach

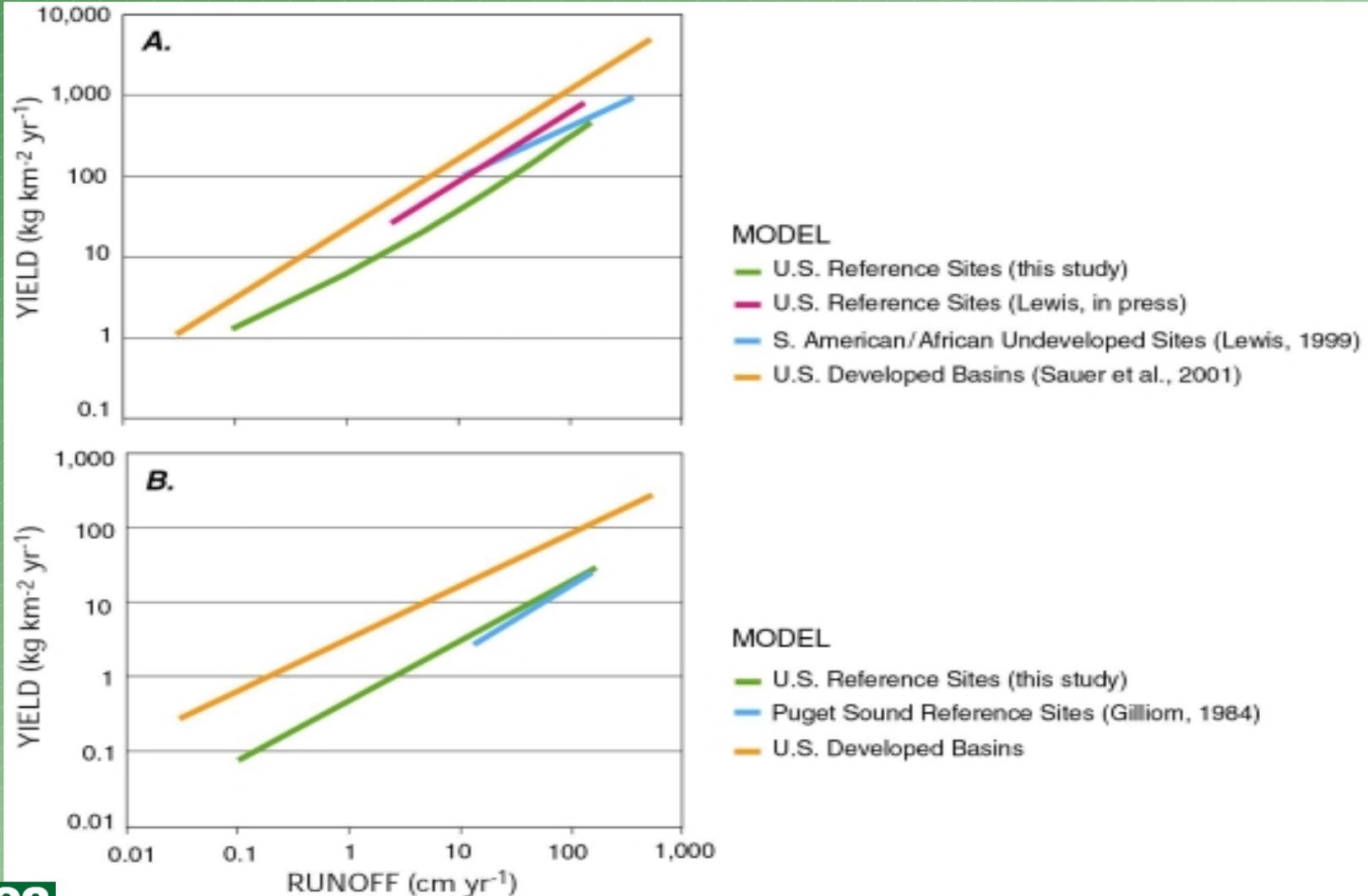
1. Calibrate regression models of background TN and TP yield from headwater stream reference sites as functions of runoff, basin size, atmospheric TN deposition, and regional factors.

# US EPA Nutrient Ecoregions & USGS Reference Sites



# Comparison with Other Models

(A. = TN; B. = TP)



# Approach (cont.)

2. Use the atmospheric deposition term in the reference site regression model to correct for this source of TN.
3. Use the regression models to estimate background nutrient loadings to larger streams and rivers (defined as RF1 reaches).

# Approach (cont.)

3. Use previously calibrated SPARROW models to predict the effects of transport in larger streams and rivers on background nutrient concentrations.

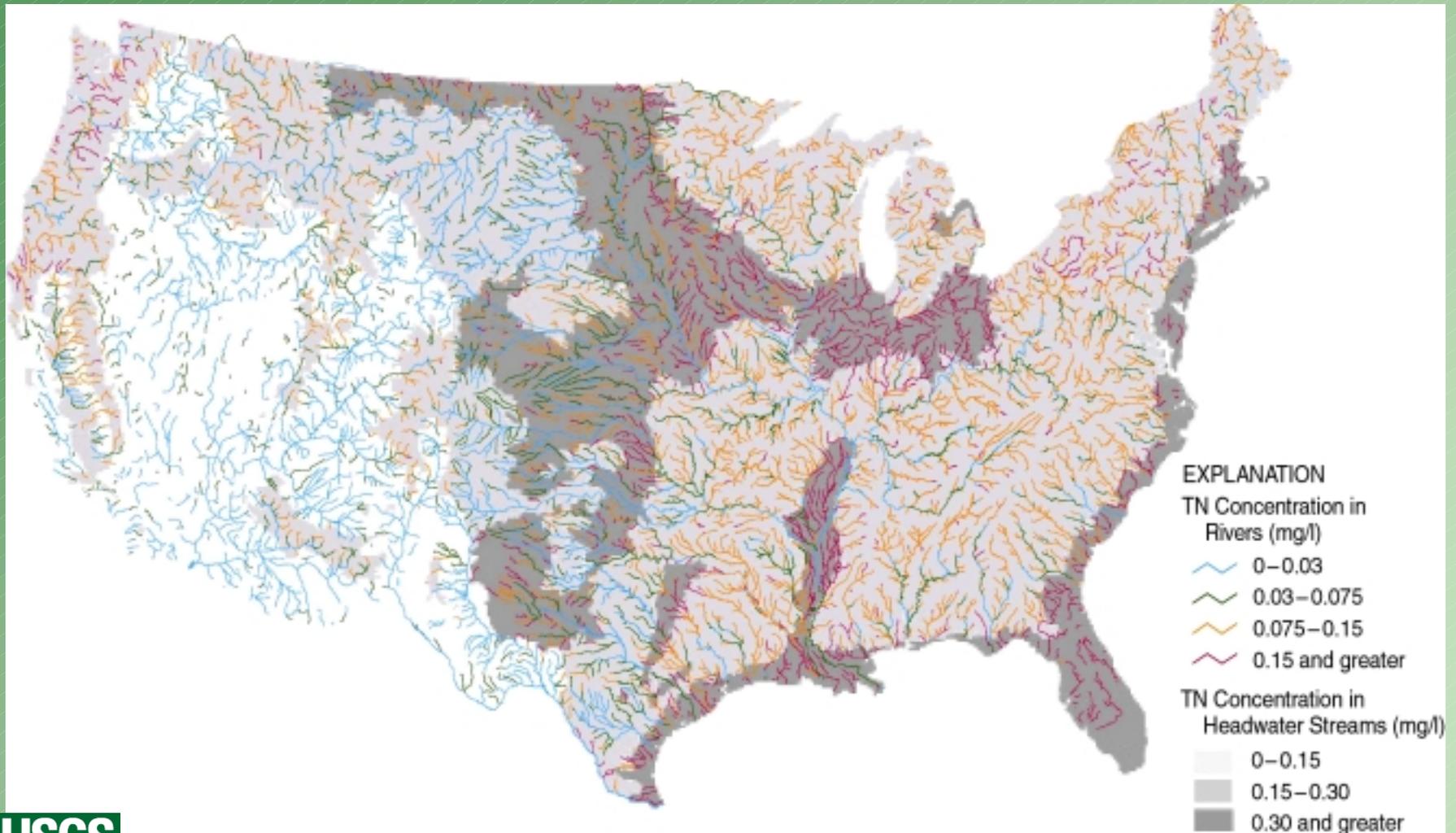
# SPARROW Transport Equation

$$L_i = \sum_{j \in J(i)} Y_j A_j [\exp(-\mathbf{k}' \mathbf{T}_{i,j})]$$

## Approach (cont.)

4. Also, use the reservoir sedimentation term in the SPARROW transport model to “correct” for the effect of dams on total P concentrations.

# Estimated Background TN Concentrations in RF1 Streams and Rivers



# Estimated Background TP Concentrations in RF1 Streams and Rivers

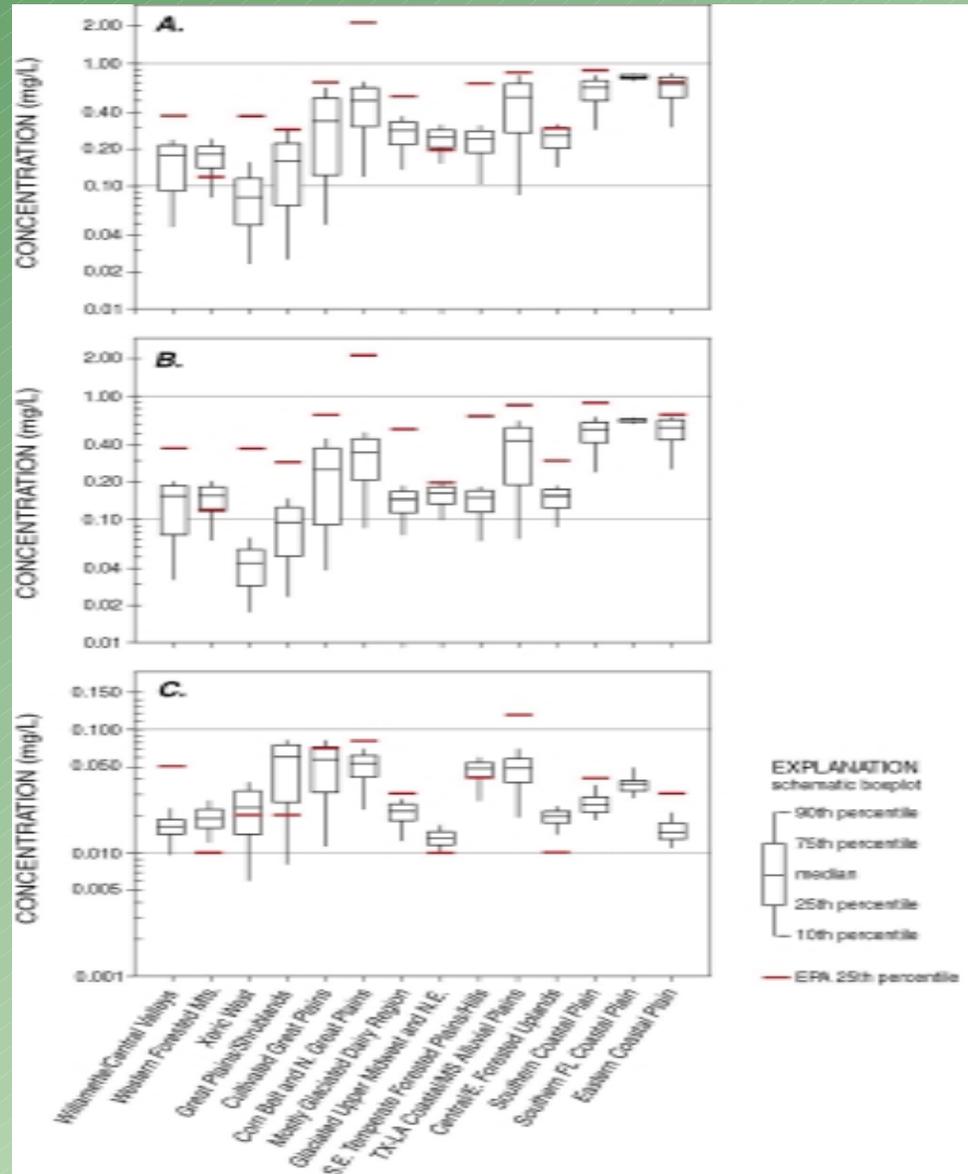


# Background Nutrient Concentrations in RF1 Streams and Rivers

TN Concentration

Deposition-adjusted TN  
Concentration

TP Concentration



# Conclusions

- Actual (i.e. current) TN concentrations (Dodds *et al*, 1998) exceed background levels by a much larger factor than do actual TP concentrations.
- Reasons: nutrient loadings, pollution controls, dams and reservoirs.

# Conclusions (cont.)

- As much as a 10X variation in natural background concentrations of TN and TP within EPA nutrient ecoregions.
- Predicted background TP concentrations exceed EPA 25<sup>th</sup> percentile values in many streams (52% nationwide).

# Conclusions (cont.)

- Fundamental problem for setting nutrient criteria: large local variation in background concentrations due to runoff and stream-river junctions.
- Localized variation hinders solving this problem through sub-division of major eco-regions.

# SPARROW Management Applications

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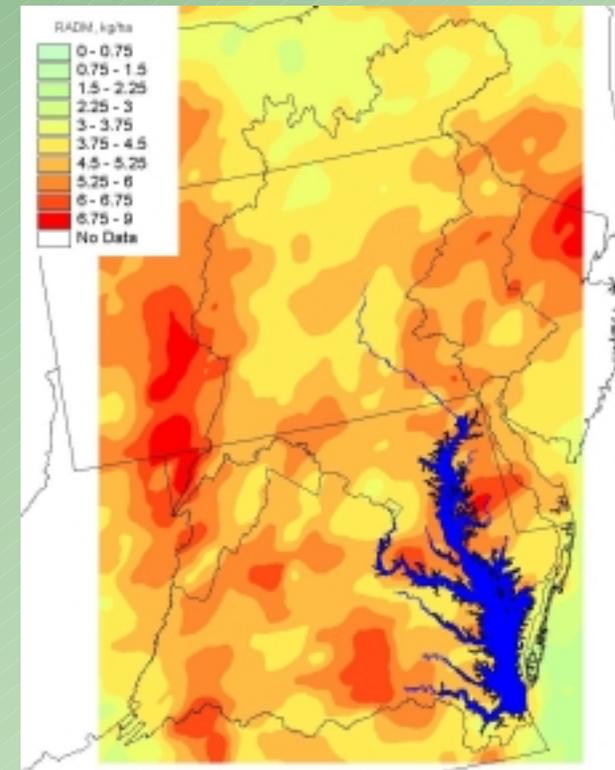
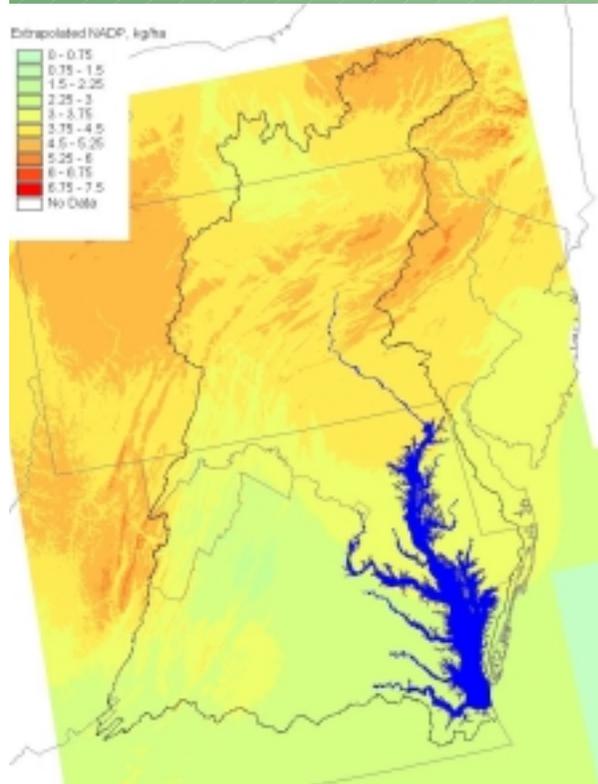
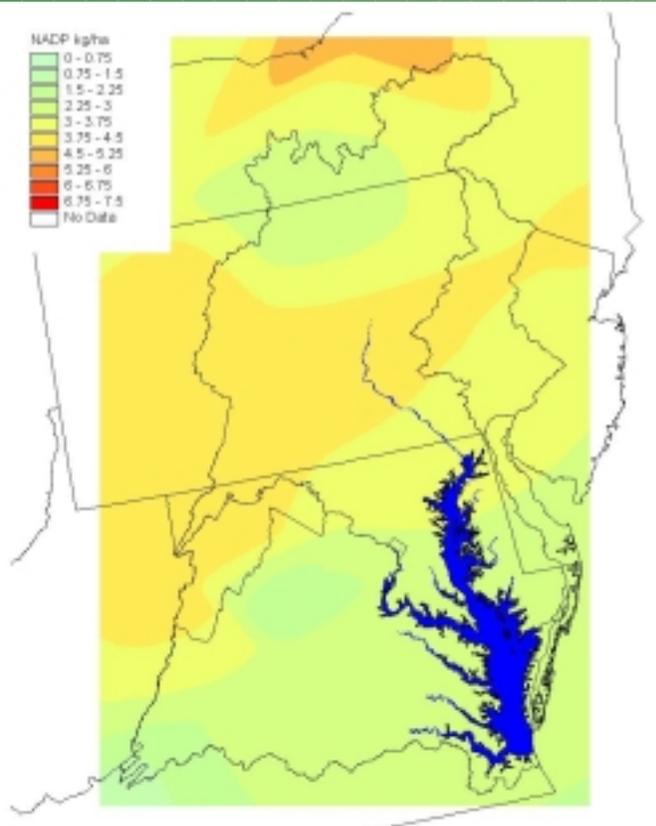
- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking Water Quality
- Network design

# Nitrate Wet-Deposition Data Sets Chesapeake Bay Region

Interpolated  
NADP  
Data

Penn State  
Modeled  
NADP Data

RADM  
Model



# CB Total Nitrogen SPARROW (1992) Five Models Evaluated

---

## Sources:

Atmospheric deposition:

NADP wet nitrate

Penn St. wet nitrate

RADM (wet, dry, total)

Municipal / industrial point

Septic systems

Urban runoff

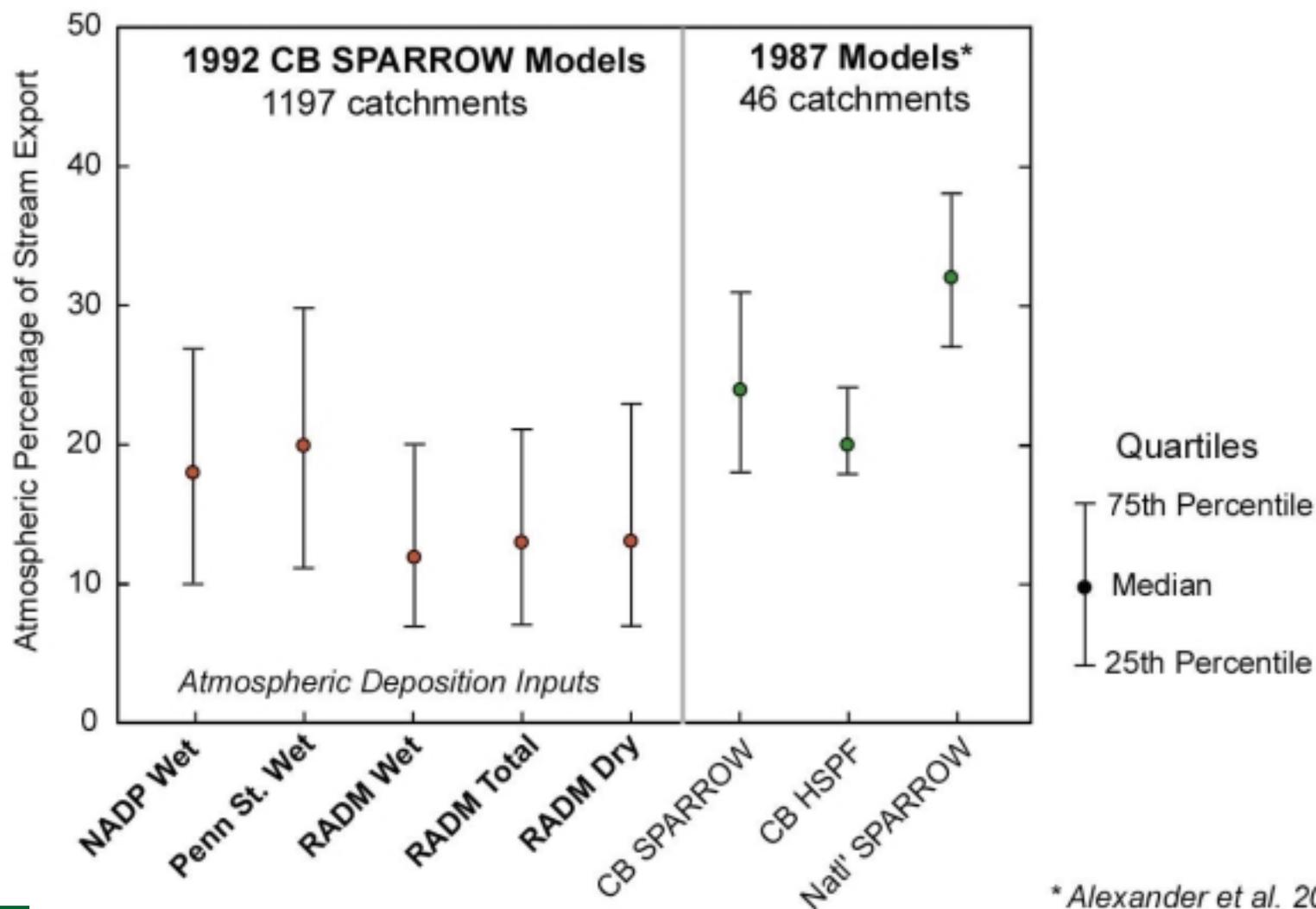
Fertilizer

Livestock waste

## Results:

- Model fits similar ( $R^2=0.98$ ); statistically inseparable
- Source contributions to stream TN flux similar
  - Modest differences in atmospheric & fertilizer sources

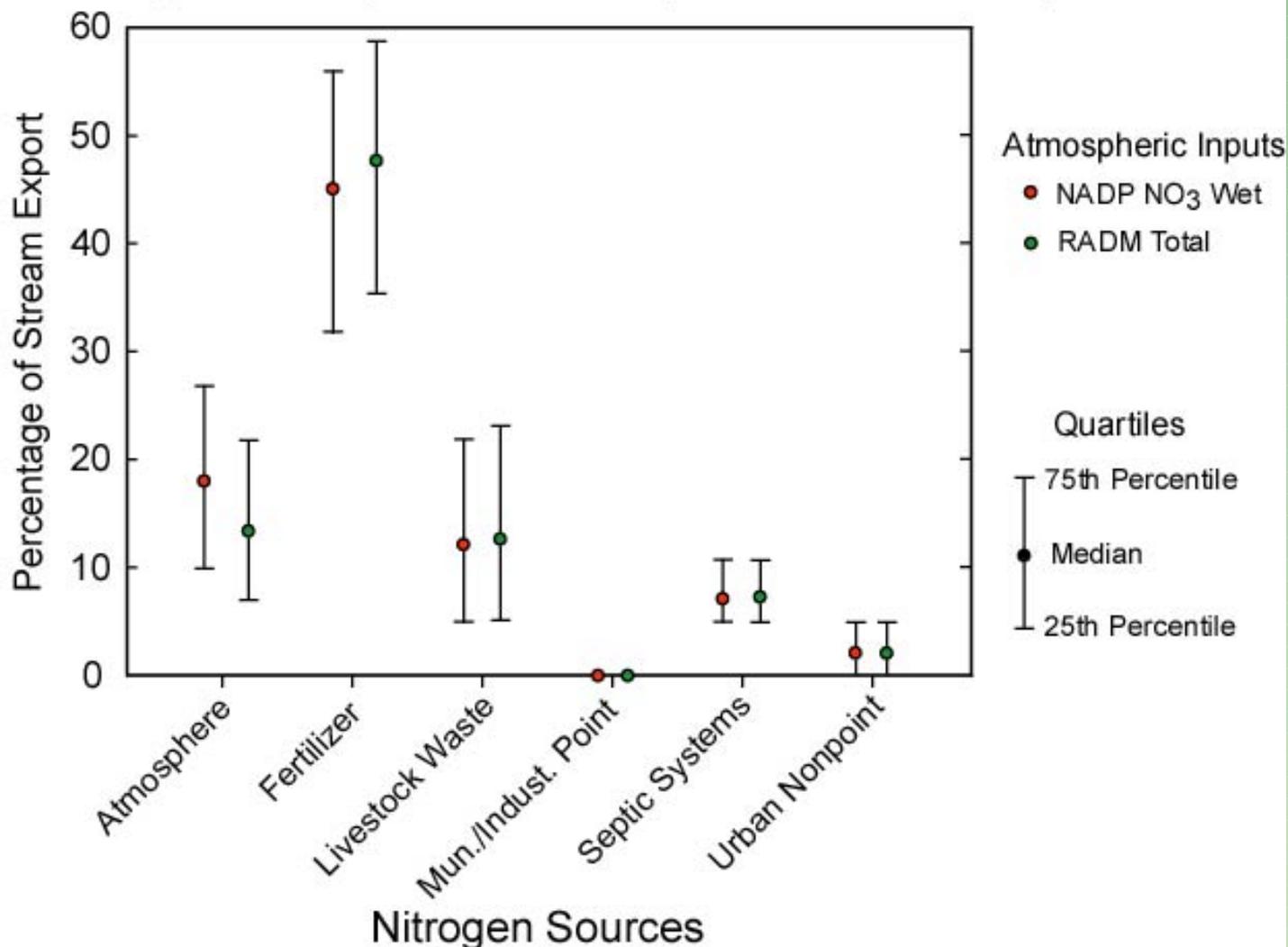
# Chesapeake Bay Watershed Atmospheric Contributions to Stream TN Export



\* Alexander et al. 2001

# CB SPARROW 1992 Estimates of Source Contributions to Stream TN Export

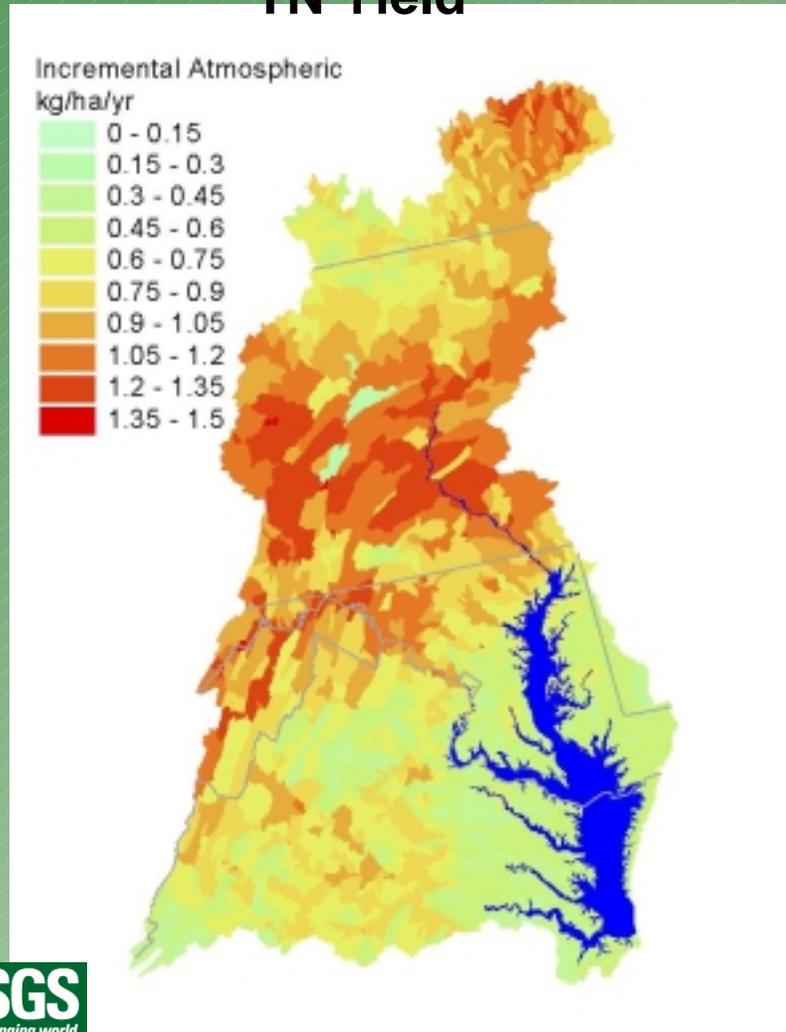
Chesapeake Bay Watershed (1197 catchments)



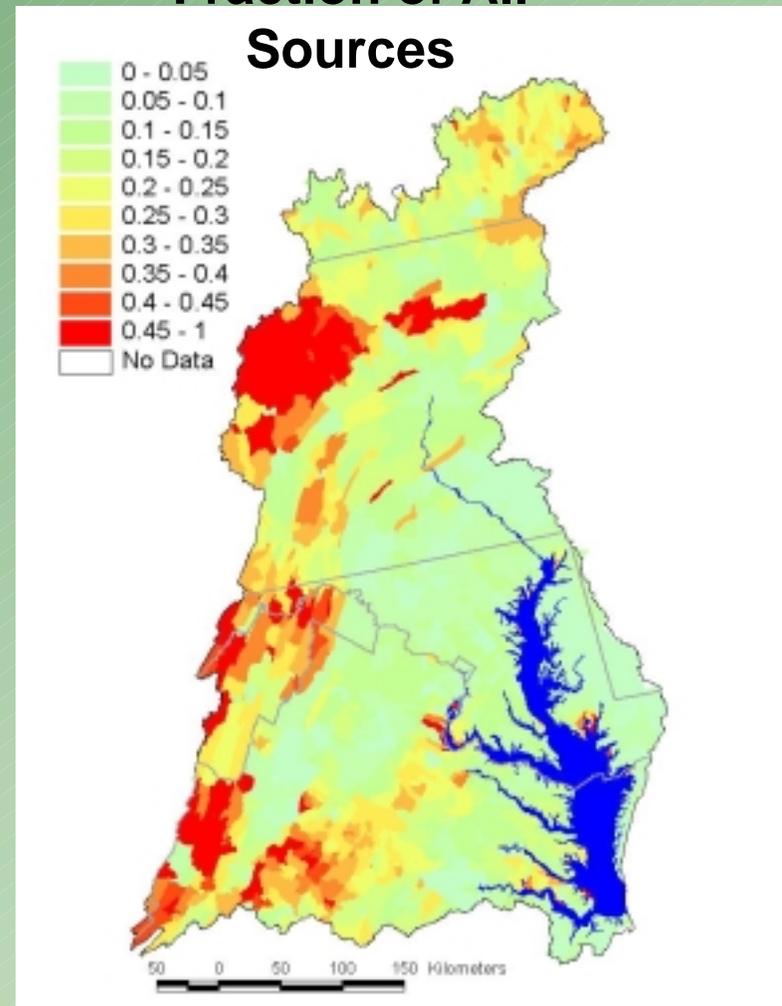
# CB SPARROW Atmospheric Contributions Exported from Reach Catchments

(Based on Interpolated NADP Wet  $\text{NO}_3$  Deposition)

## TN Yield



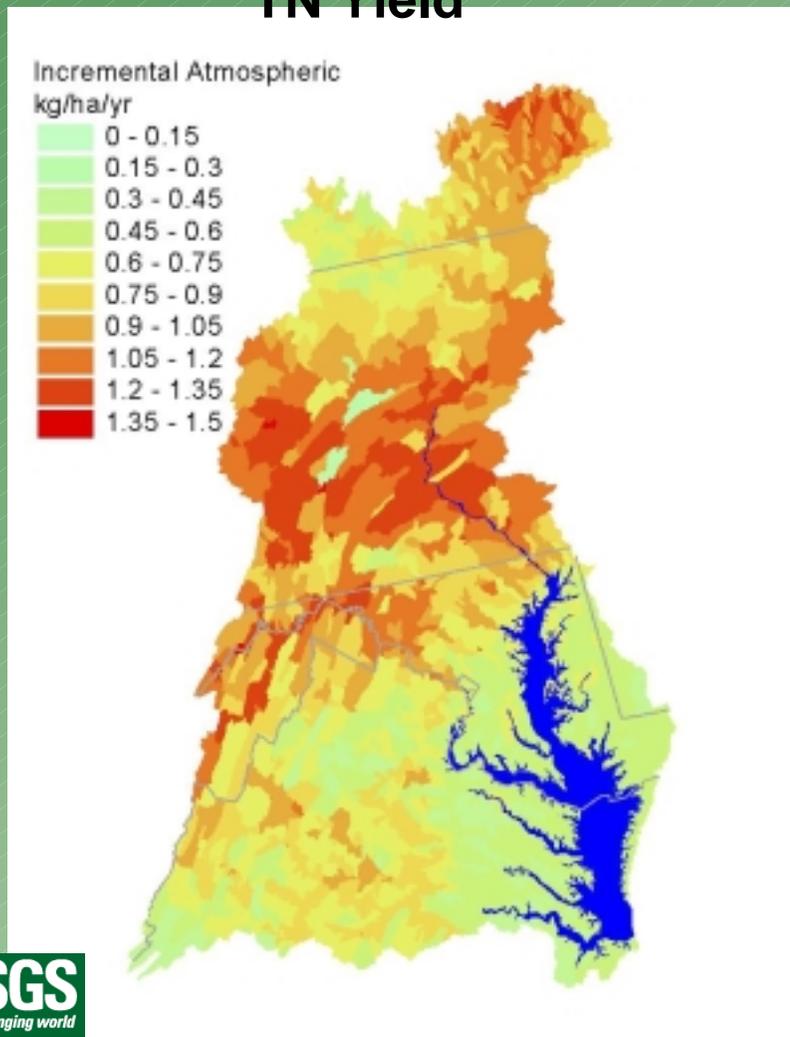
## Fraction of All Sources



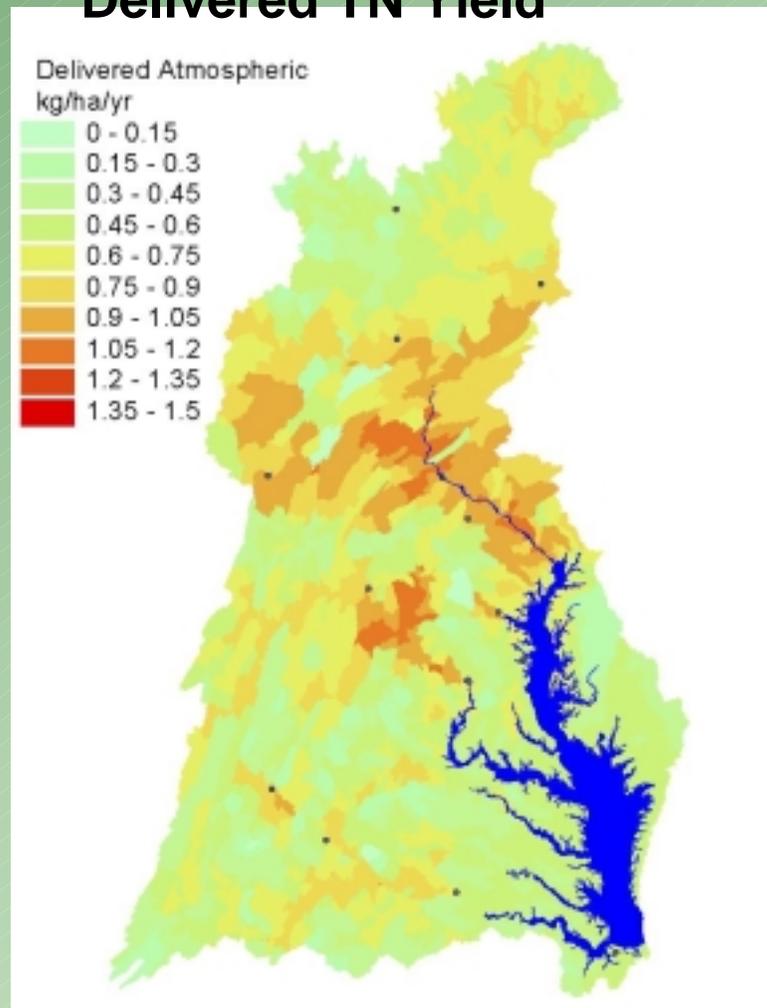
# CB SPARROW Atmospheric Contributions Exported from Catchments & Delivered to Bay

(Based on Interpolated NADP Wet  $\text{NO}_3$  Deposition)

## TN Yield



## Delivered TN Yield



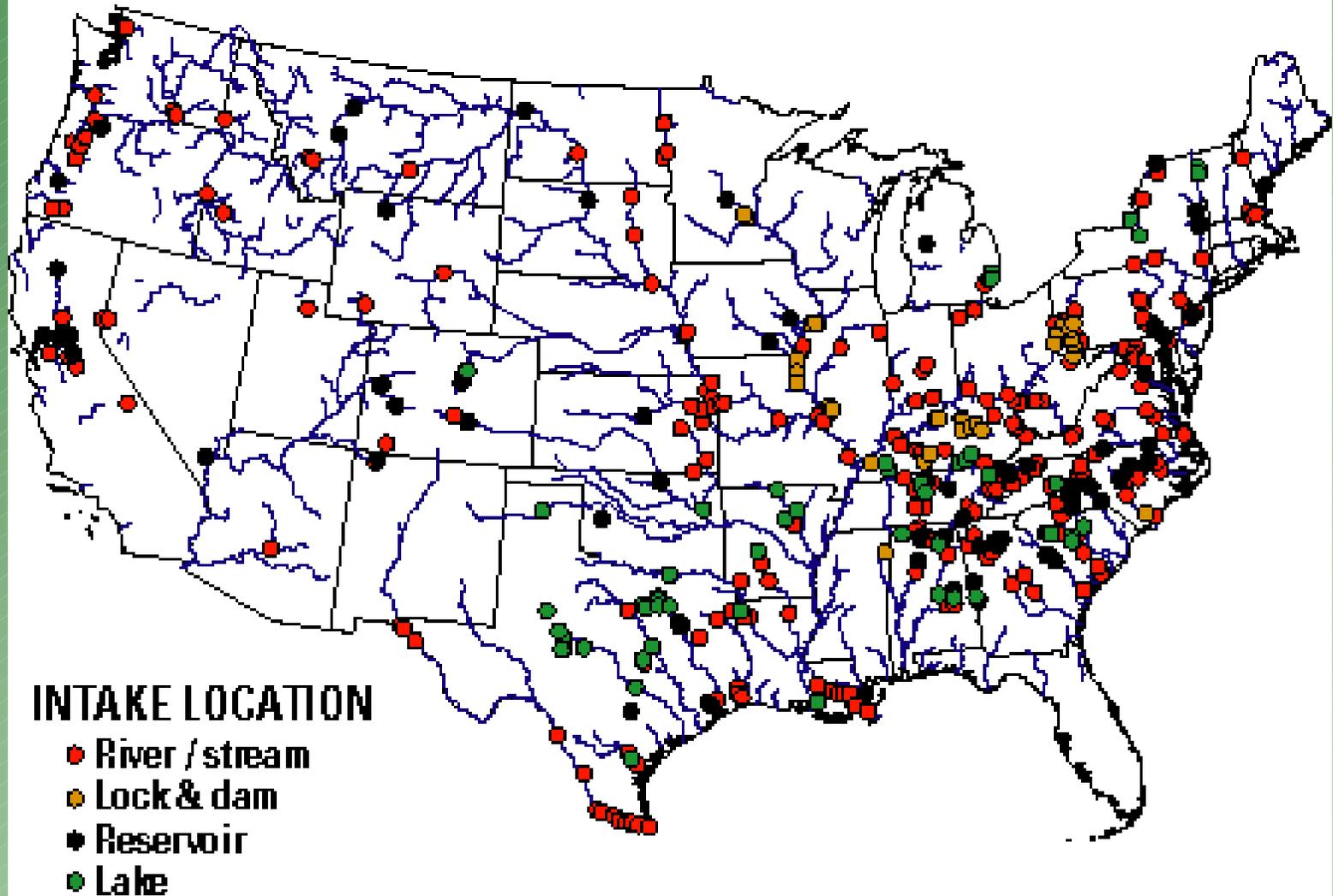
# SPARROW Management Applications

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- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking Water Quality
- Network design

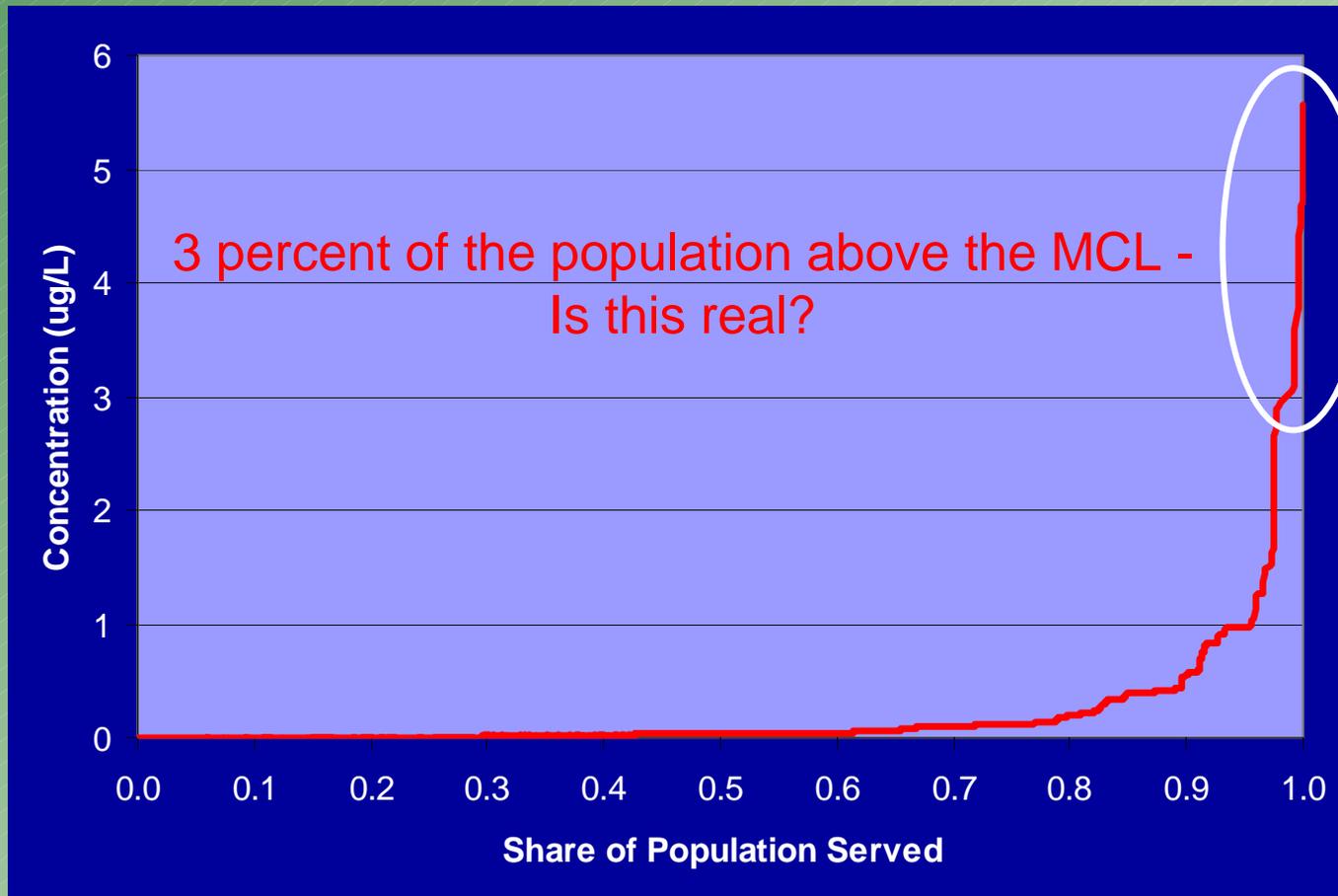
# SURFACE-WATER INTAKES IN THE UNITED STATES

Serving Populations above 10,000 in Watersheds Greater than 1,000 Sq. Km.



# Cumulative Population with Atrazine Exposure Below Given Concentration

(567 intakes serving 60 million people)



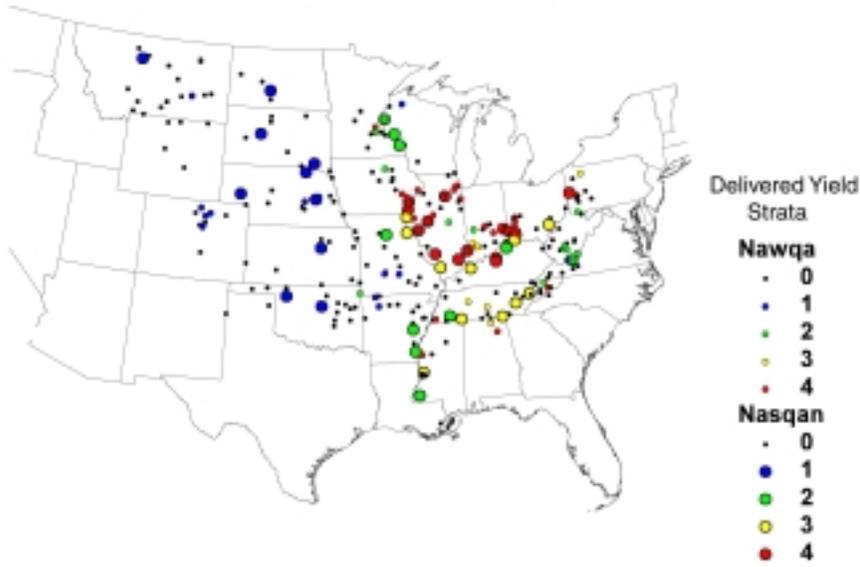
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# Network design

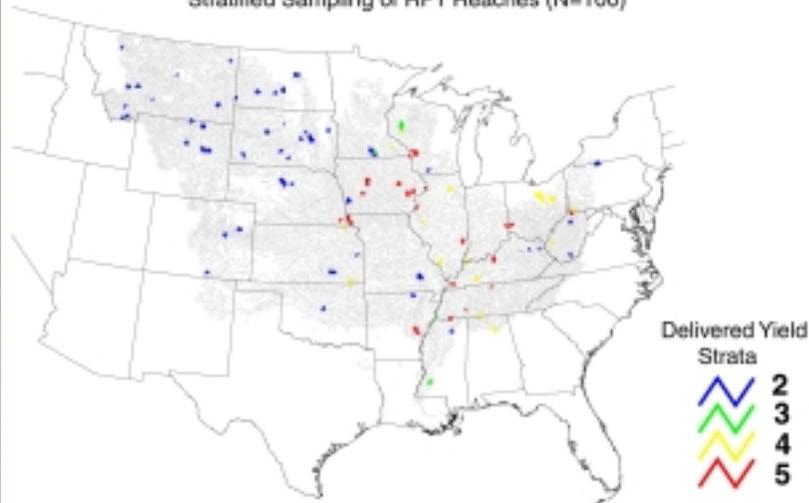
## Optimal network design to predict TN yield to Gulf of Mexico

# Network Design Using SPARROW

Stratified Sampling of Monitoring Sites (N=100)



Stratified Sampling of RF1 Reaches (N=100)



Objective: Select the “optimal” set of monitoring locations that improves the precision of model estimates of the “delivered TN yield” to the Gulf of Mexico

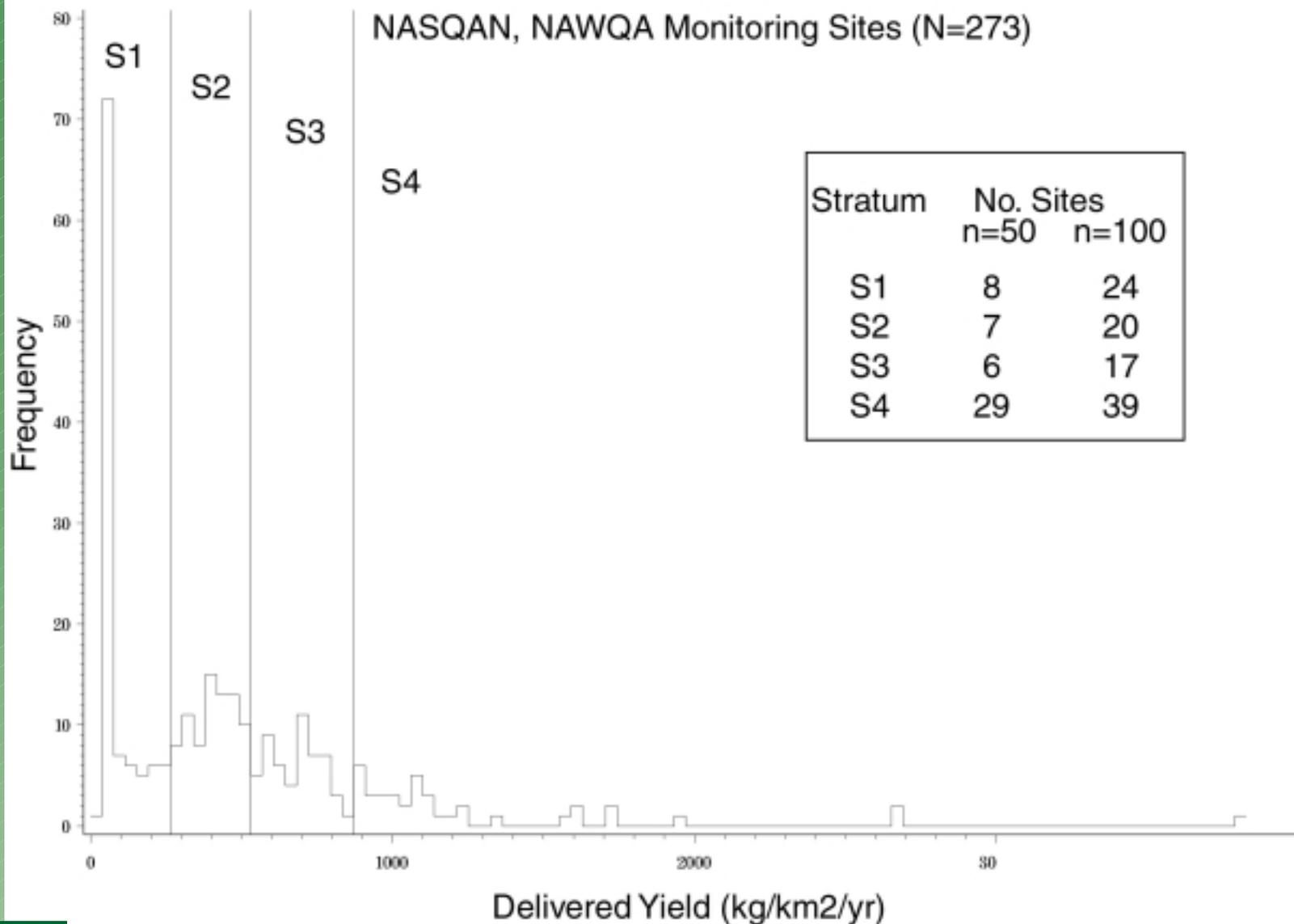
Method: (a) stratify the distribution of delivered yield for sites (273 NASQAN & NAWQA) and reaches; (b) determine the sample size from each strata that satisfies the objective; (c) randomly select 100 locations from the four strata

Additional design scenarios possible:  
(a) alternate populations of streams having different attributes; (b) effect of station sample size; (c) different objective functions (e.g., concentration)

# Frequency Distribution and Stratum Delineatio

{Stratifiying variable is delivlyld, groups: Group = A

## NASQAN, NAWQA Monitoring Sites (N=273)

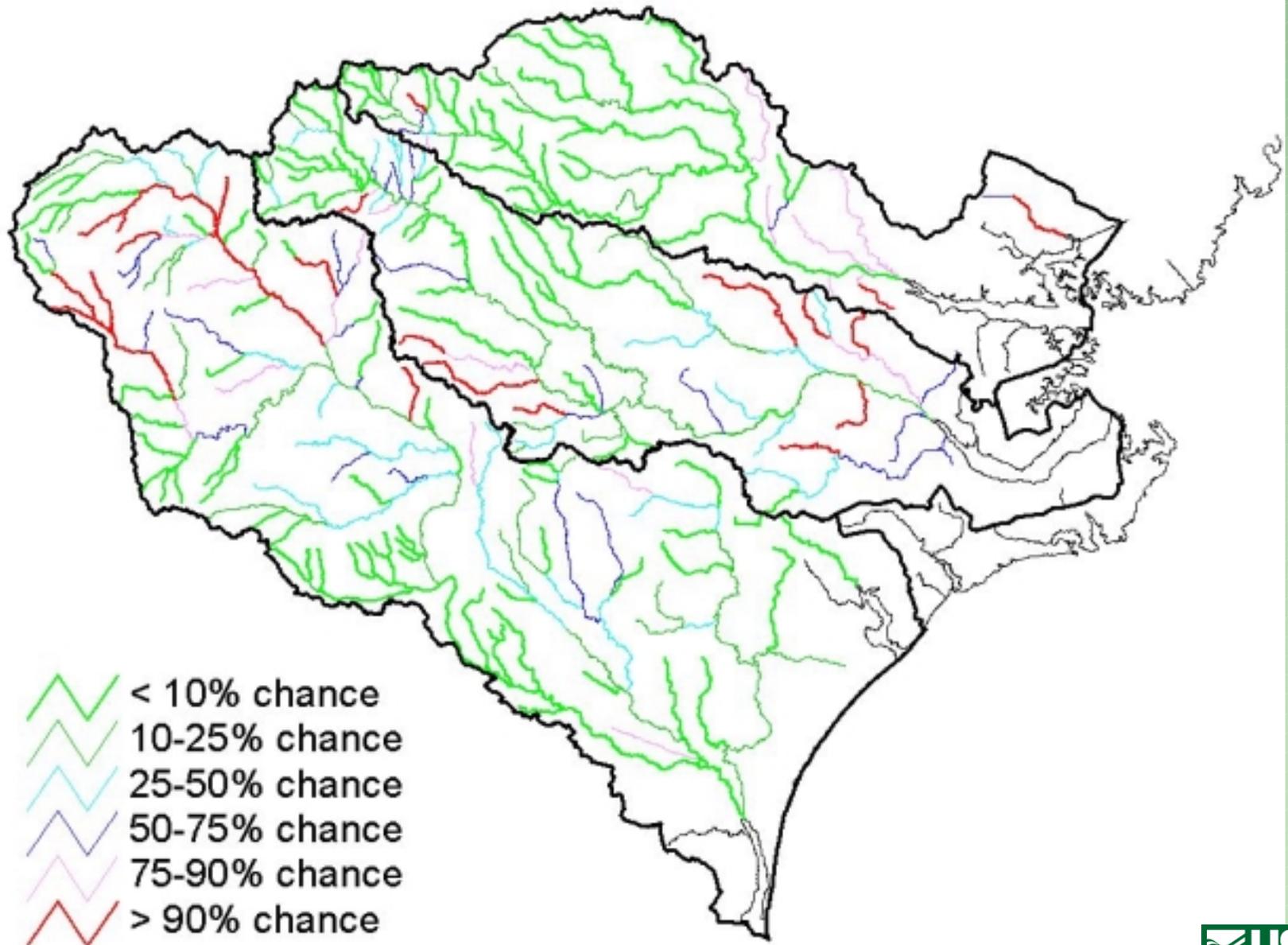


Stratum	No. Sites	
	n=50	n=100
S1	8	24
S2	7	20
S3	6	17
S4	29	39

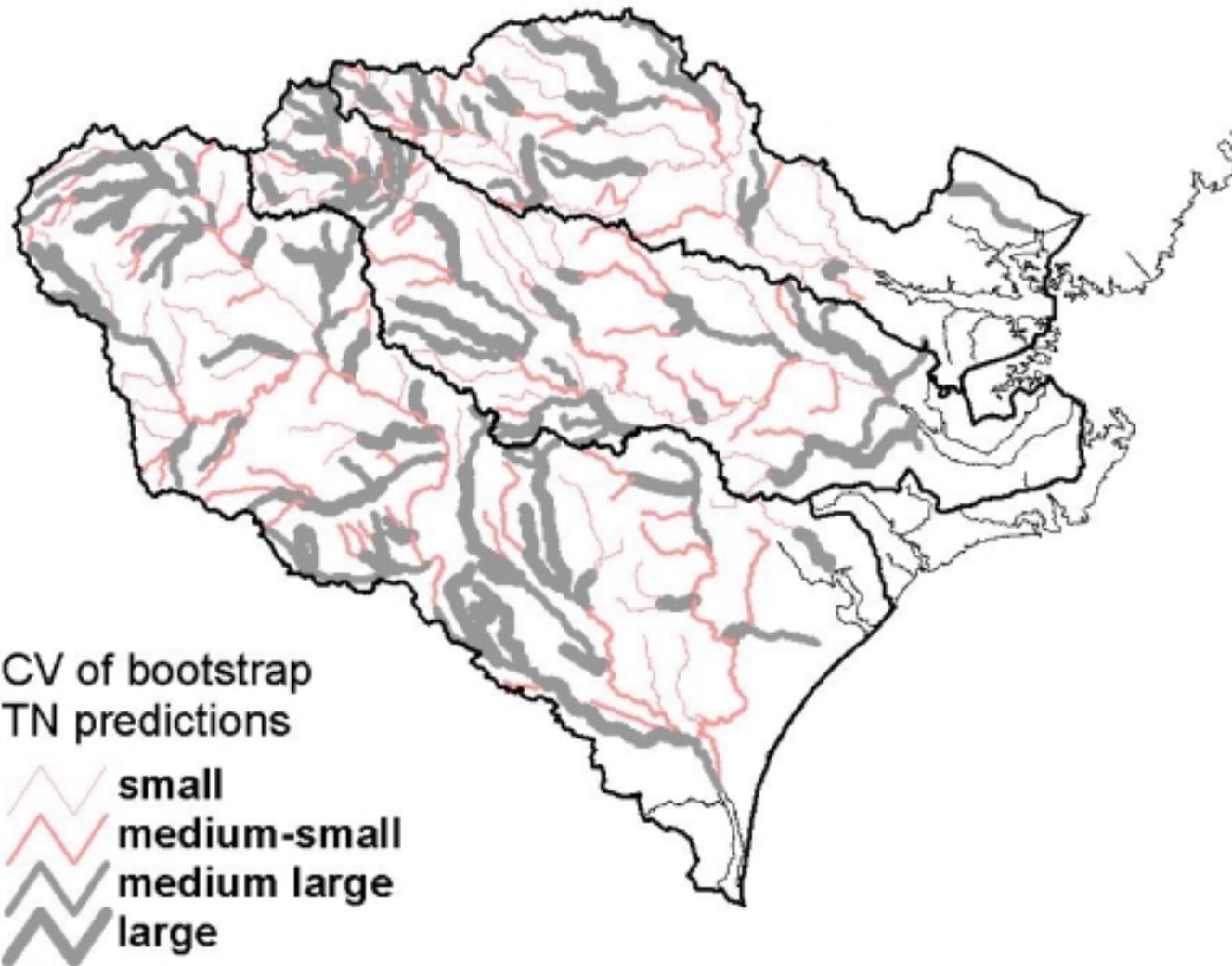
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Network design  
Using exceedence probability and  
prediction uncertainty to locate  
additional monitoring sites

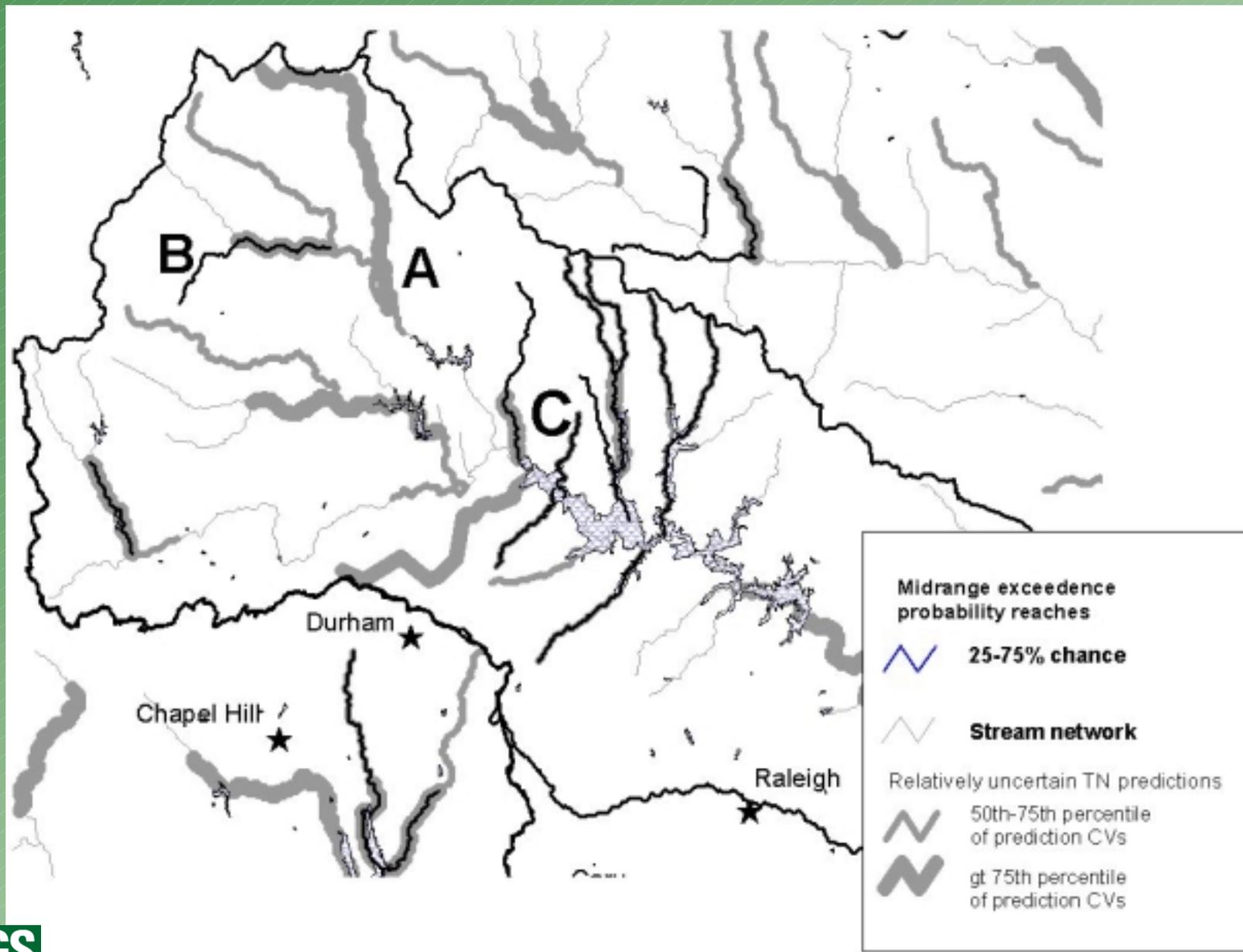
# Probability of exceeding TN concentration of 1.5 mg/L



# Relative variability of TN predictions



# Identifying locations for further monitoring?



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Network design  
Chesapeake Bay  
Non-Tidal Monitoring Network Design

# *Key Aspects of the Non-Tidal Monitoring Program*

- \* Non-Tidal Monitoring Funded Primarily by the States for Other Objectives
- \* Objectives of Non-tidal Monitoring for CBP  
Focus on How Watershed Activities Affect the Bay
- \* States Have Agreed to Work With the CBP to Make Modest Changes to Achieve All Objectives

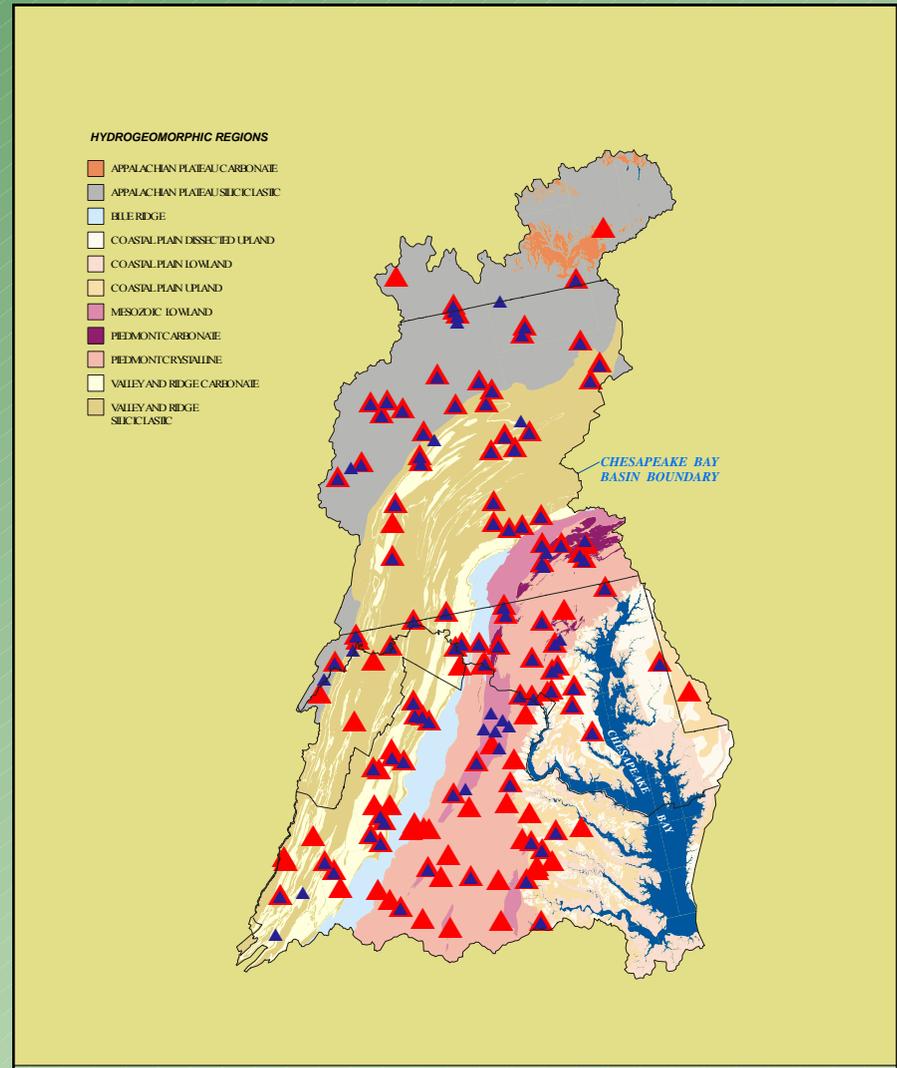
# Chesapeake Bay SPARROW

Version II

HGMR / Load Site  
Distribution

▲ Version I - 1987

▲ Version II - 1992



# *Criteria for Non-Tidal Site Inclusion*

## A. Load Estimation

- Must be associated with a stream gage
- Sites must represent broad range of watershed characteristics
- Minimum of 12 samples per year over 3 consecutive years

## B. Temporal Trend Analysis

- Must be associated with a stream gage
- Sites must represent broad range of watershed characteristics
- Minimum of 4 samples per year over 10 consecutive years

## C. HSPF Watershed Modeling

- Must be associated with a stream gage
- Sites must represent broad range of watershed characteristics
- Minimum record length of 5 consecutive years
- Sites must be located near segment boundary

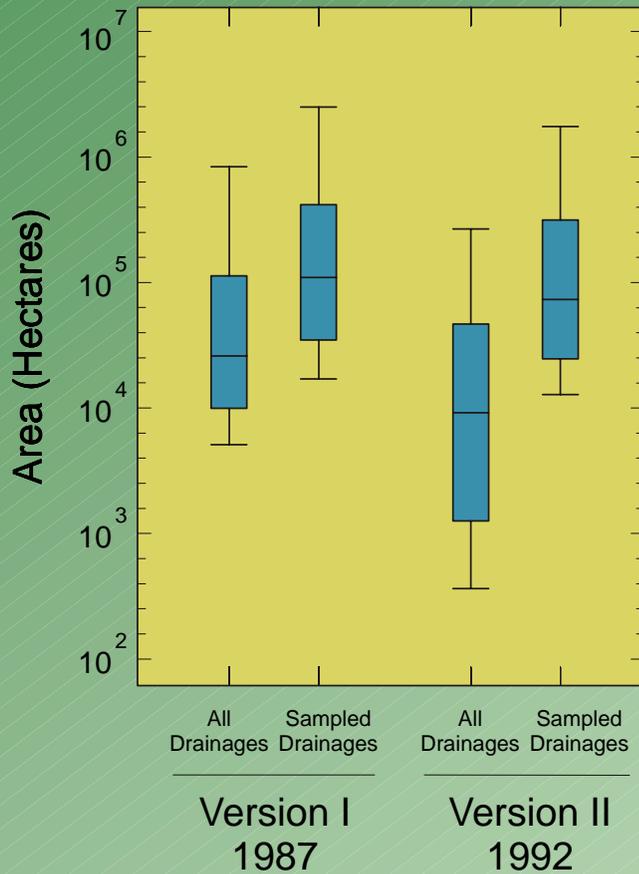
# *Preliminary Results of Criteria Application*

## Langland and others, WRIR 95-4233

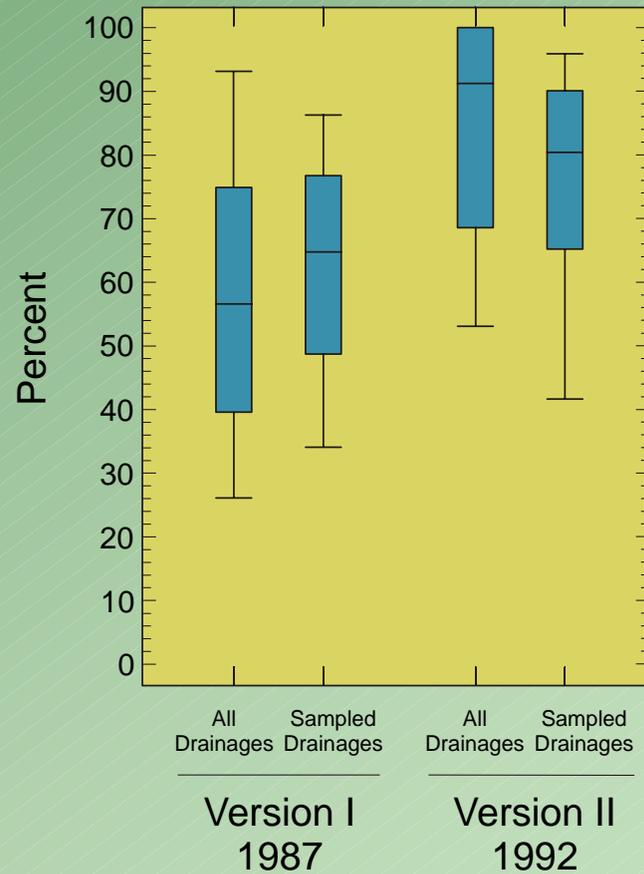
- \* A Total of 1,058 Sites With at Least 12 Nutrient or Sediment Samples Collected Over 3 Years or More
- \* Of the 1,058 Sites, 613 had at Least 50 Nutrient or Sediment Samples Collected Over 3 Years or More
- \* Of the 613 Sites, Only 127 Were Associated With a Flow Gage

# MONITORING NETWORK REPRESENTATIVENESS

## DRAINAGE AREA

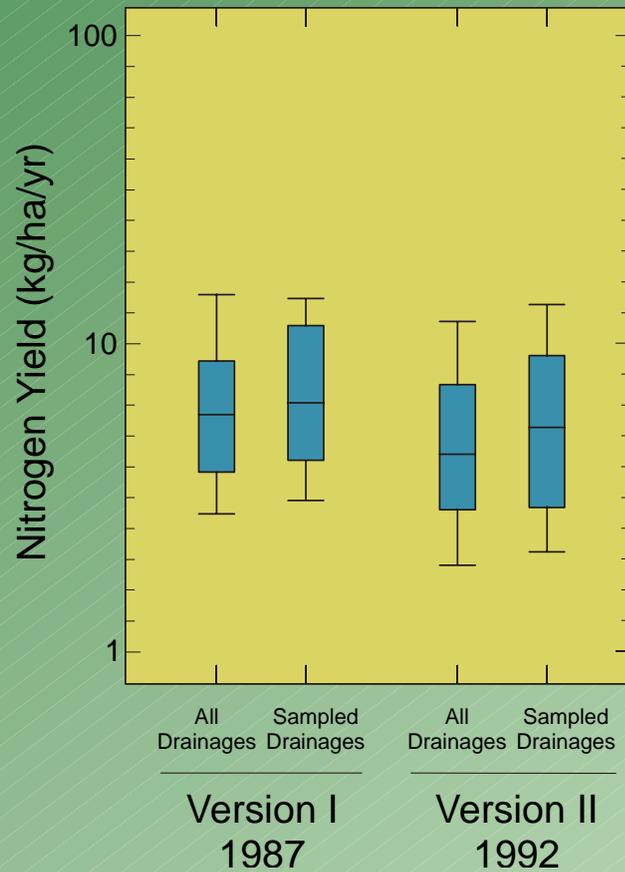


## PERCENT DELIVERY

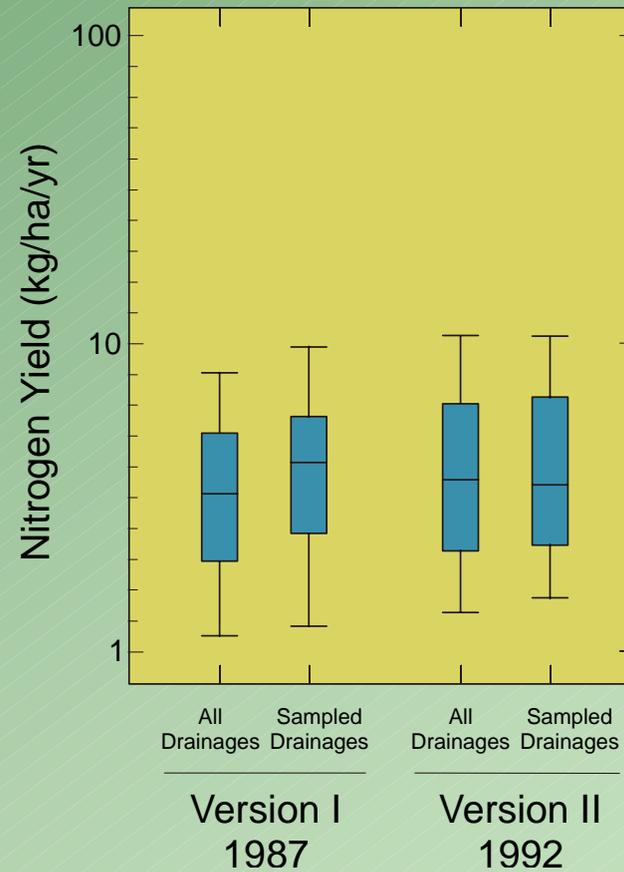


# MONITORING NETWORK REPRESENTATIVENESS

## INCREMENTAL YIELD

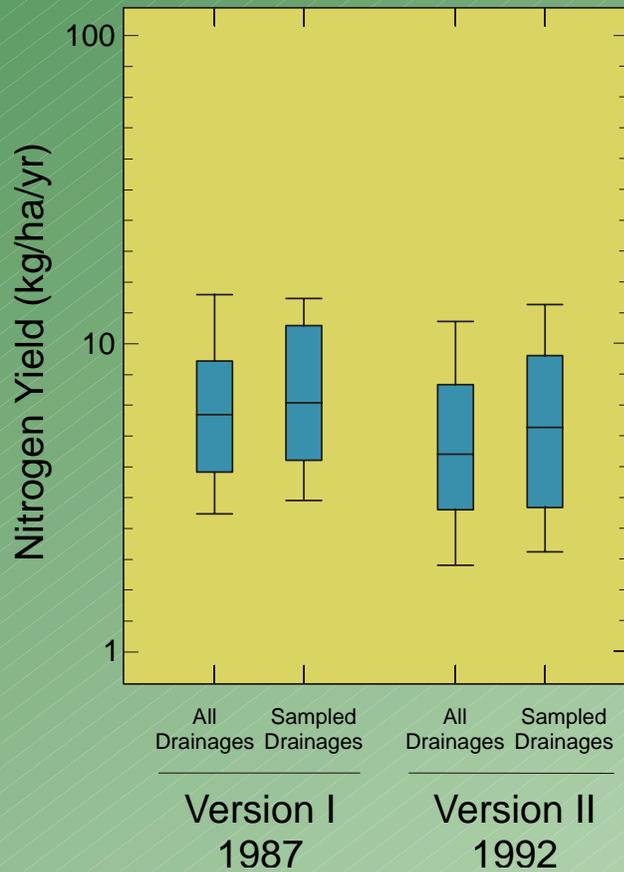


## DELIVERED YIELD

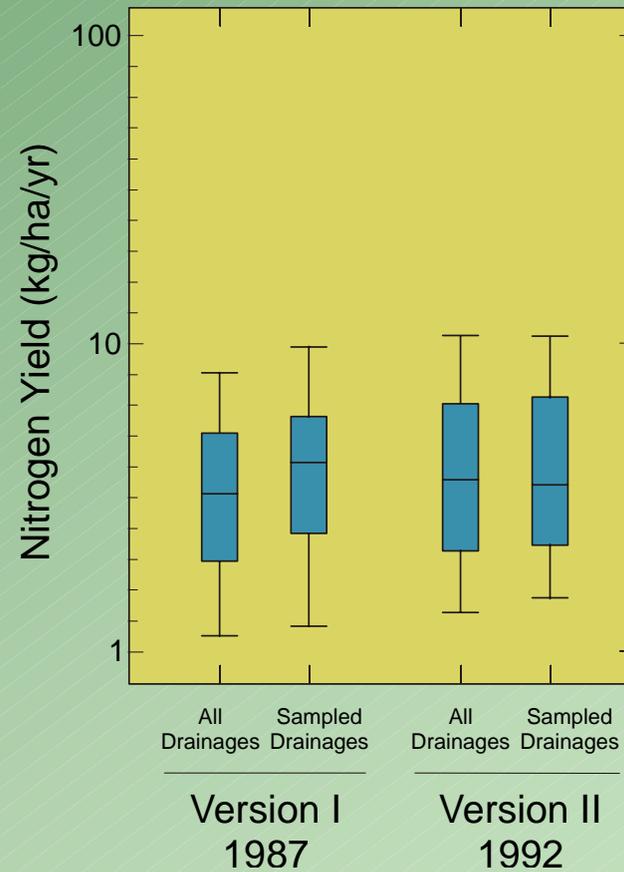


# MONITORING NETWORK REPRESENTATIVENESS

## INCREMENTAL YIELD

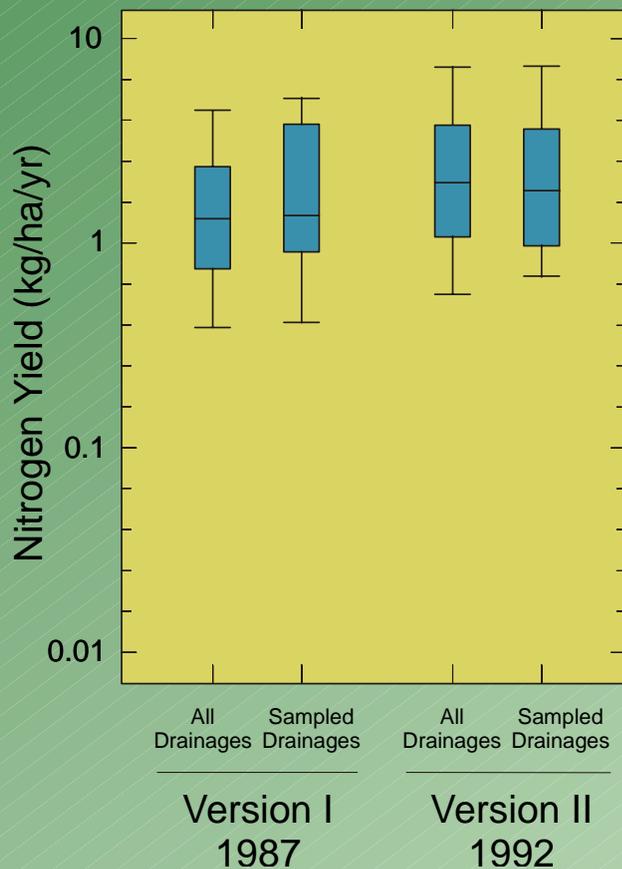


## DELIVERED YIELD

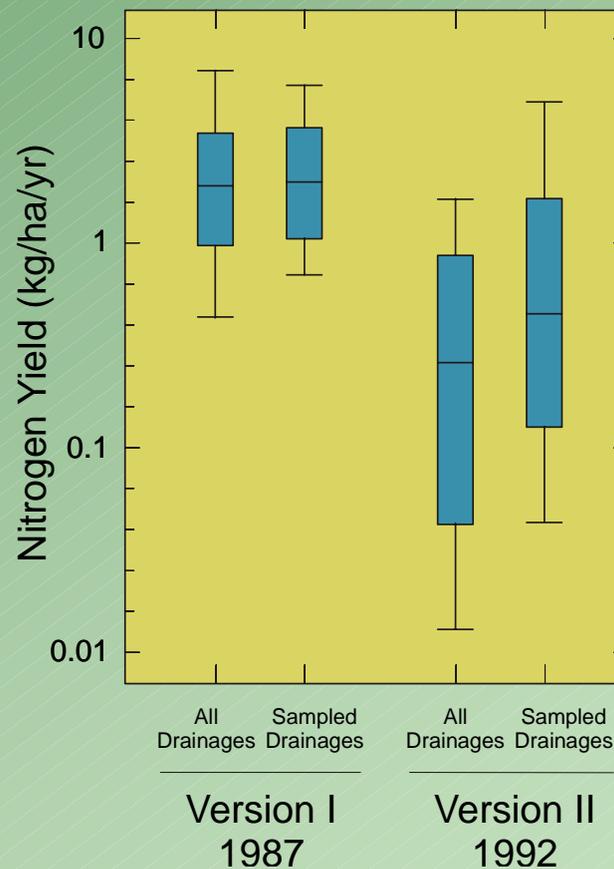


# MONITORING NETWORK REPRESENTATIVENESS

## FERTILIZER APPLICATION

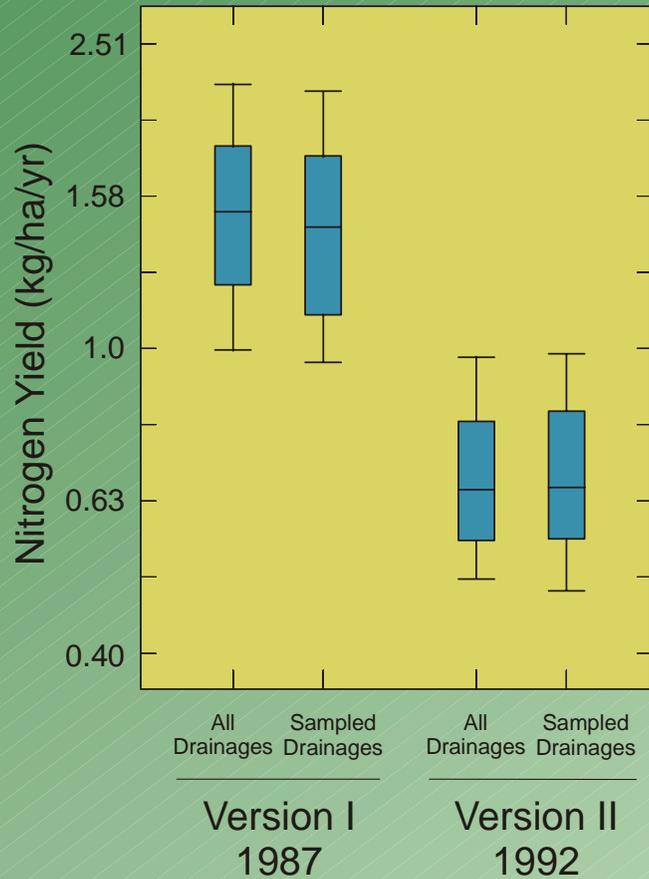


## MANURE GENERATION

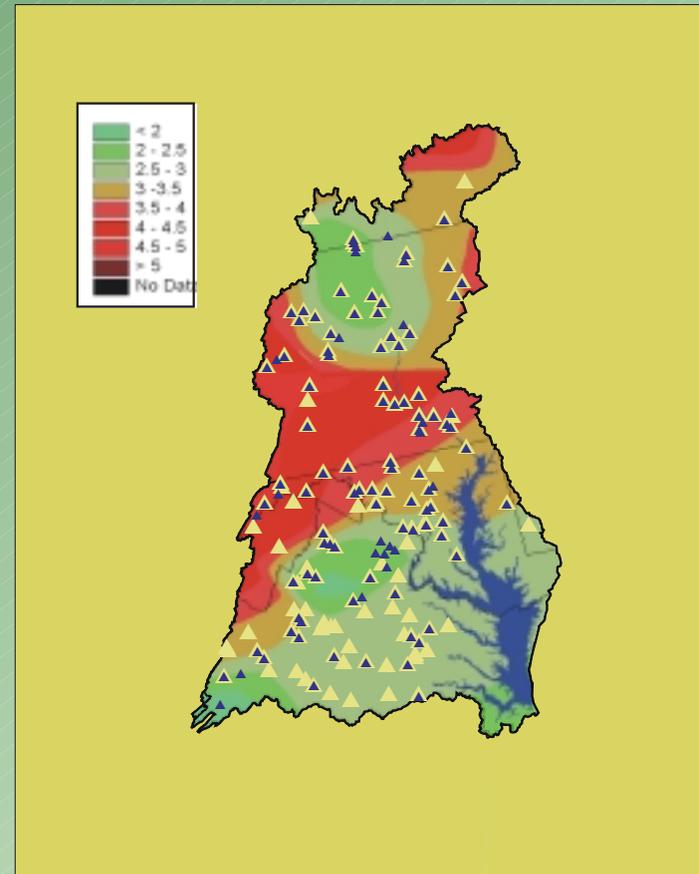


# MONITORING NETWORK REPRESENTATIVENESS

## ATMOSPHERIC DEPOSITION

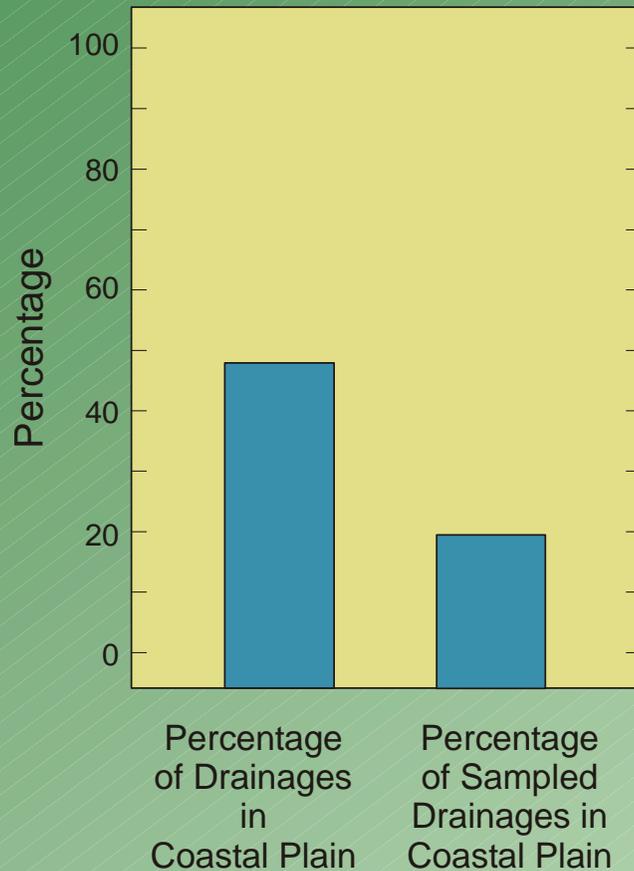


## NADP / STREAM LOAD SITES

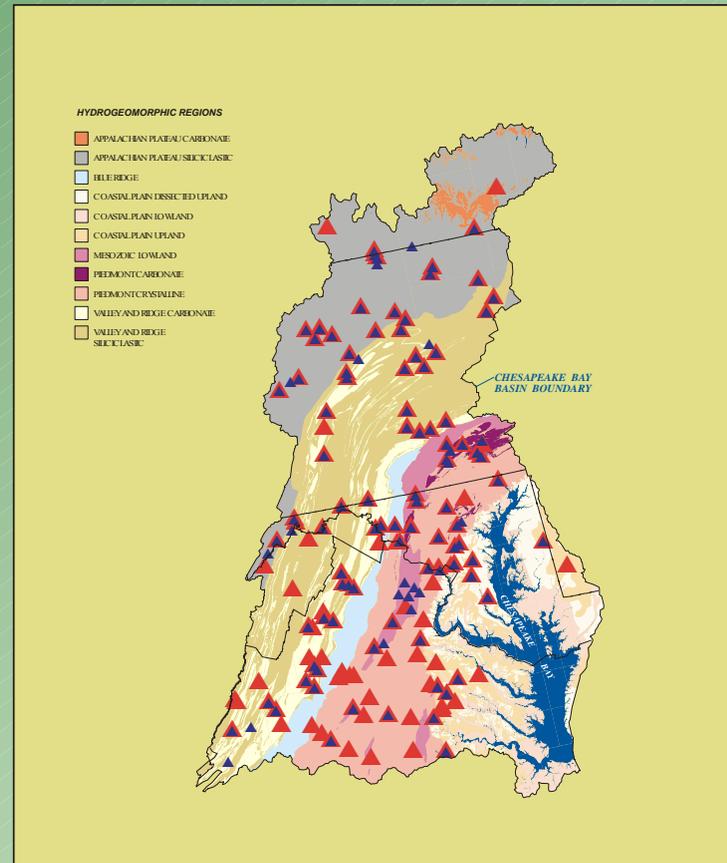


# MONITORING NETWORK REPRESENTATIVENESS

COASTAL PLAIN PERCENTAGE



HGMR / STREAM LOAD SITES



# *Preliminary Recommendations for Non-Tidal Monitoring Network*

- \* Add Sites to the Coastal Plain Part of the Watershed
- \* Add Sites at Drainage Boundaries of Management Strategy Design Units
- \* Increase the Amount of Storm Sampling

# SPARROW Management Applications

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- TMDL
- Studying change over time
- Targeting of nutrient controls
- Natural background
- Atmospheric deposition
- Drinking Water Quality
- Network design
- Marginal Effects of Changing Inputs

## *Application of SPARROW in Simulation Mode*

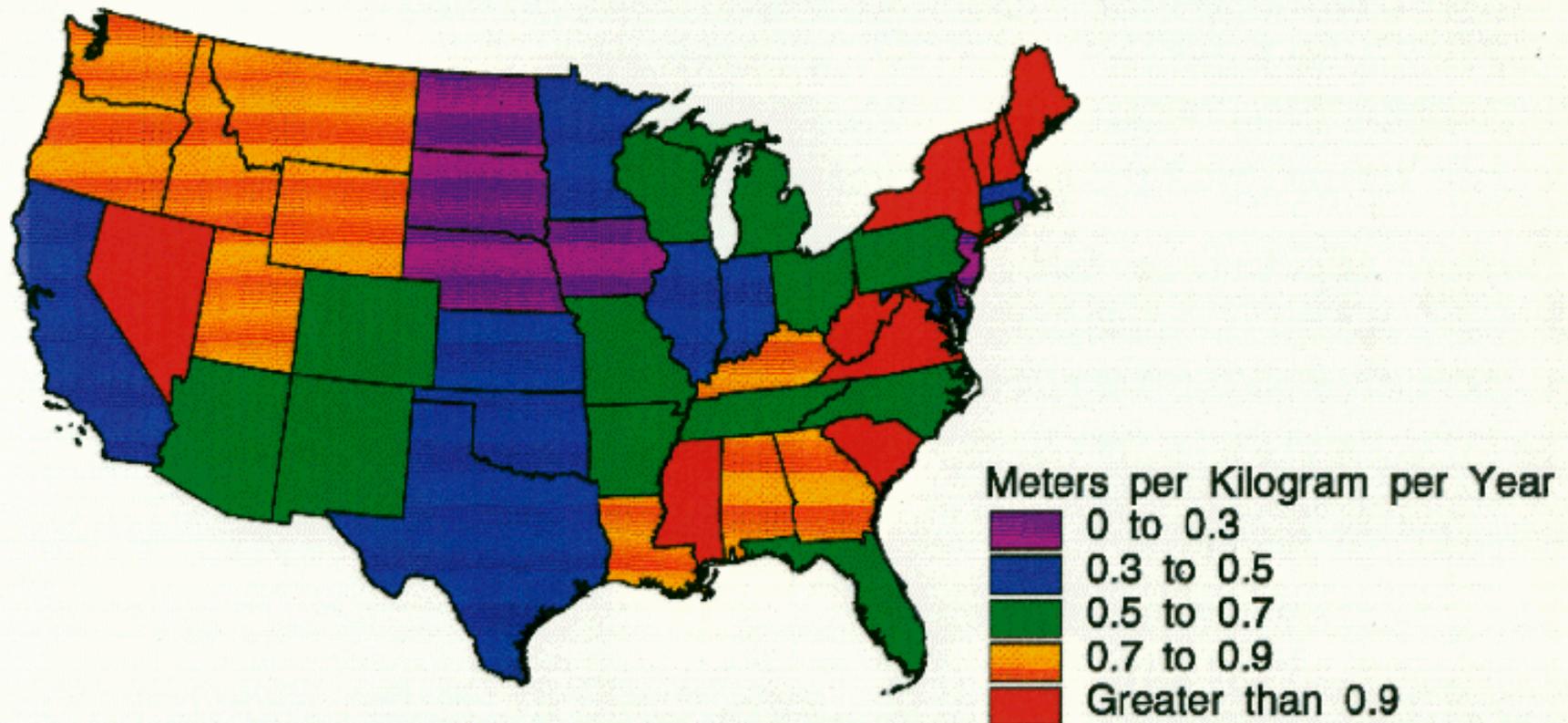
# Marginal Effects of Changing Inputs

(e.g. Meters of stream channel brought into compliance with a w.q. standard per kilogram of TP reduction)

- Run model with a small incremental reduction in loads from specified sources
- Track reaches in which concentration falls below 0.1 mg/l
- Summarize results over desired region (and map reaches that change status)
- Results not easily anticipated
- Note: results will differ with a larger reduction

# *Marginal Benefits of Phosphorus Control:*

**Meters of U.S. Streams Brought into Compliance per Kilogram per Year of Phosphorus Source Reduction by Individual States**



# SPARROW Model

## Applications: Other issues

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- Model uncertainty in predictions
- Web access to SPARROW applications

# Evaluation of Uncertainty in SPARROW

# Three Sources of Uncertainty

- Parameter uncertainty due to finite sample size
  - Goes to zero as sample size goes to infinity
- Model uncertainty due to unaccounted factors affecting water quality
  - Goes to zero only by including additional explanatory factors
- Measurement error
  - Exists in both the dependent variables and the predictors
  - Cannot be removed by introducing either more observations or more variables
  - Measurement error in predictors causes biased coefficient estimates, but not necessarily biased predictions
  - The use of estimated loads as the dependent variable creates complications in deriving prediction intervals

# Measures of Uncertainty

- Standard Error of Prediction

$$\text{StandardError } \hat{y} = \sqrt{E(y - \hat{y})^2}$$

- Confidence Intervals

$$\text{Pr}\left(\hat{\theta}_{-k} \leq \theta_k \leq \hat{\theta}_k\right) = \alpha$$

# Problems with Standard Uncertainty Measures in the SPARROW Model

- Parameters are estimated using non-linear least squares
  - Estimates of coefficient error are valid only asymptotically (that is, for large sample sizes)
- Errors in model may not be normally distributed
- Predictions are generally not linear functions of the parameters or model errors
  - Analytic derivation of uncertainty measures is intractable
  - Predictions may be biased

# Uncertainty in Parameters vs. Uncertainty in Predictions

- Uncertainty in Parameters

Objective function:

$$S = \sum_{i=1}^N (y_i - f_i(\theta))^2$$

Covariance Matrix:

$$V(\hat{\theta}) = s^2 \left( \sum_{i=1}^N f_{i,\theta} f'_{i,\theta} \right)^{-1}$$

# Bootstrap Variance

- The bootstrap method computes  $B$  estimates of  $\theta$ , call them  $\hat{\theta}_b$ ,  $b = 1, \dots, B$ , by minimizing:

$$S^b = \sum_{i=1}^N w_i^b (y_i - f_i(\theta))^2$$

where  $w_i^b$  are integer random weights that sum to  $N$ .

# Bootstrap Variance

$$V(\hat{\theta}_k)^* = \frac{1}{B} \sum_{b=1}^B \left( \hat{\theta}_{k,b} - \hat{\theta}_k^* \right)^2$$

where,  $\hat{\theta}_k^* = \frac{1}{B} \sum_{b=1}^B \hat{\theta}_{k,b}$

# Parametric Confidence Intervals

$$\hat{\theta}_{k-} = \hat{\theta}_k - \sqrt{V(\hat{\theta}_k)}\Phi^{-1}((1 + \alpha)/2), \text{ and}$$
$$\hat{\theta}_{k+} = \hat{\theta}_k + \sqrt{V(\hat{\theta}_k)}\Phi^{-1}((1 - \alpha)/2)$$

where  $\Phi^{-1}$  is the inverse standard normal distribution

This confidence interval is second order accurate.

# Bootstrap Confidence Intervals

$$\hat{\theta}_{k-}^* = \hat{\theta}_k - H^{*-1}((1 + \alpha)/2), \text{ and}$$

$$\hat{\theta}_k^* = \hat{\theta}_k - H^{*-1}((1 - \alpha)/2)$$

where  $H^{*-1}(p)$  is the  $p^{\text{th}}$  quantile of the empirical distribution of  $\hat{\theta}_{k,b} - \hat{\theta}$

This confidence interval is also second order accurate.

# Uncertainty in Predictions

- Parametric Prediction

$$c = g(\theta, \varepsilon)$$

If  $P_\varepsilon(z)$  and  $\theta$  were known, the prediction of  $c$  would be

$$\bar{c} = \int g(\theta, z) dP_\varepsilon(z)$$

# Parametric Prediction – Stage 1

Use coefficient estimates and estimated errors

$$\hat{c} = \frac{1}{N} \sum_{i=1}^N g(\hat{\theta}, \hat{\varepsilon}_i)$$

Because of non-linearity of  $g$ , this estimate is biased.  
Assume proportional bias:

$$\beta = \frac{E[\hat{c}]}{\bar{c}}$$

# Bootstrap Method for the Correction of Proportional Bias

Bootstrap resampled iteration  $b$  prediction  $\hat{c}_b = \frac{1}{N} \sum_{i=1}^N g(\hat{\theta}_b, \hat{\varepsilon}_i)$

and mean  $\overline{\hat{c}_b} = \frac{1}{B} \sum_{b=1}^B \hat{c}_b$

Bootstrap estimated bias  $\beta^* = \frac{\overline{\hat{c}_b}}{\hat{c}}$

Bias corrected estimate of  $c$   $\hat{c}_{BC} = \frac{\hat{c}}{\beta^*} = \frac{\hat{c}^2}{\overline{\hat{c}_b}} > 0$

# Variance Estimate

$$\hat{V}[c - \hat{c}_{BC}] = \frac{1}{N} \sum_{i=1}^N g(\hat{\theta}, \hat{\varepsilon}_i)^2 - \hat{c}^2 + \frac{\frac{1}{B} \sum_{b=1}^B (\hat{c}_b - \overline{\hat{c}_b})^2}{\beta^*}$$

# Bootstrap Prediction Interval

$$\text{Lowerbound} = \hat{c} \exp\left(-H_{\hat{c}_b^* - \hat{c}}^{-1} \left(\frac{1 + \alpha}{2}\right)\right)$$

$$\text{Upperbound} = \hat{c} \exp\left(-H_{\hat{c}_b^* - \hat{c}}^{-1} \left(\frac{1 - \alpha}{2}\right)\right)$$

where  $\hat{c}^* = g(\hat{\theta}, \hat{\varepsilon}^*)$ ,  $\hat{\varepsilon}^*$  is a randomly-selected residual from among the  $N$  residuals obtained in the original full model calibration, and  $H_{\hat{c}_b^* - \hat{c}}^{-1}(x)$  is the empirical distribution of  $\ln(\hat{c}_b^*) - \ln(\hat{c}^*)$

This prediction interval is first order accurate and strictly positive.

# SPARROW Model

## Applications: Other issues

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- Model uncertainty in predictions
- Web access to SPARROW applications

# SPARROW WEB

## Watershed Data and Model Predictions for 62,000 Stream Reaches

- Mean-annual streamflow, water velocity, drainage area
- NLCD land use (1992)
- Population, waste disposal type (1990 Census)
- Mean-annual nutrient conditions (yield, concentration, sources, prediction uncertainties)
- Natural background nutrient conditions
- Public release: 2003



Example of Nested Hydrologic Units in the Mid Atlantic Region 02



Subregion 0207



Accounting Unit 020700



Cataloging Unit 02070000

